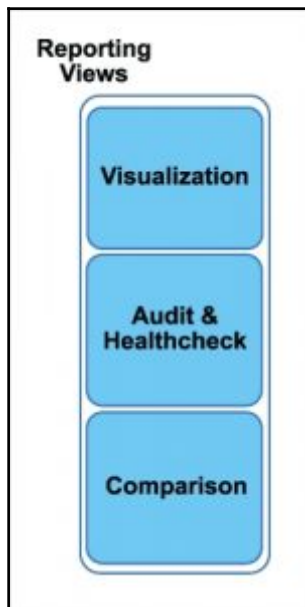
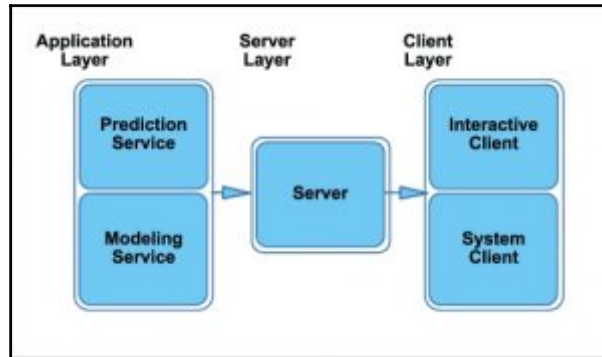
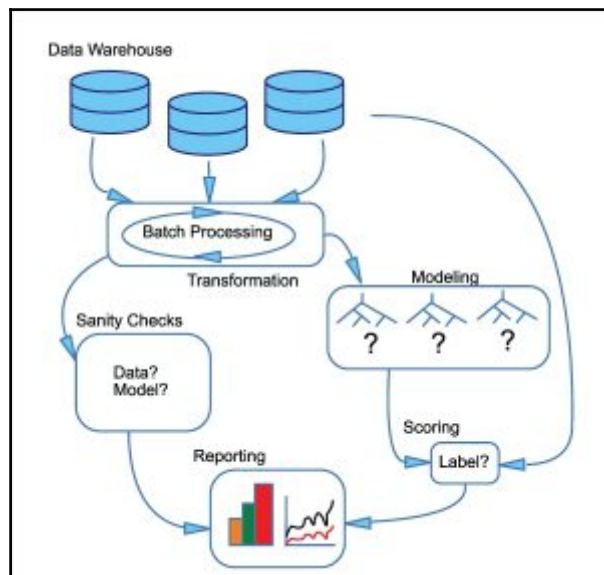
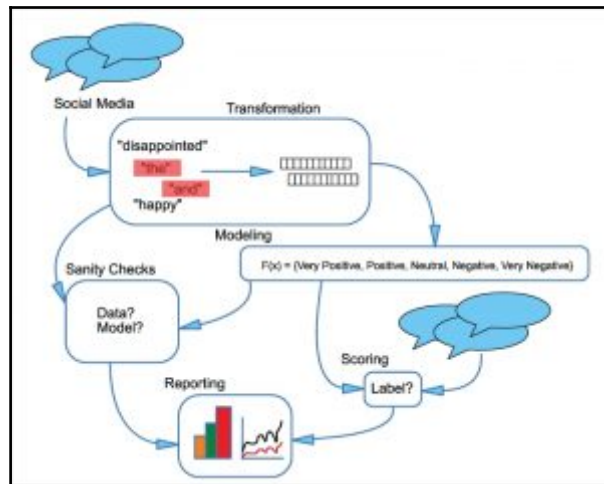
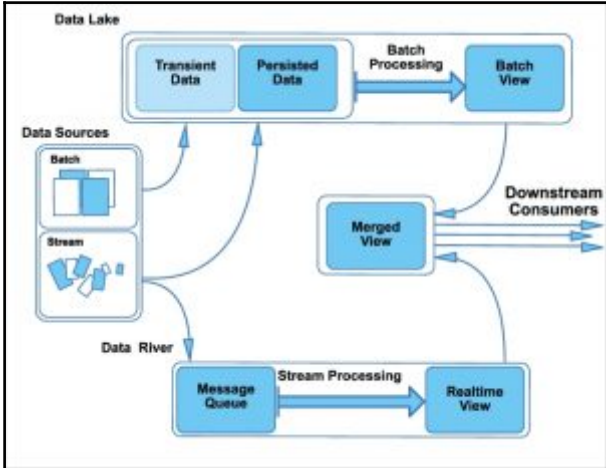
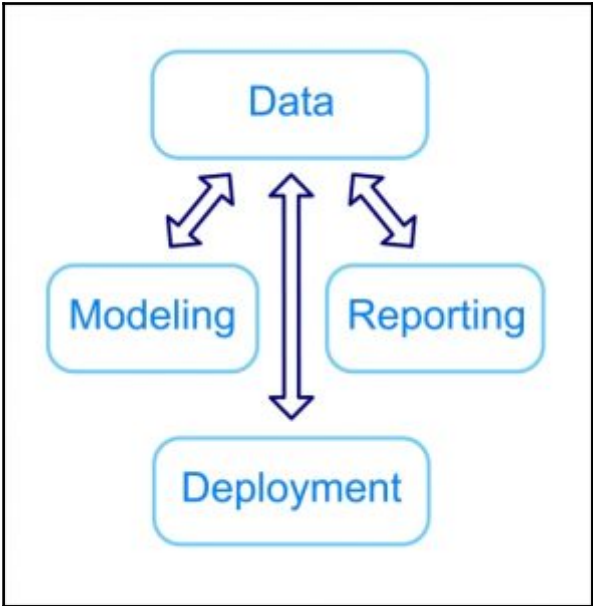
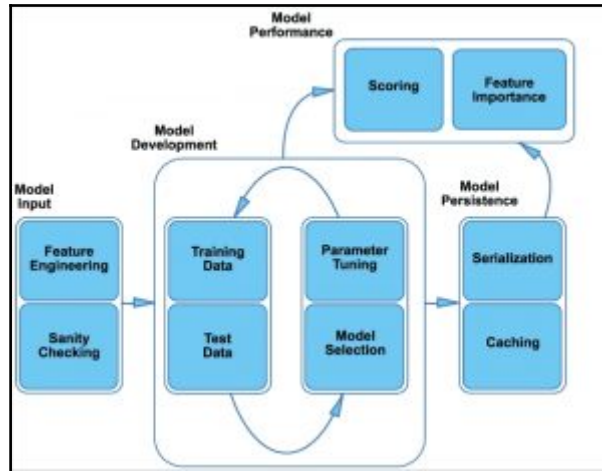


Chapter 1: From Data to Decisions – Getting Started with Analytic Applications









Chapter 2: Exploratory Data Analysis and Visualization in Python

	Unnamed: 0	year	length	budget	rating	votes	r1
count	58788.000000	58788.000000	58788.000000	5.219000e+03	58788.000000	58788.000000	58788.000000
mean	29394.500000	1976.130582	82.337875	1.341251e+07	5.902890	632.130384	7.014382
std	18970.77815	23.735125	44.347717	2.335028e+07	1.553031	3829.621413	10.806799
min	1.000000	1883.000000	1.000000	0.000000e+00	1.000000	5.000000	0.000000
25%	14697.750000	1958.000000	74.000000	2.500000e+05	5.000000	11.000000	0.000000
50%	29394.500000	1983.000000	90.000000	3.000000e+06	6.100000	30.000000	4.500000
75%	44091.250000	1997.000000	100.000000	1.500000e+07	7.000000	112.000000	4.500000
max	58788.000000	2005.000000	5220.000000	2.000000e+08	10.000000	157698.000000	100.000000

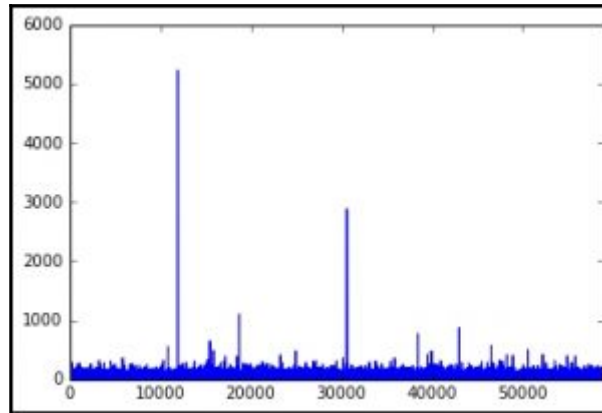
```
Unnamed: 0      int64
title           object
year            int64
length          int64
budget          float64
rating          float64
votes           int64
r1              float64
r2              float64
r3              float64
r4              float64
r5              float64
r6              float64
r7              float64
r8              float64
r9              float64
r10             float64
mpaa            object
Action          int64
Animation       int64
Comedy          int64
Drama           int64
Documentary     int64
Romance         int64
Short           int64
dtype: object
```

```
0      1971
1      1939
2      1941
3      1996
4      1975
Name: year, dtype: int64
```

2002	2168
2003	2158
2001	2121
2000	2048
2004	1945
1999	1927
1998	1705
1997	1568
1996	1390
1995	1248
1994	1199
1993	1016
1987	957
1992	948
1989	944
1988	944
1990	899
1991	888
1985	792
1986	792
1984	749

	Year	Oil prices in constant 1997 dollars, 1870-1997
123	1993	17.15
124	1994	18.27
125	1995	19.40
126	1996	20.52
127	Oil prices in constant 1997 dollars, 1870-1997	NaN

	Unnamed: 0	title	year	length	budget	rating	votes	r1	r2	r3	r4	r5	r6	r7	r8	r9	r10	rmas	Action	Animation
6	7	Swindle	2002	93	NaN	5.3	200	4.5	0.0	4.5	-	4.5	14.5	R	1	0				
42	43	'R Xmas	2001	83	NaN	4.9	288	14.5	4.5	4.5	-	4.5	4.5	R	0	0				
122	123	100 Girls	2000	90	NaN	5.8	3349	4.5	4.5	4.5	-	4.5	4.5	R	0	0				
123	124	100 Mile Rule	2002	98	1100000	5.6	161	4.5	4.5	4.5	-	4.5	14.5	R	0	0				
152	153	11:11	2004	95	NaN	4.3	222	14.5	14.5	4.5	-	4.5	14.5	R	0	0				



	Year	Oil_Price_1997_Dollars
0	1870-01-01	58.53
1	1871-01-01	49.09
2	1872-01-01	24.68
3	1873-01-01	16.71
4	1874-01-01	19.86

jupyter

File Running Clusters

Currently running Jupyter processes

Terminates +

There are no terminable running.

Reconnects +

There are no reconnectable running.

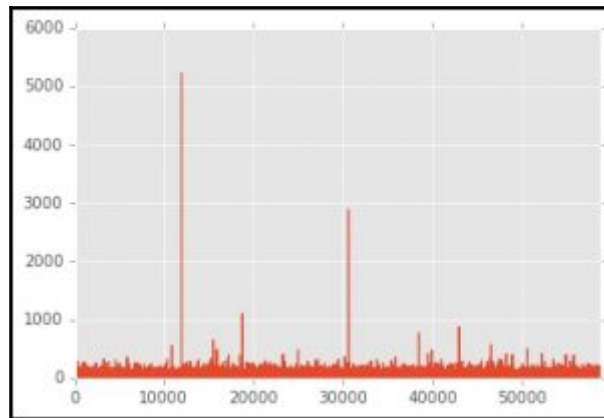
2005	349
2004	1945
2003	2158
2002	2168
2001	2121
2000	2048
1999	1927
1998	1705
1997	1568
1996	1390
1995	1248
1994	1199
1993	1016
1992	948
1991	888
1990	899
1989	944
1988	944
1987	957
1986	792
1985	792
1984	749
1983	698
1982	689

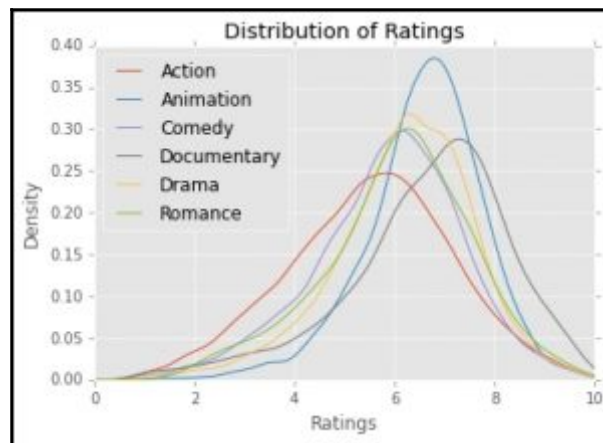
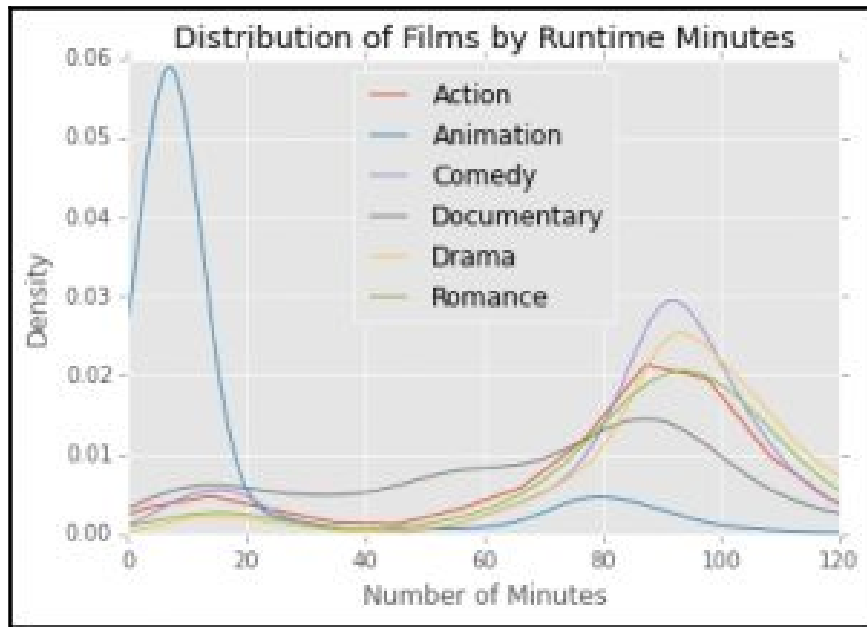
	mean	std
year		
1893	7.000000	NaN
1894	4.888889	0.727056
1895	5.500000	0.624500
1896	5.269231	1.325635
1897	4.677778	0.732765
1898	5.040000	0.950263
1899	4.277778	0.713754
1900	4.731250	1.358783
1901	4.682143	1.081513
1902	4.900000	1.615549
1903	4.808108	1.334662
1904	4.223810	1.291588
1905	5.047059	1.196410
1906	5.676471	1.274034

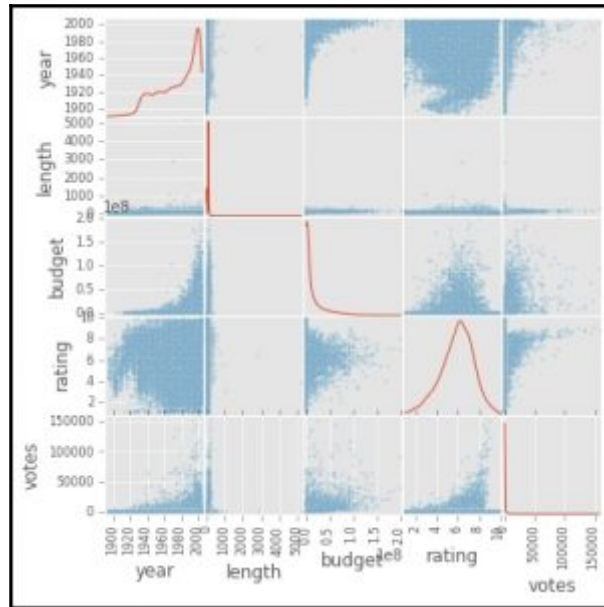
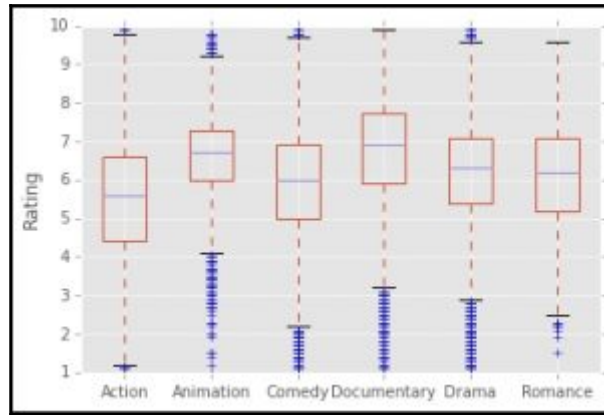
0	Comedy
1	Comedy
2	Animation
3	Comedy
4	Action

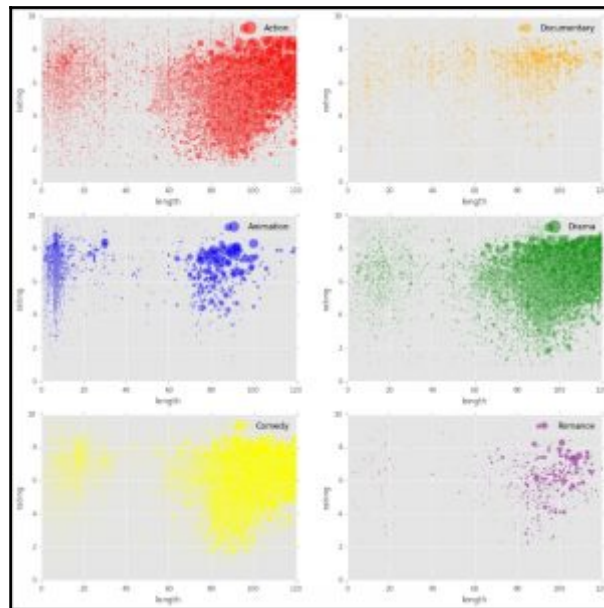
0	yellow
1	yellow
2	blue
3	yellow
4	red

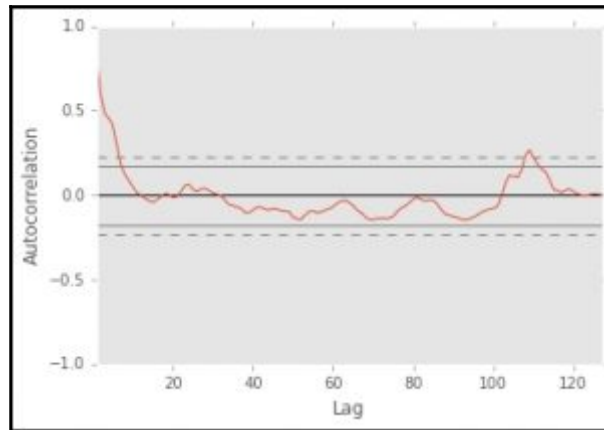
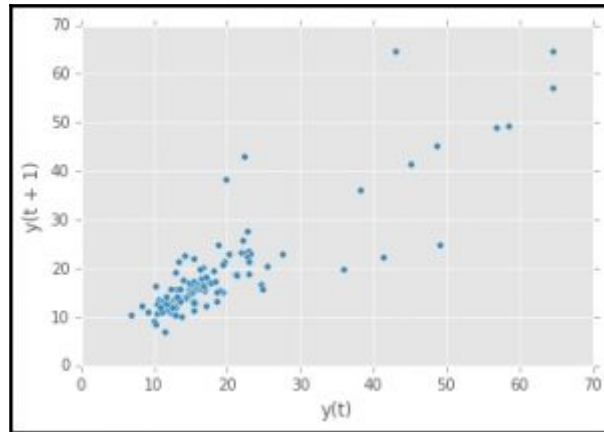
genre	Action	Animation	Comedy	Documentary	Drama	Romance
year						
1893	7.000000	NaN	NaN	NaN	NaN	NaN
1894	5.100000	NaN	NaN	4.720000	NaN	NaN
1895	5.700000	NaN	NaN	5.400000	NaN	NaN
1896	5.875000	NaN	3.900000	5.571429	2.100000	NaN
1897	5.900000	NaN	5.200000	4.300000	NaN	NaN
1898	6.000000	NaN	5.050000	5.500000	3.600000	NaN
1899	4.533333	NaN	3.600000	3.866667	4.850000	NaN



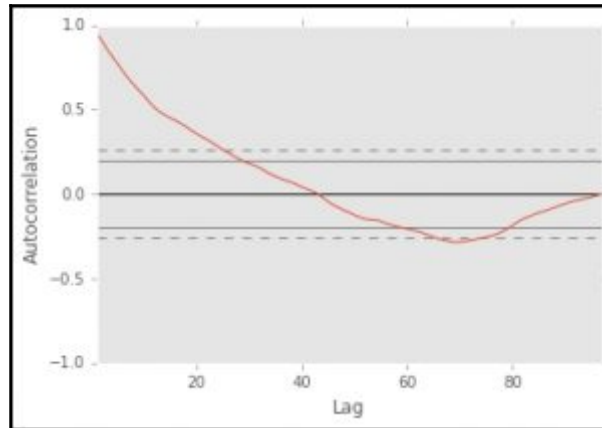
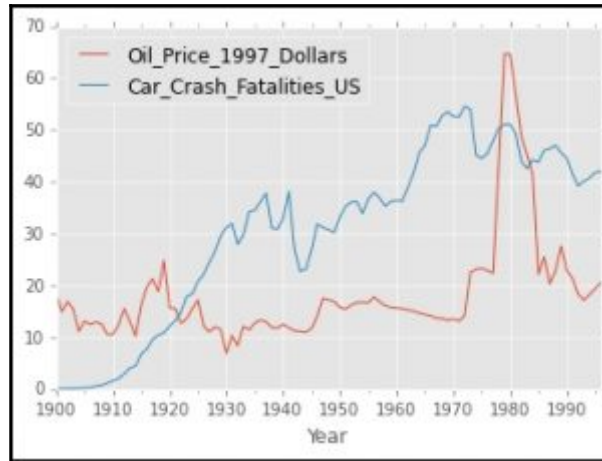




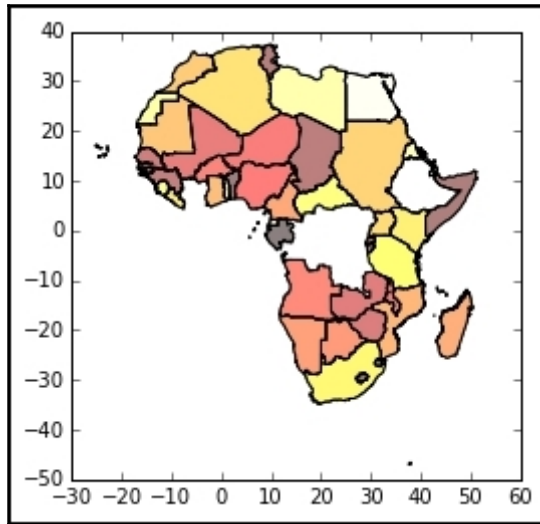
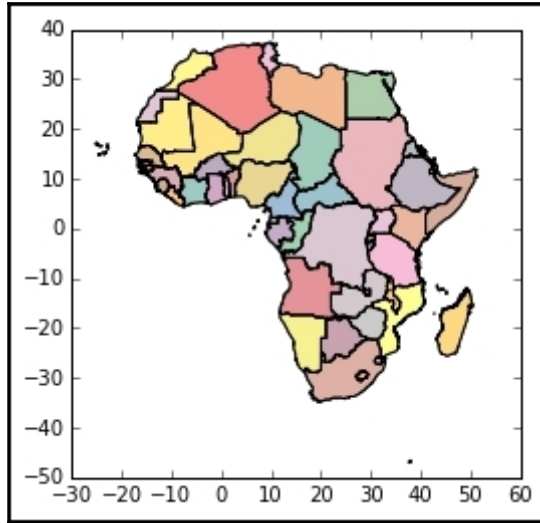




	Year	Car_Crash_Fatalities_US
0	1900-01-01	36
1	1901-01-01	54
2	1902-01-01	79
3	1903-01-01	117
4	1904-01-01	172



	CODE	COUNTRY	ID	geometry
0	ALG	Algeria	1	POLYGON ((-5.76361999999979 25.586249999999302, ...
1	ANG	Angola	2	POLYGON ((13.36632442474365 -8.32172966003418, ...
2	ANG	Angola	3	POLYGON ((12.80576000000292 -4.806490000002668, ...
3	ANG	Angola	4	POLYGON ((11.76834011077881 -16.79932975769043, ...
4	ANG	Angola	5	POLYGON ((12.89840030670166 -5.988018989552988, ...




```

2015/05/17 20:58:36 INFO SparkContext: Running Spark version 1.5.0
2015/05/17 20:58:36 INFO SecurityManager: Changing view acls to: jhdoback
2015/05/17 20:58:36 INFO SecurityManager: Changing modify acls to: jhdoback
2015/05/17 20:58:36 INFO SecurityManager: SecurityManager: authentication disabled; ui acls disabled; users with view permission: Set(jhdoback); users with modify permissions: Set(jhdoback)
2015/05/17 20:58:36 INFO LifeJuggler: LifeJuggler started
2015/05/17 20:58:36 INFO Resolving: Starting resolving
2015/05/17 20:58:36 INFO Resolving: Resolving started; listening on addresses: (jhdoback,http://spark@driver:localhost:9821)
2015/05/17 20:58:36 INFO Utils: Successfully started service 'spark@driver' on port 9821.
2015/05/17 20:58:36 INFO SparkView: Registering WebOutputTracker
2015/05/17 20:58:36 INFO SparkView: Registering FloodManagerMaster
2015/05/17 20:58:36 INFO ShuffleBlockManager: Created local directory at /private/var/folders/mw/gf7_2ed36d_81hc56-44baqjxrs6/T/fockag-817826-e-6764-4247-8b68-82e11326823
2015/05/17 20:58:36 INFO MemoryStore: MemoryStore started with capacity 504.1 MB
2015/05/17 20:58:36 INFO straffilerServer: HTTP File server directory is /private/var/folders/mw/gf7_2ed36d_81hc56-44baqjxrs6/T/spark-6c29ff77-5730-4691-cc8d-638d344c36/httpd-6cc28201-7c48-43dd-926a-654606a1181e
2015/05/17 20:58:36 INFO HttpServer: Starting HTTP Server
2015/05/17 20:58:36 INFO Server: Jetty-8.y.a-SMP500T
2015/05/17 20:58:36 INFO AbstractConnector: Started SocketConnector@0.0.0.0:9820
2015/05/17 20:58:36 INFO Utils: Successfully started service 'HTTP file server' on port 9820.
2015/05/17 20:58:36 INFO SparkView: Registering OutputCommitCoordinator
2015/05/17 20:58:36 INFO Server: Jetty-8.y.a-SMP500T
2015/05/17 20:58:36 INFO AbstractConnector: Started SelectChannelConnector@0.0.0.0:8888
2015/05/17 20:58:36 INFO Utils: Successfully started service 'SparkUI' on port 8888.
2015/05/17 20:58:36 INFO SparkUI: Started SparkUI at http://localhost:8888
2015/05/17 20:58:36 WARN MetricsSystem: Using default case DAGScheduler for source because spark.app.id is not set.
2015/05/17 20:58:36 INFO Executor: Starting executor ID driver on host localhost
2015/05/17 20:58:36 INFO Utils: Successfully started service 'org.apache.spark.network.netty.NettyBlockTransferService' on port

```



```

Index([Unnamed: 0', 'title', 'year', 'length', 'budget', 'rating', 'votes',
      'r1', 'r2', 'r3', 'r4', 'r5', 'r6', 'r7', 'r8', 'r9', 'r10', 'mpaa',
      'Action', 'Animation', 'Comedy', 'Drama', 'Documentary', 'Romance',
      'Short'],
      dtype='object')

```

$$K(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

$$f(x) = \frac{1}{nh} \sum_{i=1}^n K\left(\frac{x-x_i}{h}\right)$$

Year	object
Oil prices in constant 1997 dollars. 1870-1997	float64
dtype: object	

```

[12:36:21.313 kernel@qtp] Serving notebooks from local directory: /Users/gabecoo/OneDrive/Marketing_Predictive_Anal
[12:36:21.313 kernel@qtp] 0 active kernels
[12:36:21.313 kernel@qtp] The Jupyter Notebook is running at: http://localhost:8888/
[12:36:21.313 kernel@qtp] Use Control-C to stop this server and shut down all kernels (twice to skip confirmation)

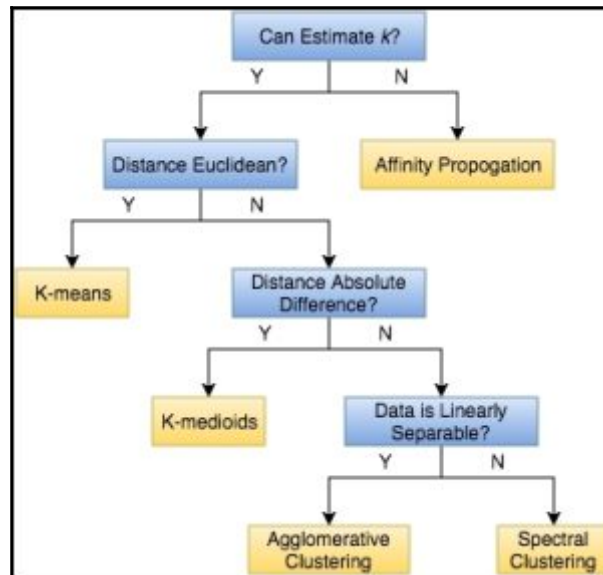
```



Unnamed: 0	title	year	length	budget	rating	votes	r1	r2	r3	...	r9	r10	mpaa	Action
0 1	\$	1971	121	NaN	6.4	368	4.5	4.5	4.5	...	4.5	4.5	NaN	0
1 2	\$1000 a Touchdown	1939	71	NaN	6.0	20	0.0	14.5	4.5	...	4.5	14.5	NaN	0
2 3	\$21 a Day Once a Month	1941	7	NaN	6.2	5	0.0	0.0	0.0	...	24.5	24.5	NaN	0
3 4	\$40,000	1996	70	NaN	6.2	6	14.5	0.0	0.0	...	34.5	45.5	NaN	0
4 5	\$50,000 Climax Show, The	1975	71	NaN	3.4	17	24.5	4.5	0.0	...	0.0	24.5	NaN	0

Unnamed: 0	title	year	length	budget	rating	votes	r1	r2	r3
58773	58774 deadend.com	2002	120	NaN	6.9	53	64.5	4.5	0.0
58774	58775 e-Dreams	2001	94	NaN	6.8	95	4.5	0.0	0.0
58775	58776 eMale	2001	17	NaN	7.3	15	0.0	0.0	0.0
58776	58777 eRATice	2003	9	NaN	6.0	5	0.0	0.0	0.0
58777	58778 eXXXorclimas	2002	78	NaN	4.2	11	34.5	0.0	0.0
58778	58779 eXstenZ	1999	97	NaN	6.7	14742	4.5	4.5	4.5
58779	58780 GpointB	2002	20	NaN	5.0	13	4.5	0.0	4.5
58780	58781 It	2001	13	NaN	7.6	7	0.0	0.0	0.0
58781	58782 pJRe kILLjoy	1996	67	NaN	5.2	6	0.0	14.5	14.5
58782	58783 sDney	2002	16	NaN	7.0	8	14.5	0.0	0.0
58783	58784 tom thumb	1958	98	NaN	6.5	274	4.5	4.5	4.5
58784	58785 www.XXX.com	2003	105	NaN	1.1	12	45.5	0.0	0.0
58785	58786 www.hellsoapopera.com	1999	100	NaN	6.6	5	24.5	0.0	24.5

Chapter 3: Finding Patterns in the Noise – Clustering and Unsupervised Learning



$$r(i, k) = s(i, k) - \max_{k' \neq k} \{a(i, k') + s(i, k')\}$$

$$a(i, k) = \min \left(0, r(k, k) + \sum_{i' \in \{i, k\}} \max(0, r(i', k)) \right)$$

$$a(k, k) = \sum_{i' \in \{i, k\}} \max(0, r(i', k))$$

$$e^{-\gamma D(x_i, x_j)^2}$$

$$L = I - D^{1/2} K D^{1/2}$$

$$D_{ii} = \sum_{j=1}^n K_{ij}$$

$$Av = \lambda v$$

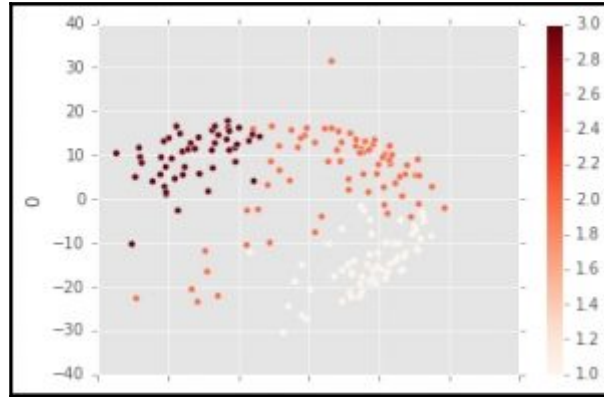
$$\begin{bmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{bmatrix}$$

	0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	1	14.23	1.71	2.43	15.6	127	2.80	3.06	0.28	2.29	5.64	1.04	3.92	1065
1	1	13.20	1.78	2.14	11.2	100	2.65	2.76	0.26	1.28	4.38	1.05	3.40	1050
2	1	13.16	2.36	2.67	18.6	101	2.80	3.24	0.30	2.81	5.68	1.03	3.17	1185
3	1	14.37	1.95	2.50	16.8	113	3.85	3.49	0.24	2.18	7.80	0.86	3.45	1480
4	1	13.24	2.59	2.87	21.0	118	2.80	2.69	0.39	1.82	4.32	1.04	2.93	735

	Class	Alcohol	Maleic	Ash	Alcalinity	Magnesium	Total	Flavonoids
count	178.000000	178.000000	178.000000	178.000000	178.000000	178.000000	178.000000	178.000000
mean	1.938202	13.000818	2.336348	2.366517	19.494944	98.741573	2.295112	2.026270
std	0.775035	0.811827	1.117146	0.274344	3.339564	14.282484	0.625851	0.998659
min	1.000000	11.000000	0.740000	1.360000	10.600000	70.000000	0.980000	0.340000
25%	1.000000	12.362500	1.602500	2.210000	17.200000	88.000000	1.742500	1.205000
50%	2.000000	13.060000	1.866000	2.360000	19.500000	98.000000	2.355000	2.135000
75%	3.000000	13.677500	3.062500	2.567500	21.500000	107.000000	2.800000	2.875000
max	3.000000	14.830000	5.800000	3.230000	30.000000	162.000000	3.890000	5.080000

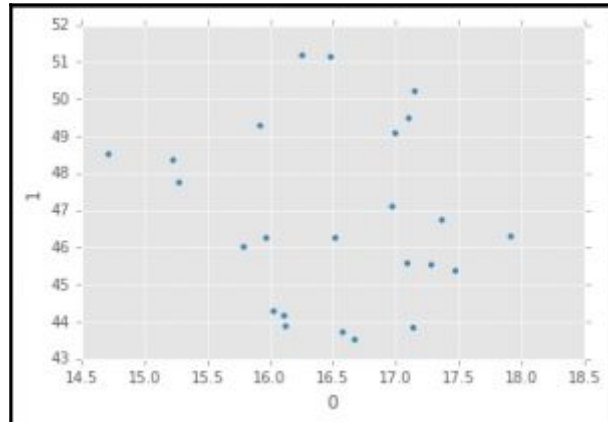
	Alcohol	Maleic	Ash	Alcalinity	Magnesium	Total	Flavonoids
count	1.780000e+02	1.780000e+02	1.780000e+02	1.780000e+02	1.780000e+02	178.000000	1.780000e+02
mean	-8.262806e-16	-1.197544e-16	-8.370330e-16	-3.991813e-17	-3.591813e-17	0.000000	-3.591813e-16
std	1.002821e+00	1.002821e+00	1.002821e+00	1.002821e+00	1.002821e+00	1.002821	1.002821e+00
min	-2.434235e+00	-1.432983e+00	-3.679162e+00	-2.671018e+00	-2.088250e+00	-2.107246	-1.886971e+00
25%	-7.882448e-01	-6.587486e-01	-5.721225e-01	-6.891372e-01	-8.244151e-01	-0.885468	-8.275300e-01
50%	6.099986e-02	-4.231120e-01	-2.362130e-02	1.518295e-03	-1.220917e-01	0.099960	1.061467e-01
75%	8.361286e-01	6.697929e-01	6.961066e-01	6.020883e-01	5.096384e-01	0.808997	8.480651e-01
max	2.259772e+00	3.109192e+00	3.156025e+00	3.154911e+00	4.371372e+00	2.539515	3.062802e+00

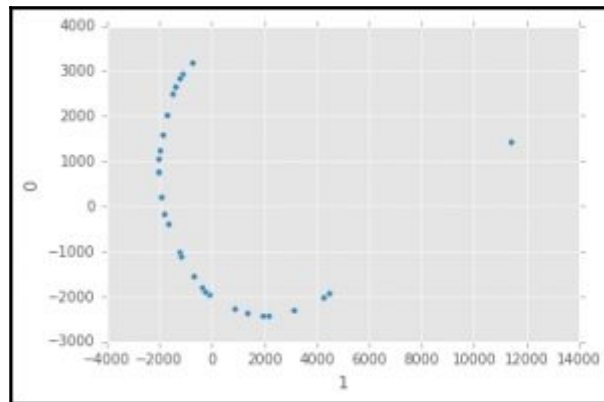
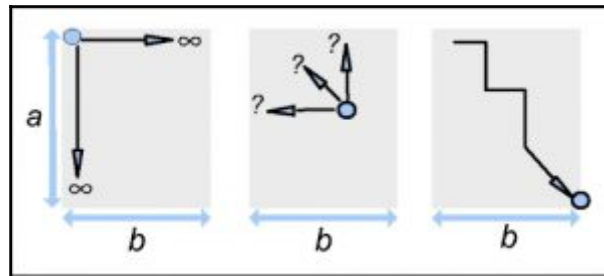
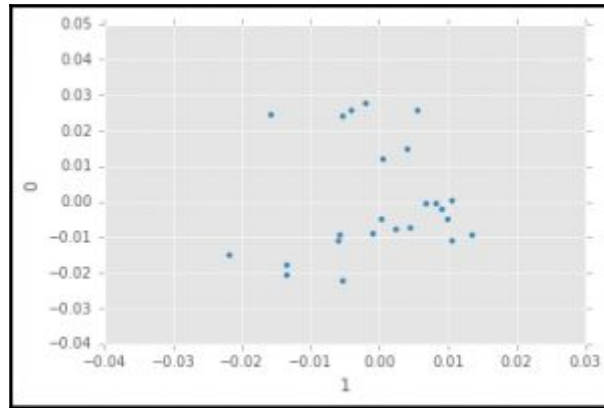
$$D(x, y) = \sqrt{\sum_{i=1}^n (x_i - y_i)^2}$$



	quarter	stock	date	open	high	low	close	volume	percent_change_price
0	1	AA	1/7/2011	\$15.82	\$16.72	\$15.78	\$16.42	239655616	3.78267
1	1	AA	1/14/2011	\$16.71	\$16.71	\$15.84	\$15.97	242963398	-4.42849
2	1	AA	1/21/2011	\$16.19	\$16.38	\$15.80	\$15.79	138428496	-2.47086
3	1	AA	1/28/2011	\$15.87	\$16.63	\$15.82	\$16.13	151379173	1.63831
4	1	AA	2/4/2011	\$16.18	\$17.39	\$16.18	\$17.14	154387761	5.93325

date	stock	2011-01-07 00:00:00	2011-01-14 00:00:00	2011-01-21 00:00:00	2011-01-28 00:00:00	2011-02-04 00:00:00	2011-02-11 00:00:00	2011-02-18 00:00:00	2011-02-25 00:00:00
0	AA	16.42	15.87	15.79	16.13	17.14	17.37	17.28	16.66
1	AXP	44.36	48.25	48.00	43.86	43.82	46.75	45.53	43.53
2	BA	68.38	75.07	71.88	69.23	71.38	72.14	73.04	72.30
3	BAC	14.25	15.25	14.25	13.80	14.29	14.77	14.75	14.20
4	CAF	83.73	84.01	82.75	85.88	89.59	103.54	105.86	102.00



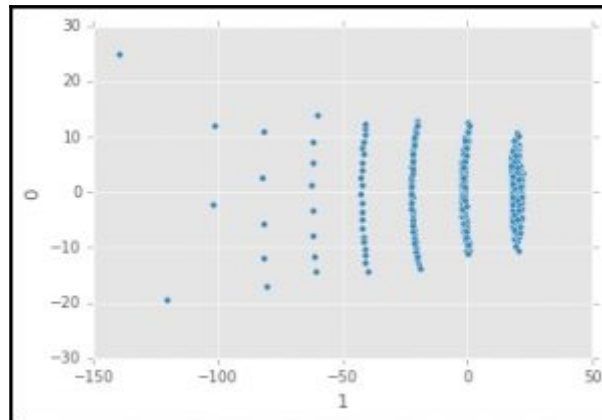


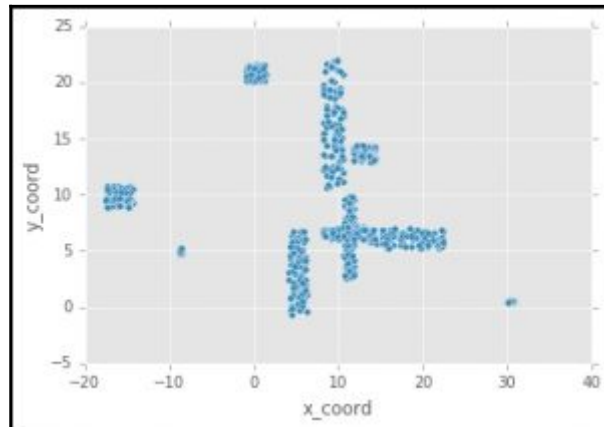
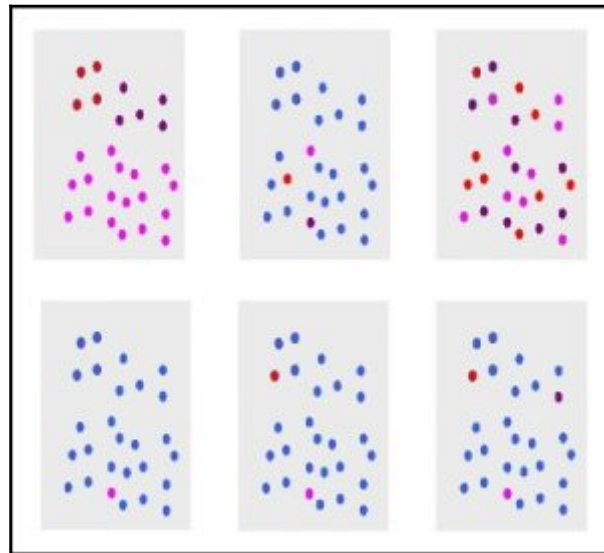
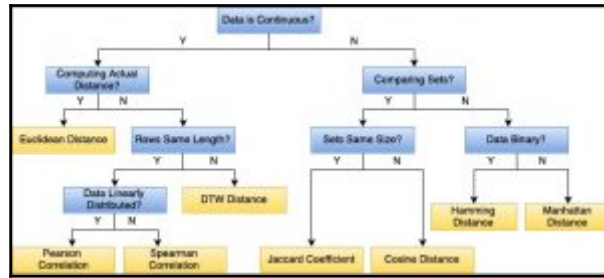
$$P(a,b) = \frac{Cov(a,b)}{\sigma(a)\sigma(b)} = \frac{\frac{1}{n} \sum_{i=1}^n (a_i - \mu(a))(b_i - \mu(b))}{\sqrt{\frac{1}{n} \sum_{i=1}^n (a_i - \mu(a))^2} \sqrt{\frac{1}{n} \sum_{i=1}^n (b_i - \mu(b))^2}}$$

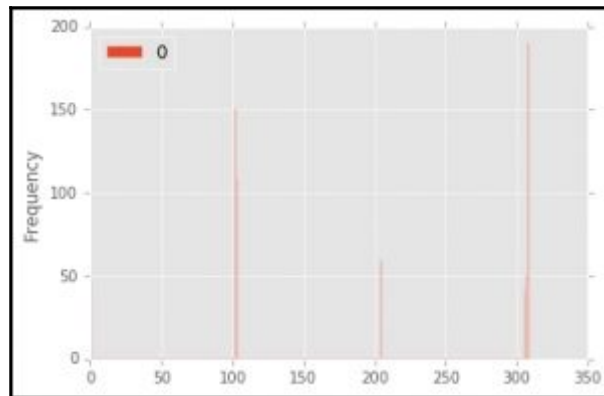
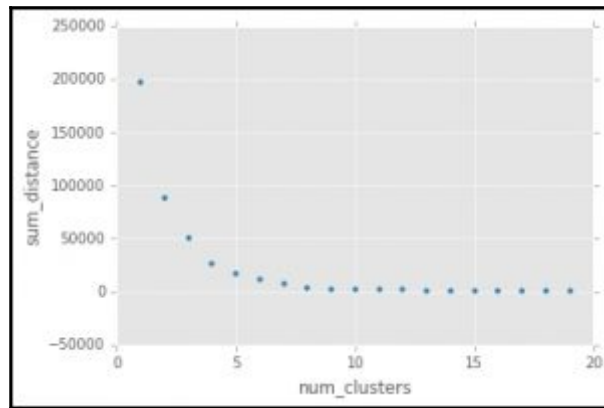
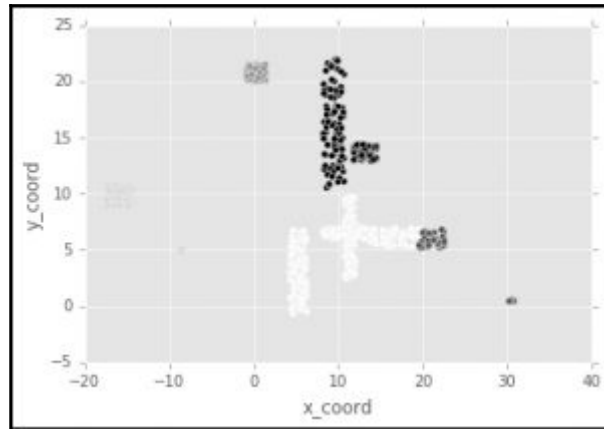
id	authors	groups	keywords	topics	abstract
0	Kemalized Bayesian Transfer Learning Mehmet Gönen and Adam A. Margolin	Novel Machine Learning Algorithms (NMLA)	cross-domain learning/in-domain adaptation/learn...	APP: Biomedical / Bioinformatics/NMLA: Bayes...	Transfer learning considers related but distin...
1	"Source Free" Transfer Learning for Text Class... Zhengqi Lu, Yin Zhu, Simo Park, Evan Xiang, Ye...	AI and the Web (AIW)/Novel Machine Learning A...	Transfer Learning/Auxiliary Data Retrieval/nT...	AIW: Knowledge acquisition from the web/AW: ...	Transfer learning uses relevant auxiliary data...
2	A Generalization of Probabilistic Serial to Ra... Haris Aziz and Paul Sunberg	Game Theory and Economic Paradigms (GTEP)	social choice theory/voting/in-fair division/ra...	GTEP: Game Theory/nGTEP: Social Choice / Voting	The probabilistic serial (PS) rule is one of L...

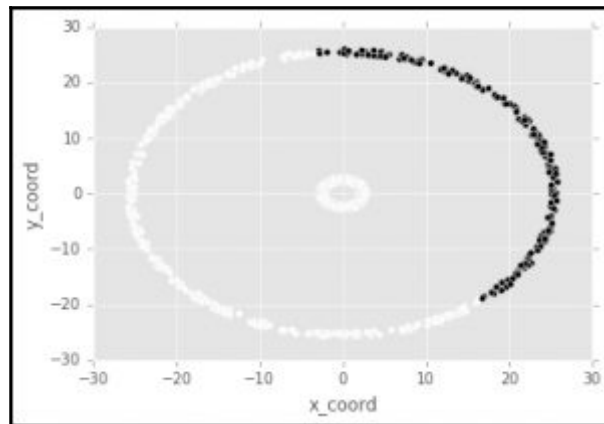
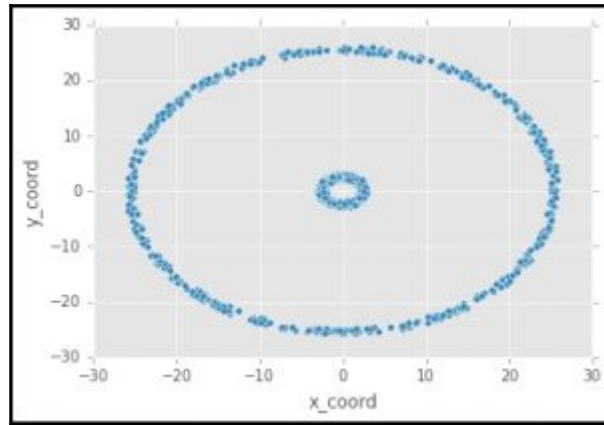
	keyword_452	keyword_1174	keyword_646	keyword_1287	keyword_312	keyword_378	keyword_826	keyword_9
0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0
2	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	0
4	0	0	0	0	0	0	0	0

$$\rho(a, b) = \frac{6 \sum_{i=1}^n d_i^2}{n(n^2 - 1)}$$

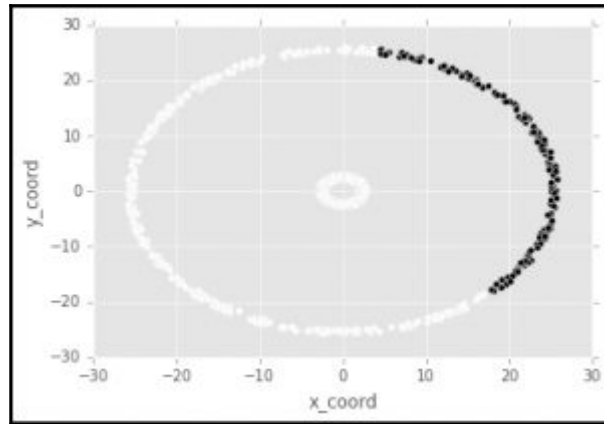








$$J(a,b) = \frac{\|a \cap b\|}{\|a \cap b\|}$$



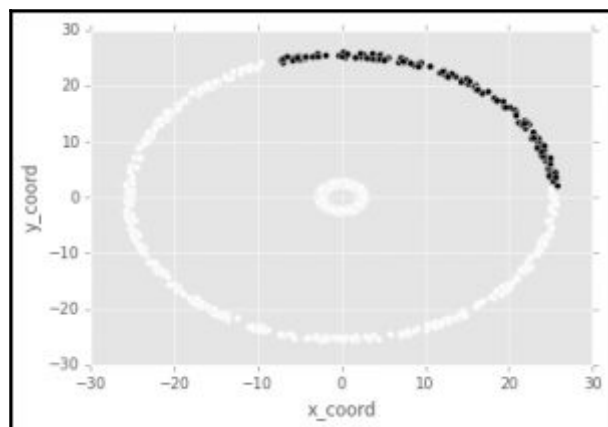
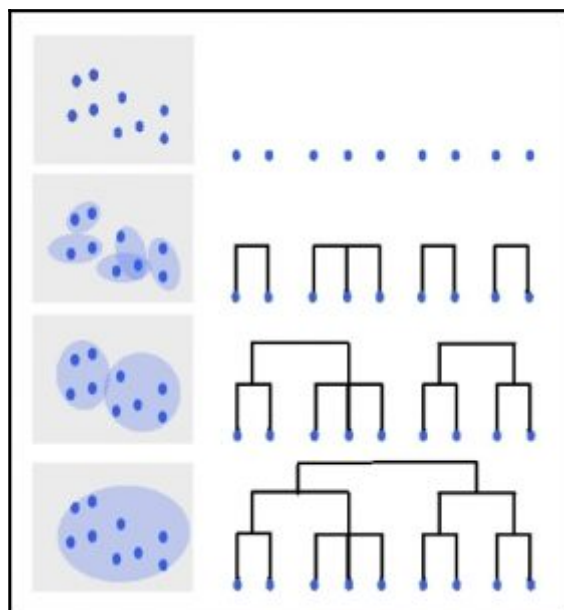
$$\text{Cos}(a,b) = \frac{a \sum b}{\|a\| \|b\|}$$

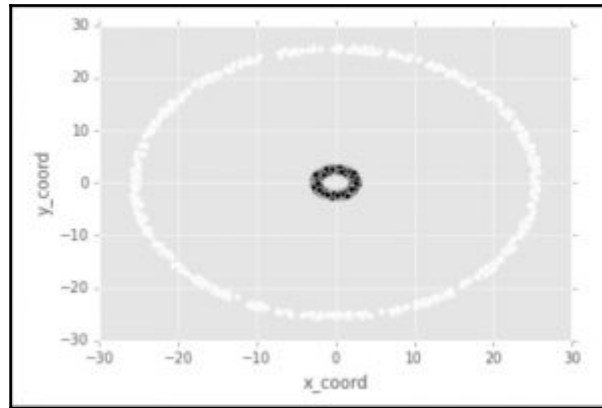
$$\|a\| = \sqrt{\sum_{i=1}^n a_i^2}$$

$$a \sum b = \sum_{i=1}^n a_i b_i$$

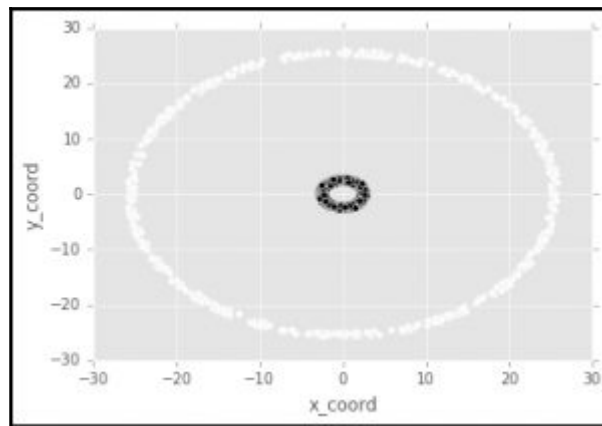
$$H(a,b) = \sum_{i=1}^n 1 \text{ if } a_i = b_i \text{ else } 0$$

$$M(a,b) = \sum_{i=1}^n |a_i - b_i|$$





$$SSE = \sum_{i=1}^n D(x_i, c_i)^2$$



Chapter 4: Connecting the Dots with Models – Regression Methods

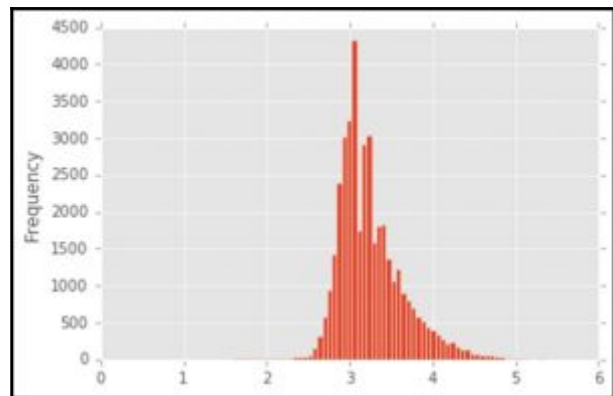
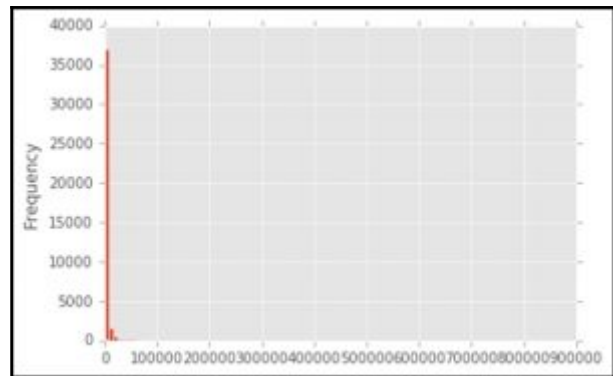
$$VR(L, R) = \frac{1}{|A|^2} \sum_{n \in A} \sum_{n \in A} \frac{1}{2} (y_i - y_j)^2 - \left(\frac{1}{|L|^2} \sum_{n \in L} \sum_{n \in L} \frac{1}{2} (y_i - y_j)^2 + \frac{1}{|R|^2} \sum_{n \in R} \sum_{n \in R} \frac{1}{2} (y_i - y_j)^2 \right)$$

$$IG(L, R) = -\sum_{k=1}^K f_{L_k} \log_2 f_{L_k} - \left(-\alpha \sum_{k=1}^K f_{L_k} \log_2 f_{L_k} + (1-\alpha) \sum_{k=1}^K f_{R_k} \log_2 f_{R_k} \right)$$

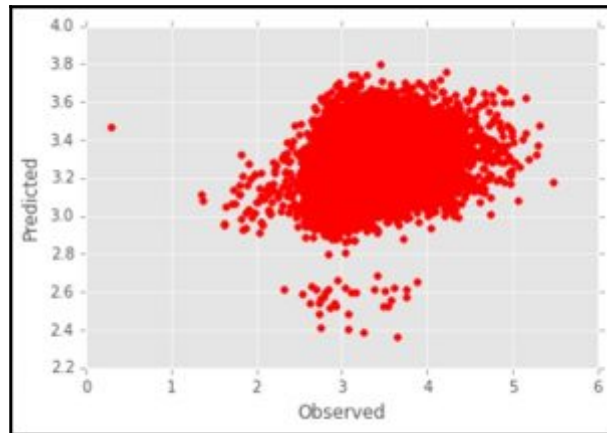
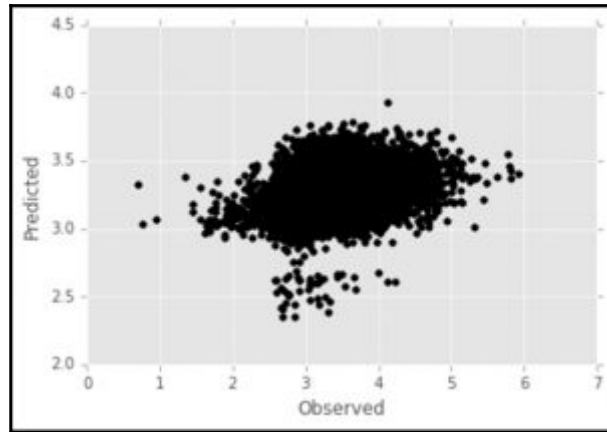
$$GI(L, R) = 1 - \left(\alpha \sum_{k=1}^K f_{L_k}^2 + (1-\alpha) \sum_{k=1}^K f_{R_k}^2 \right)$$

$$GI(L, R) = 1 - \left(\alpha \sum_{k=1}^K f_{L_k}^2 + (1-\alpha) \sum_{k=1}^K f_{R_k}^2 \right)$$

	tfidf_delta	n_tokens_title	n_tokens_content	n_unique_tokens	n_non_stop_words	n_non_stop_unique_tok
count	39644.000000	39644.000000	39644.000000	39644.000000	39644.000000	39644.000000
mean	354.530471	15.388749	548.514731	0.549216	0.899489	0.889175
std	214.163767	2.114037	471.107938	3.520706	5.231231	3.264816
min	0.000000	2.000000	0.000000	0.000000	0.000000	0.000000
25%	164.000000	9.000000	246.000000	0.470970	1.000000	0.825739
50%	306.000000	10.000000	429.000000	0.539026	1.000000	0.895476
75%	542.000000	12.000000	718.000000	0.808696	1.000000	0.754630
max	731.000000	23.000000	8474.000000	701.000000	1042.000000	650.000000



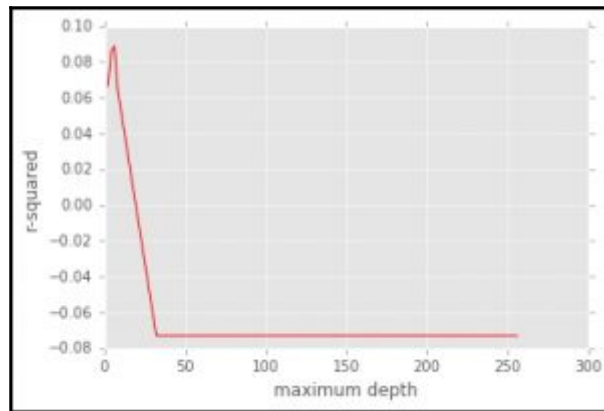
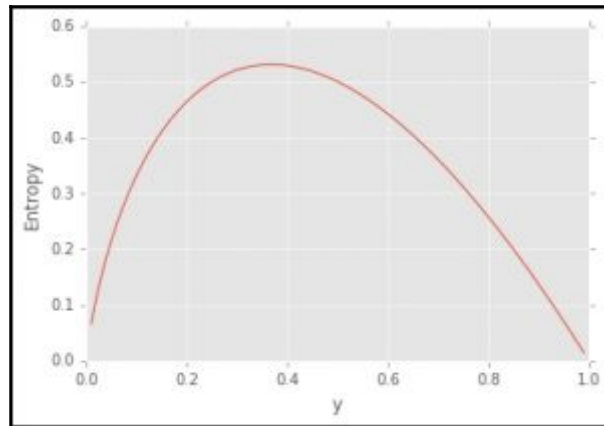
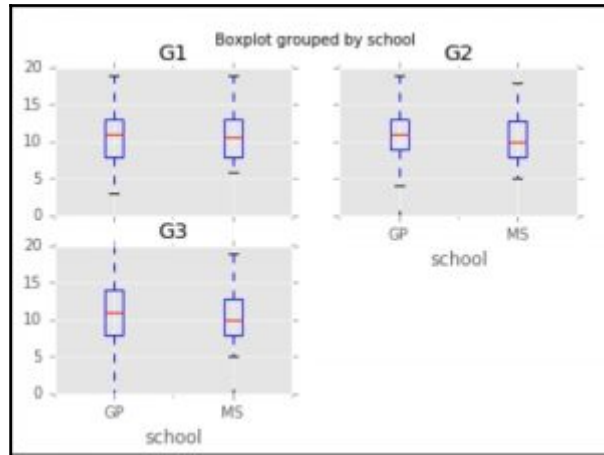
	linedelta	n_tokens_bill	n_tokens_content	n_unique_tokens	n_non_stop_words	n_non_stop_unique_tokens	num_feats
count	28644.000000	28644.000000	28644.000000	28644.000000	28644.000000	28644.000000	28644.000000
mean	0.537730	0.311272	0.542389	0.072893	0.115889	0.086493	0.276788
std	0.052046	0.017781	0.102187	0.016811	0.018287	0.017808	0.087166
min	0.299976	0.169476	0.000000	0.000000	0.000000	0.000000	0.000000
25%	0.507516	0.301000	0.532545	0.067266	0.114287	0.083162	0.330768
50%	0.547687	0.308627	0.567942	0.074867	0.114287	0.082020	0.390818
75%	0.572287	0.325083	0.588583	0.081518	0.114287	0.084888	0.331877
max	0.587385	0.378676	0.602883	0.082477	0.066241	0.081333	0.542118

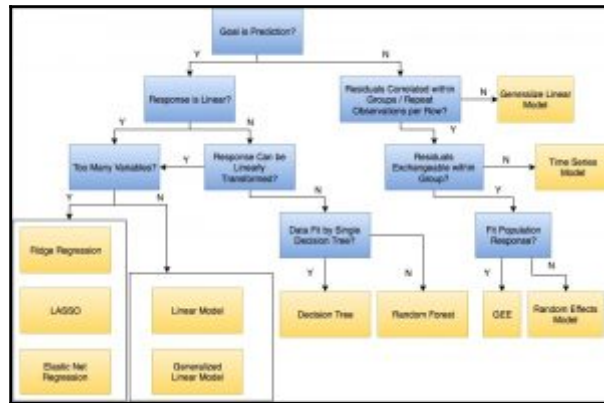
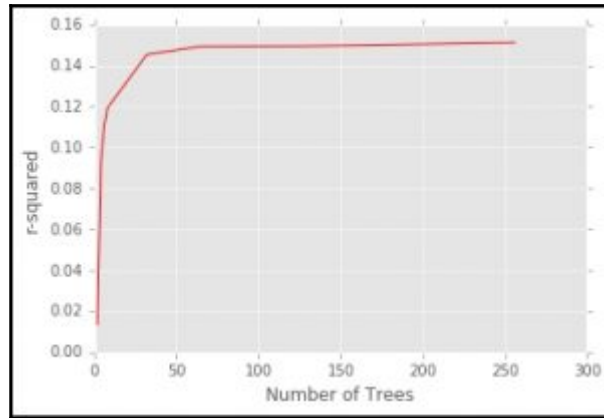


OLS Regression Results			
Dep. Variable:	shares	R-squared:	0.123
Model:	OLS	Adj. R-squared:	0.121
Method:	Least Squares	F-statistic:	98.80
Date:	Mon, 21 Mar 2016	Prob (F-statistic):	0.00
Time:	00:03:53	Log-Likelihood:	-17704.
No. Observations:	39644	AIC:	3.552e+04
Df Residuals:	39587	BIC:	3.601e+04
Df Model:	56		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[95.0% Conf. Int.]
timedelta	0.0142	0.006	2.322	0.020	0.002 0.026
n_tokens_title	0.0640	0.024	2.626	0.009	0.016 0.112
n_tokens_content	-0.0897	0.020	-4.451	0.000	-0.129 -0.050
n_unique_tokens	-1.3315	0.320	-4.164	0.000	-1.958 -0.705
n_non_stop_words	0.8054	0.215	3.740	0.000	0.383 1.228
n_non_stop_unique_tokens	0.5612	0.233	2.411	0.016	0.105 1.017
num_hrefs	0.0973	0.008	11.474	0.000	0.081 0.114
num_self_hrefs	-0.1083	0.011	-9.649	0.000	-0.130 -0.086
num_imgs	0.0487	0.006	7.981	0.000	0.037 0.061
num_videos	0.0667	0.008	8.620	0.000	0.052 0.082
average_token_length	-0.2459	0.103	-2.390	0.017	-0.448 -0.044
num_keywords	0.1209	0.024	5.130	0.000	0.075 0.167
data_channel_is_lifestyle	-0.0592	0.013	-4.545	0.000	-0.085 -0.034
data_channel_is_entertainment	-0.1166	0.008	-14.059	0.000	-0.133 -0.100

Omnibus:	7432.190	Durbin-Watson:	1.940
Prob(Omnibus):	0.000	Jarque-Bera (JB):	19103.164
Skew:	1.030	Prob(JB):	0.00
Kurtosis:	5.705	Cond. No.	3.16e+03





$$\begin{aligned}
I &= (X^T X)^{-1} A \\
L(\beta) &= \sum_{i=1}^n (y_i - X_i \beta)^2 \\
R^2 &= \left(\frac{\text{Cov}(\text{predicted}, \text{observed})}{\sqrt{\text{Var}(\text{predicted}) \text{Var}(\text{observed})}} \right)^2 \\
R_{adj}^2 &= R^2 - \left(\frac{p}{n-p-1} \right) (1-R^2) \\
L(\beta) &= \prod_{i=1}^n \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(y_i - X_i \beta - \mu)^2}{2\sigma^2}} \\
\log(L(\beta)) &= -\frac{1}{\sigma \sqrt{2\pi}} \sum_{i=1}^n \frac{(y_i - X_i \beta - \mu)^2}{2\sigma^2} \\
2n - 2 \ln(L(\beta)) &= -2L(\beta) + n \ln(n) \\
y &= X\beta \\
U(\beta) &= \sum_{i=1}^n \frac{\partial U_i}{\partial \beta_j} V_i^{-1}(y_i - \mu_i(\beta)) \\
y &= X\beta + \epsilon \\
y &= X\beta + Zu + \epsilon \\
x_i &= F_i x_{i-1} + \beta u_i + w_i \\
y_i &= H_i x_i + v_i \\
G(Y) &= X\beta + \epsilon \\
L(\beta) &= \sum_{i=1}^n (y_i - X_i \beta)^2 + \alpha \sum_{i=1}^n \beta_i^2 \\
L(\beta) &= \sum_{i=1}^n (y_i - X_i \beta)^2 + \alpha \sum_{i=1}^n |\beta_i| \\
L(\beta) &= \sum_{i=1}^n (y_i - X_i \beta)^2 + \alpha \sum_{i=1}^n \beta_i^2 + \alpha_0 \sum_{i=1}^n |\beta_i|
\end{aligned}$$

$$\begin{aligned}
y &= X\beta \\
X^T y &= X^T X \beta \\
\beta &= \frac{X^T y}{(X^T X)^{-1}}
\end{aligned}$$

$$I = (X^T X)^{-1} A$$

$$L(\beta) = \sum_{i=1}^n (y - \hat{y})^2 = \sum_{i=1}^n (y - X\beta)^2$$

$$y = X\beta$$

$$\sum_{i=1}^n (y - X\beta)^2$$

$$R^2 = \left(\frac{\text{Cov}(\text{predicted}, \text{observed})}{\text{Var}(\text{predicted})\text{Var}(\text{observed})} \right)^2$$

$$R_{adj}^2 = R^2 - \left(\frac{p}{n - p - 1} \right) (1 - R^2)$$

$$L(\beta) = \prod_{i=1}^n \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{((y_i - x_i\beta) - \mu)^2}{2\sigma^2}}$$

$$\text{Log}(L(\beta)) = \frac{1}{\sigma\sqrt{2\pi}} \sum_{i=1}^n \frac{((y_i - x_i\beta) - \mu)^2}{2\sigma^2}$$

$$2m - 2\ln(L(\beta))$$

$$-2L(\beta) + m \ln(n)$$

$$\frac{\sum_{t=2}^T (e_t - e_{t-1})^2}{\sum_{t=1}^T e_t^2}$$

$$U(\beta) = \sum_{k=1}^K \frac{\partial \mu_k}{\partial \beta} V_k^{-1} (Y_k - \mu_k(\beta))$$

$$y = X\beta + \varepsilon$$

$$y = X\beta + Zu + \varepsilon$$

$$x_t = F_t x_{t-1} + \beta_t u_t + w_t$$

$$y_t = H_t x_t + v_t$$

$$y = X\beta + \varepsilon$$

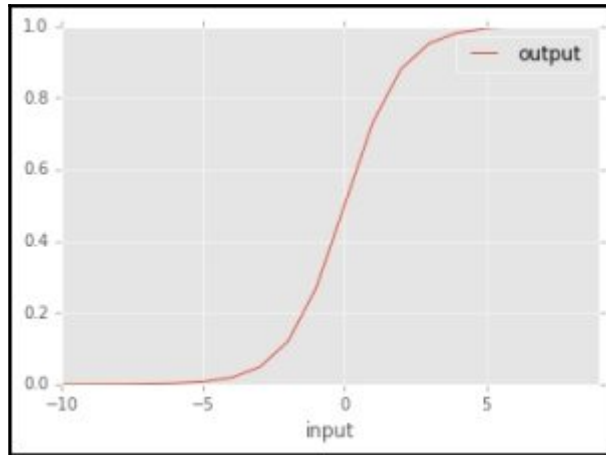
$$G(Y) = X\beta + \varepsilon$$

$$L(\beta) = \sum_{i=1}^n (y_i - x_i \beta)^2 + \alpha \sum_{j=1}^m \beta_j^2$$

$$L(\beta) = \sum_{i=1}^n (y_i - x_i \beta)^2 + \alpha \sum_{j=1}^m |\beta_j|$$

$$L(\beta) = \sum_{i=1}^n (y_i - x_i \beta)^2 + \alpha_1 \sum_{j=1}^m \beta_j^2 + \alpha_2 \sum_{i=1}^n |\beta|$$

Chapter 5: Putting Data in its Place – Classification Methods and Analysis



$$Y = 1 - \text{logistic}(z) = 1 - \frac{1}{1 + e^{(-z)}} = \frac{1 + e^{(-z)}}{1 + e^{(-z)}} - \frac{1}{1 + e^{(-z)}} = \frac{e^{(-z)}}{1 + e^{(-z)}}$$

$$\log\left(\frac{P(Y=1)}{1 - P(Y=1)}\right) = \log\left(\frac{\frac{1}{1 + e^{(-z)}}}{\frac{e^{(-z)}}{1 + e^{(-z)}}}\right) = \log(1) - \log(e^{(-z)}) = X\beta^T$$

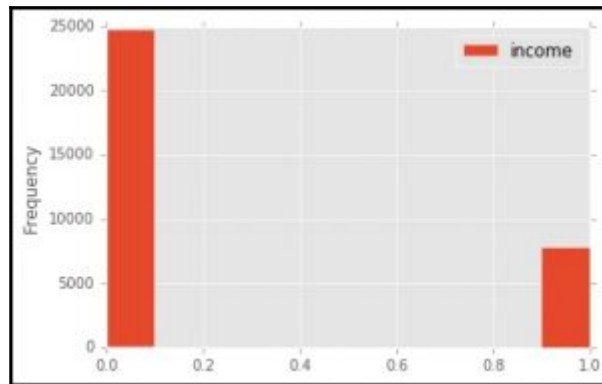
$$e^{\log\left(\frac{P(Y=1)}{1 - P(Y=1)}\right)} = \frac{\text{logistic}(z)}{1 - \text{logistic}(z)} = \frac{\frac{1}{1 + e^{(-z)}}}{\frac{e^{(-z)}}{1 + e^{(-z)}}} = \frac{1}{e^{(-z)}} = e^{(z)} = e^{(X\beta^T)}$$

$$P(y_i = k) = \frac{e^{(x_i \beta_k^T)}}{\sum_{j=1}^K e^{(x_i \beta_j^T)}}$$

```
osense = pd.read_csv('osense.data', header=None)
```

```
osense.head()
```

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
0	35	State-gov	77516	Bachelors	13	Never-married	Adm-clerical	Not-in-family	White	Male	2174	0	40	United-States
1	50	Self-emp-not-inc	83311	Bachelors	13	Married-civ-spouse	Exec-managerial	Husband	White	Male	0	0	13	United-States
2	38	Private	215046	HS-grad	9	Divorced	Handlers-cleaners	Not-in-family	White	Male	0	0	40	United-States
3	53	Private	234721	11th	7	Married-civ-spouse	Handlers-cleaners	Husband	Black	Male	0	0	40	United-States
4	28	Private	339408	Bachelors	13	Married-civ-spouse	Prof-specialty	Wife	Black	Female	0	0	40	Cuba



$$P(y_i = 1) = \frac{1}{1 + e^{(-z)}} = F(z_i)$$

$$P(y_i = 0) = \frac{e^{(-z)}}{1 + e^{(-z)}} = 1 - F(z_i)$$

$$L(y_i) = (F(z_i))^{y_i} (1 - F(z_i))^{1 - y_i}$$

$$L(Y) = \sum_{i=1}^n (y_i \log(F(z_i)) + (1 - y_i) \log(1 - F(z_i)))$$

$$\begin{aligned}
\frac{\partial}{\partial \beta} \log(L(y_i)) &= \frac{\partial}{\partial \beta} (y_i \log(F(z_i)) + (1-y_i) \log(1-F(z_i))) = 0 \\
&= \frac{y_i}{F(z_i)} F'(z_i) + \frac{(1-y_i)}{(1-F(z_i))} F'(z_i) \\
&= \left(\frac{y_i}{F(z_i)} - \frac{(1-y_i)}{(1-F(z_i))} \right) F'(z_i) \\
&= \left(\frac{y_i}{F(z_i)} - \frac{(1-y_i)}{(1-F(z_i))} \right) \left(\frac{1}{1+e^{-\lambda \beta^T z_i}} \right) \left(\frac{e^{-\lambda \beta^T z_i}}{1+e^{-\lambda \beta^T z_i}} \right) (-x_i) \\
&= \left(\frac{y_i}{\frac{1}{1+e^{-\lambda \beta^T z_i}}} - \frac{(1-y_i)}{\frac{e^{-\lambda \beta^T z_i}}{1+e^{-\lambda \beta^T z_i}}} \right) \left(\frac{1}{1+e^{-\lambda \beta^T z_i}} \right) \left(\frac{e^{-\lambda \beta^T z_i}}{1+e^{-\lambda \beta^T z_i}} \right) (-x_i) \\
&= \left(y_i \left(\frac{e^{-\lambda \beta^T z_i}}{1+e^{-\lambda \beta^T z_i}} \right) - (1-y_i) \left(\frac{1}{1+e^{-\lambda \beta^T z_i}} \right) \right) (-x_i) \\
&= \left(\frac{y_i (1+e^{-\lambda \beta^T z_i})}{1+e^{-\lambda \beta^T z_i}} - \left(\frac{1}{1+e^{-\lambda \beta^T z_i}} \right) \right) (-x_i) \\
&= -(y_i - F(z_i)) x_i
\end{aligned}$$

$$\beta_t = \beta_{t-1} + \alpha (y_i - F(z_i)) x_i$$

$$\frac{1}{2} \lambda \beta \beta^T$$

$$\beta_t = \beta_{t-1} + \alpha (y_i - F(z_i)) x_i - \lambda \beta_{t-1}$$

$$f(x^*) = f(x_t + \Delta x)$$

$$f(x^*) = f(x_t) + f'(x_t) \Delta x + \frac{1}{2} f''(x_t) (\Delta x)^2$$

$$\frac{df(x^*)}{d\Delta x} = f'(x) + 2\left(\frac{1}{2}\right)f''(x)(\Delta x) = 0$$

$$-f'(x) = f''(x)(\Delta x)$$

$$\Delta x = -\frac{f'(x)}{f''(x)}$$

$$(y_i - F(z_i))x_i - \lambda\beta_i$$

$$\frac{\partial L(y_i)}{\partial \beta \partial \beta^T} = \frac{\partial}{\partial \beta} \left(\frac{\partial L(y_i)}{\beta^T} \right)$$

$$= \frac{\partial}{\partial \beta} (-(y_i - F(z_i))x_i - \lambda\beta)$$

$$= \frac{\partial F(z_i)x_i}{\partial \beta} - \lambda = -\frac{\partial}{\partial \beta} \left(\frac{1}{1 + e^{(-x_i\beta^T)}} \right) x_i - \lambda$$

$$= \left(\frac{1}{1 + e^{(-x_i\beta^T)}} \right) \left(\frac{e^{(-x_i\beta^T)}}{1 + e^{(-x_i\beta^T)}} \right) (x_i)(x_i)^T - \lambda$$

$$= (x_i)F(z_i)(1 - F(z_i))(x_i)^T - \lambda$$

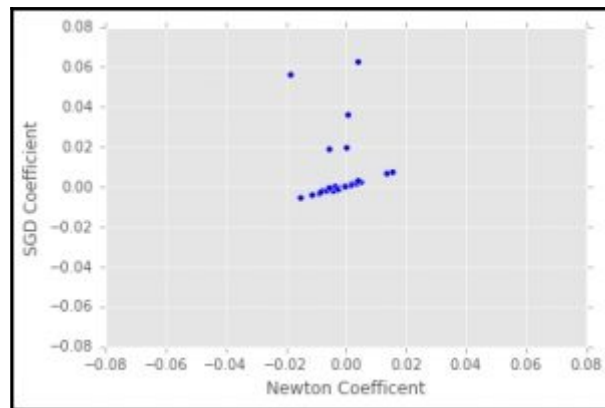
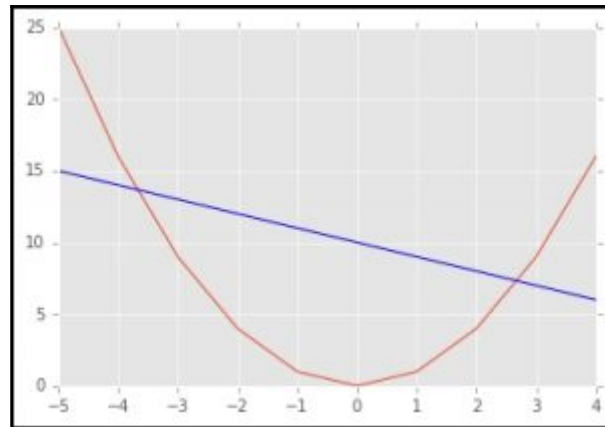
$$-\sum_{i=1}^n x_i (y_i - F(z_i)) - \lambda\beta$$

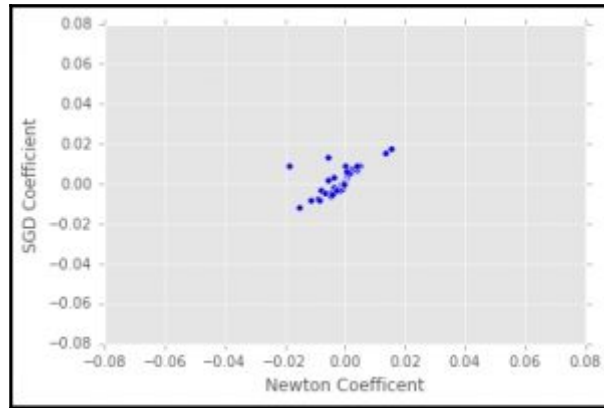
$$= (X)^T F(Z)(1 - F(Z))(X) - I\lambda$$

$$= X^T AX - I\lambda$$

$$\beta_t = \beta_{t-1} + (X^T A X - I \lambda)^{-1} \left(\sum_{i=1}^n x_i (y_i - F(z_i)) - \lambda \beta_t \right)$$

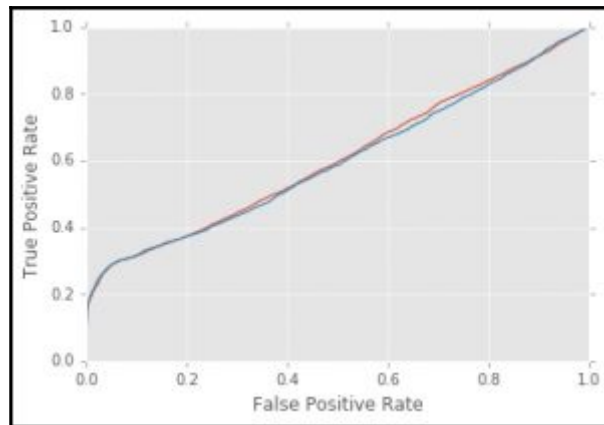
$$F(\alpha x_1 + (1-\alpha)x_2) \leq \alpha F(x_1) + (1-\alpha)F(x_2)$$

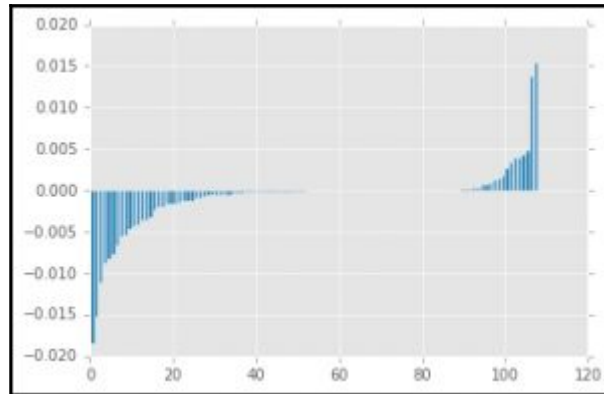




$$F_1 = 2 \frac{(\textit{precision})(\textit{recall})}{(\textit{precision} + \textit{recall})}$$

$$MCC = \frac{TP \times TN - FP \times FN}{\sqrt{(TP + FP)(TP + FN)(TN + FP)(TN + FN)}}$$





$$F(X) = X\beta^T + b$$

$$L(\beta, w, \alpha) = \frac{1}{2} \|B\|^2 - \sum_{i=1}^n \alpha_i (y_i (x_i \beta^T + b) - 1)$$

$$\|\beta\| = \sqrt{\beta_1^2 + \beta_2^2 + \dots + \beta_m^2}$$

$$\frac{\partial L}{\partial \beta} = \beta - \sum_{i=1}^n \alpha_i y_i x_i = 0$$

$$\beta = \sum_{i=1}^n \alpha_i y_i x_i$$

$$\frac{\partial L}{\partial b} = \sum_{i=1}^n \alpha_i y_i = 0$$

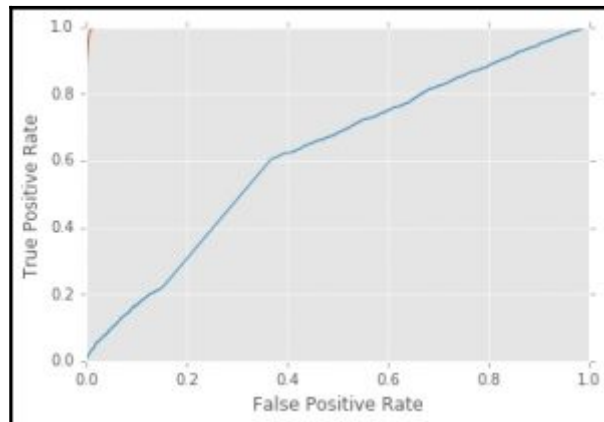
$$\begin{aligned} L(\beta, w, \alpha) &= \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n \alpha_i \alpha_j y_i y_j x_i x_j - \sum_{i=1}^n \alpha_i \left(y_i x_i \left(\sum_{i=1}^n \alpha_i y_i x_i \right) - 1 \right) \\ &= \sum_{i=1}^n \alpha_i - \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n \alpha_i \alpha_j y_i y_j x_i x_j \end{aligned}$$

$$\max(0, 1 - y_i(x_i\beta + b_i))$$

$$\langle \varphi(x_i), \varphi(x_j) \rangle$$

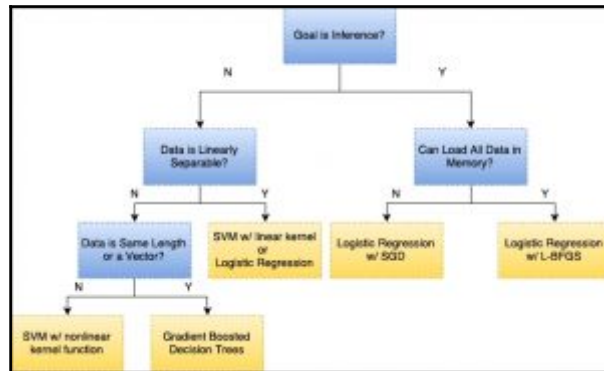
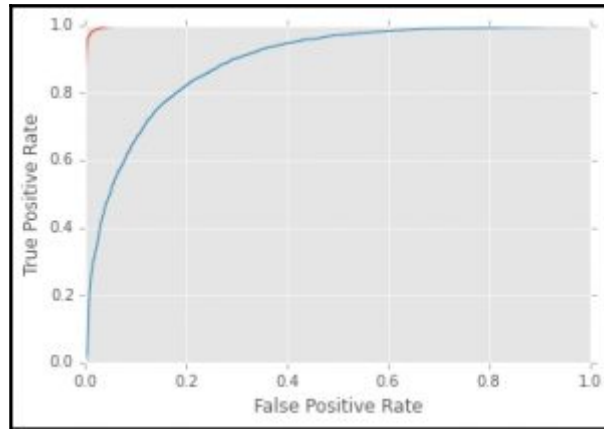
$$K(x_i, x_j) = e^{-\frac{\|x_i - x_j\|^2}{2\gamma^2}}$$

$$e^{-\frac{\|x_i - x_j\|^2}{2\gamma^2}} = e^{-\frac{1}{2\gamma^2}(-x_i)^2(-x_j)^2} e^{2(x_i x_j)} = e^{-\frac{1}{2\gamma^2}(-x_i)^2(-x_j)^2} \sum_{k=0}^{\infty} \frac{2^k x_i^k x_j^k}{k!}$$



$$\gamma_t = \frac{\arg \min}{\gamma} \sum_{i=1}^n L(y_i, F_{t-1}(x_i) + h_t(x_i))$$

$$F_t = F_{t-1}(X) + \alpha \gamma_t h_t(X)$$



$$r_i = -\frac{\partial L(y_i, F(x_i))}{\partial F(x_i)}$$

$$Y = X\beta^T$$

$$Y = \text{logistic}(X\beta^T)$$

$$\text{logistic}(X\beta^T) = \text{logistic}(z) = \frac{1}{1 + e^{(-z)}}$$

Chapter 6: Words and Pixels – Working with Unstructured Data

$$W \leftarrow W \frac{X^T H}{WH^T H}$$

$$H \leftarrow H \frac{HX^T}{HH^T W^T}$$

$$\frac{1}{B(\alpha)} \prod_{i=1}^K x_i^{\alpha_i - 1}$$

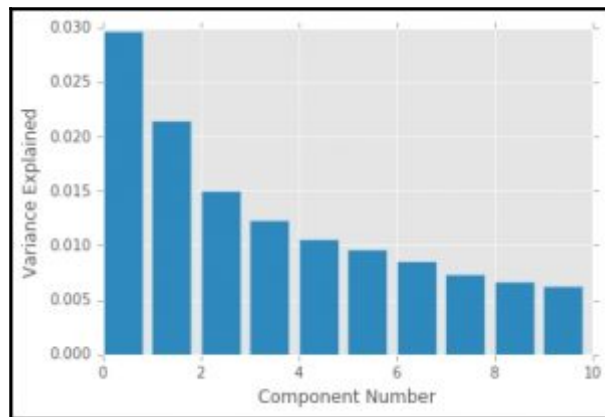
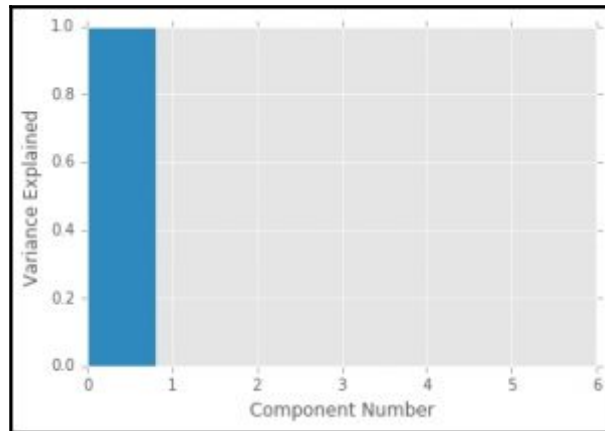
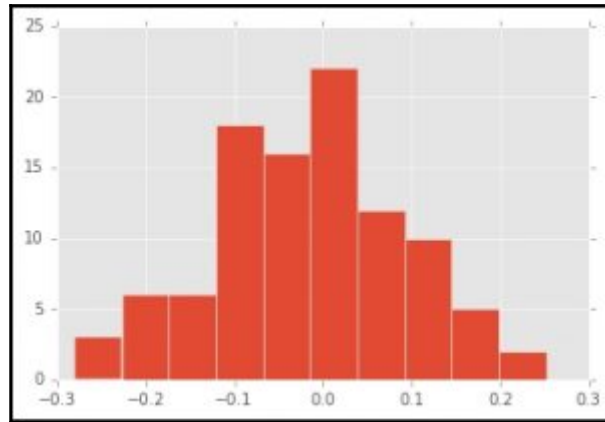
$$p = ui$$

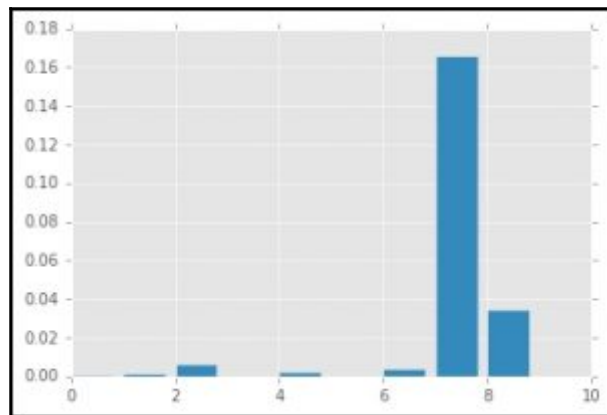
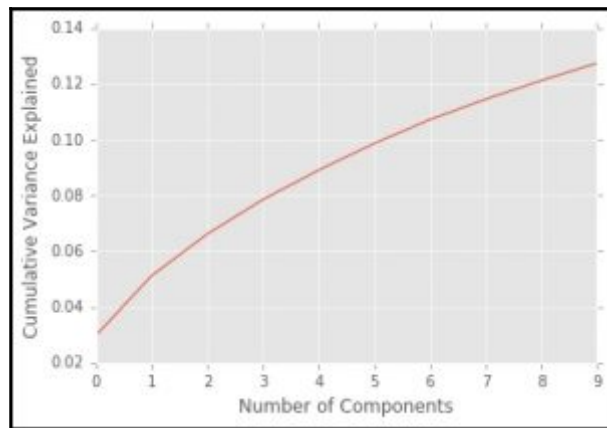
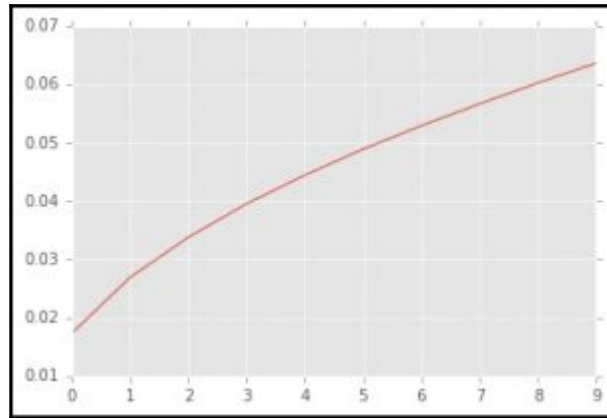
	label	text
0	ham	Go until jurong point, crazy.. Available only ...
1	ham	Ok lar... Joking wif u oni...
2	spam	Free entry in 2 a wkly comp to win FA Cup fina...
3	ham	U dun say so early hor... U c already then say...
4	ham	Nah I don't think he goes to usf, he lives aro...

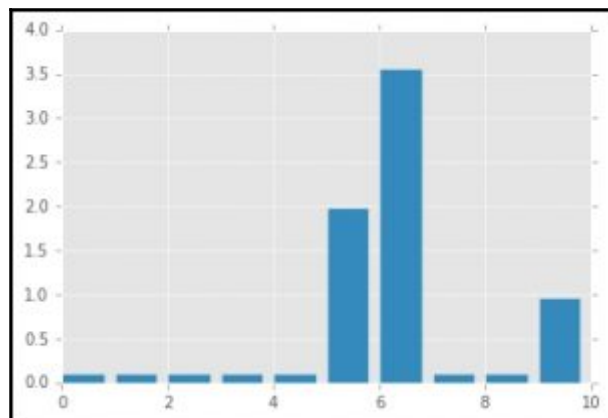
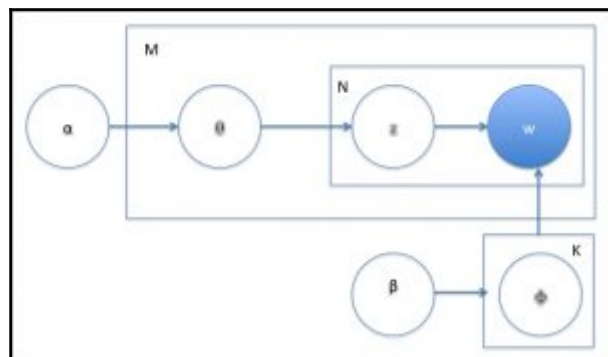
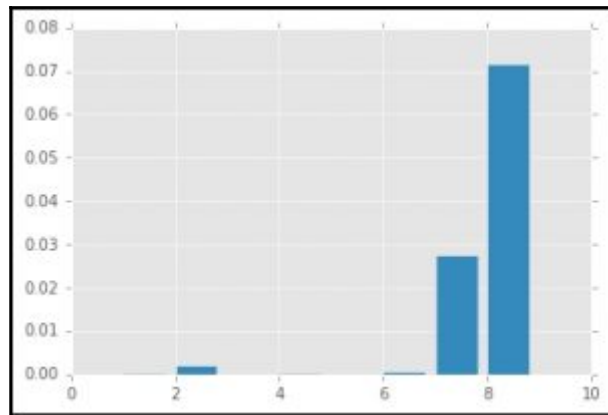
	label	text
0	ham	go until jurong point, crazy.. available only ...
1	ham	ok lar... joking wif u oni...
2	spam	free entry in 2 a wkly comp to win fa cup fina...
3	ham	u dun say so early hor... u c already then say...
4	ham	nah i don't think he goes to usf, he lives aro...

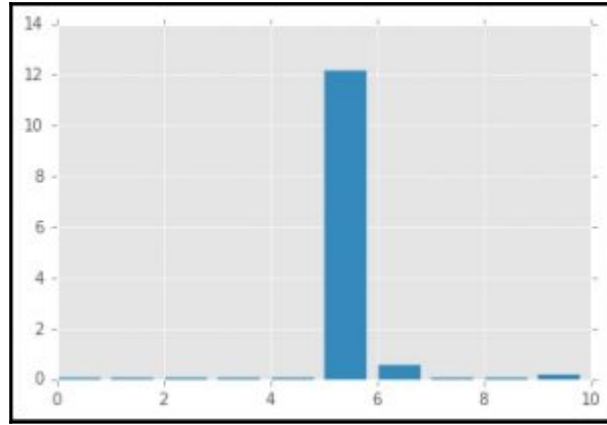
	label	text
0	ham	go jurong point , crazy.. avail bugi n grea...
1	ham	ok lar ... joke wif u oni ...
2	spam	free entri 2 wkli comp win fa cup final tkt...
3	ham	u dun say earli hor ... u c already say ...
4	ham	nah n't think goe usf , live around though

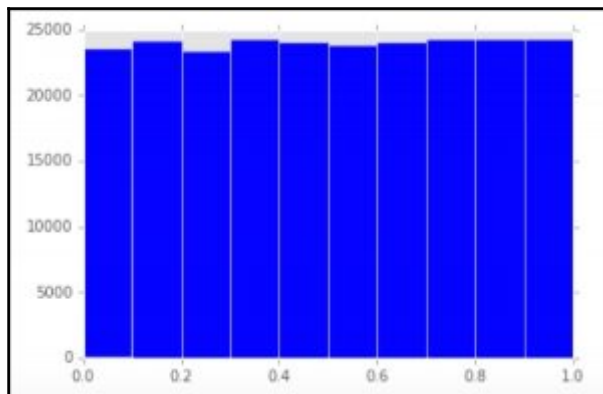
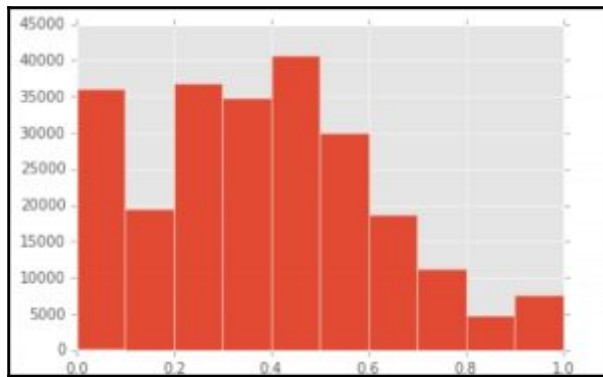
	label	text
0	ham	go jurong point , crazy.. avail bugi n grea...
1	ham	ok lar ... joke wif u oni ...
2	spam	free entri 2 wkli comp win fa cup final tkt...
3	ham	u dun say earli hor ... u c already say ...
4	ham	nah n't think goe usf , live around though

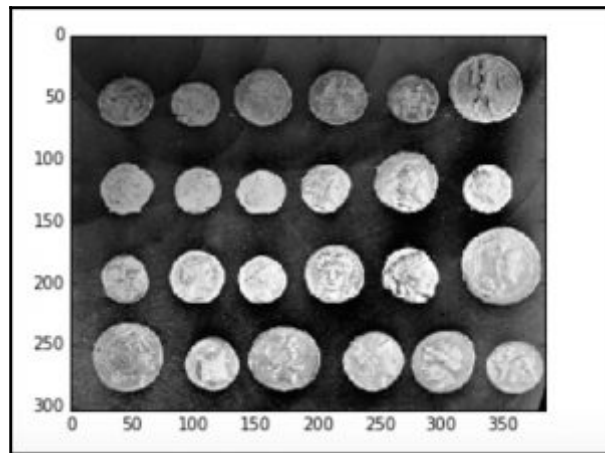
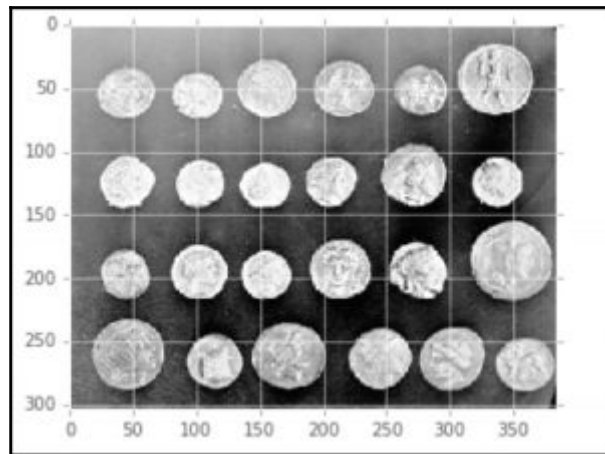


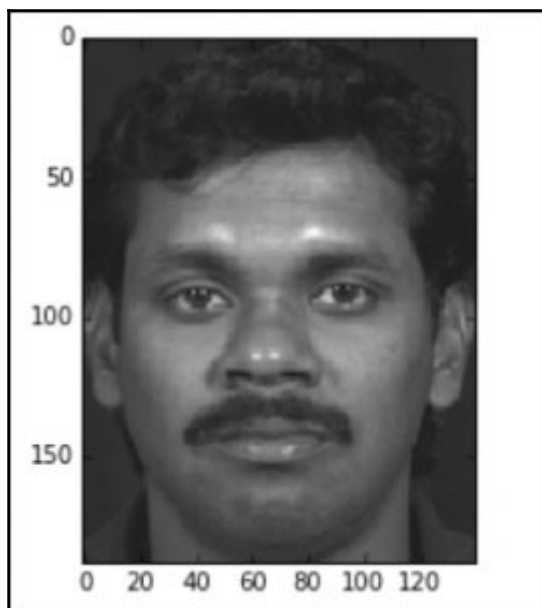
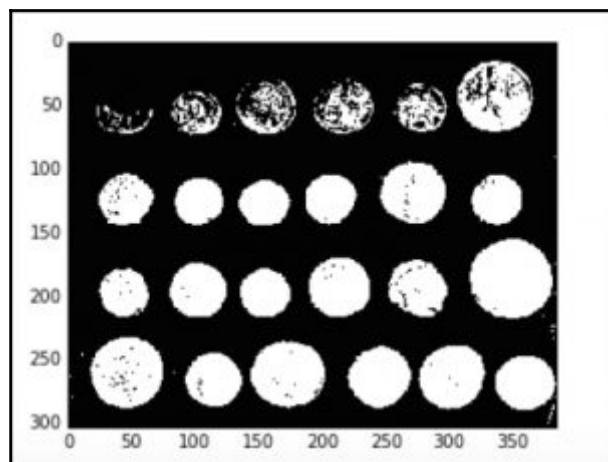


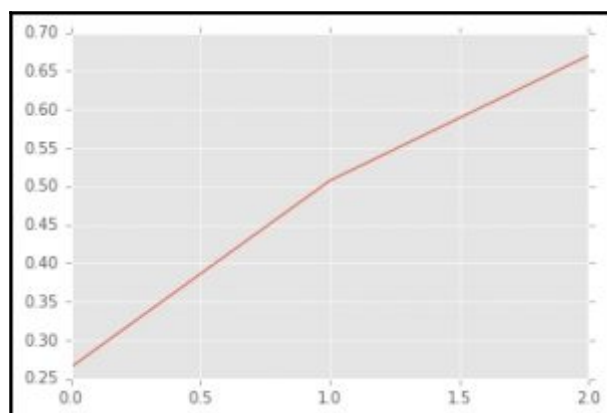
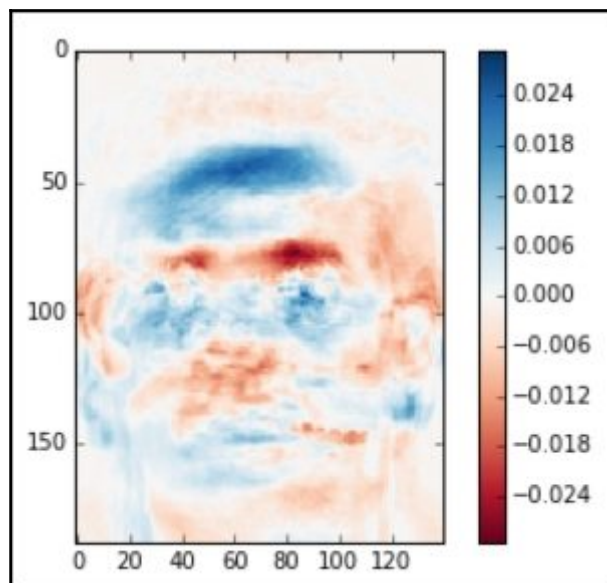


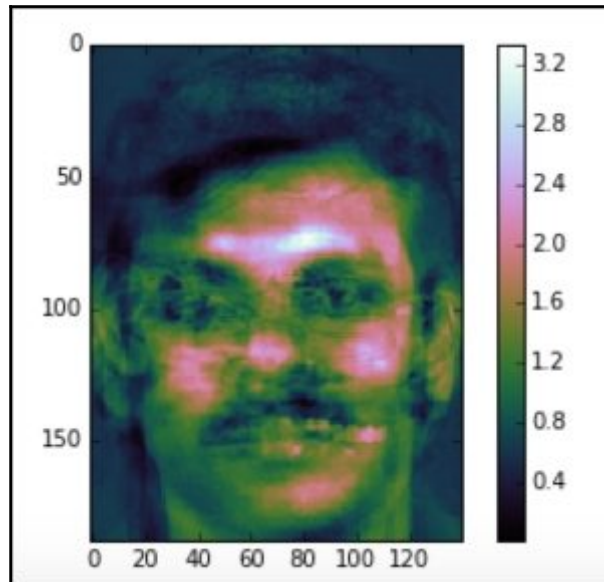
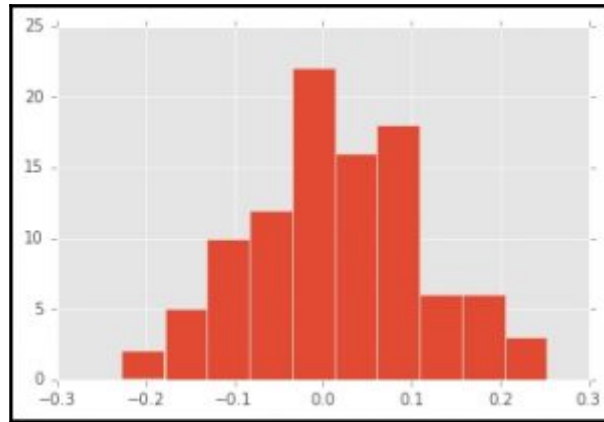












$$tf - idf(t_i, d_j) = \frac{\sum_{k=1}^{V_j} 1_{t_i=v_k}}{\frac{\sum_{j=1}^D 1_{t_i \in V_j}}{D}}$$

$$\text{Cov}(x_i, x_j) = \frac{1}{n} \sum_{i,j=1}^n (x_i - \mu_i)(x_j - \mu_j)$$

$$X^T X = W^T \sigma W$$

$$X = CUR$$

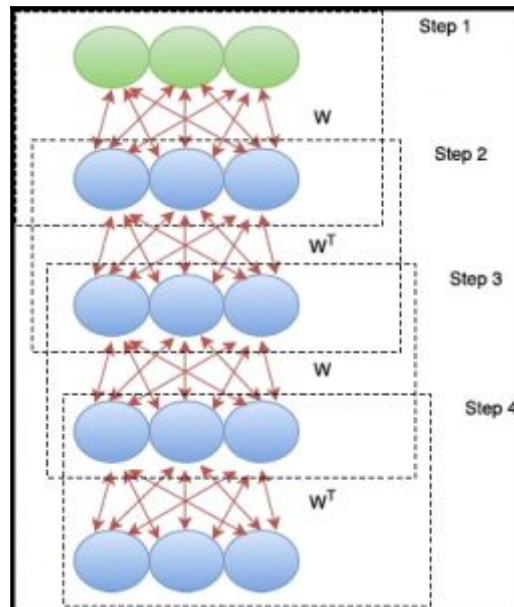
$$lv_j = \frac{1}{k} \sum_{i=1}^k (v_j^i)^2$$

$$X = WH$$

$$\|X - WH\|_F^2 = (X - WH)(X - WH)^T$$

$$\frac{\partial}{\partial W} (X - WH)(X - WH)^T \approx$$
$$-X^T H + WH^T H =$$
$$\frac{X^T H}{WH^T H}$$

Chapter 7: Learning from the Bottom Up – Deep Networks and Unsupervised Features



$$F(x) = \begin{cases} 1 & \text{if } wx > b \\ 0 & \text{otherwise} \end{cases}$$

$$\Delta w = \alpha (y_i - F(x_i)) x_i$$

$$\frac{1}{n} \sum_{i=1}^n |y_i - F(x_i)|$$

$$F(z) = \frac{1}{1 + e^{(-wx+b)}} = \frac{1}{1 + e^{(-z)}}$$

$$E(x_i) = \frac{1}{2} (F(z_i) - y_i)^2$$

$$F(x) = e^{-x^2}$$

$$\frac{\partial F}{\partial x} = \frac{\partial F \partial z}{\partial z \partial x}$$

$$\frac{\partial E}{\partial w_{ij}} = \frac{\partial E}{\partial F(z)_i} \frac{\partial F(z)_i}{z} \frac{\partial z}{\partial w_{ij}}$$

$$\frac{\partial E}{\partial F(z)_i} = 2 \frac{1}{2} (F(z)_i - y)(1) = F(z)_i - y$$

$$\frac{\partial F(z)_i}{z} = \frac{(0)(1+e^{-z}) - (1)(-e^{-z})}{(1+e^{-z})^2} =$$
$$\frac{1}{(1+e^{-z})} \frac{1-1+e^{-z}}{(1+e^{-z})} = F(z)_i (1-F(z)_i)$$

$$\frac{\partial z}{\partial w_{ij}} = F(z)_j$$

$$w_{ij-new} = w_{ij-old} - \alpha \frac{\partial E}{\partial w_{ij}}$$

$$\frac{\partial E}{\partial w_{jk}} = \frac{\partial E}{\partial F(z)_j} \frac{\partial F(z)_j}{z} \frac{\partial z}{\partial w_{jk}}$$

$$\frac{\partial E}{\partial F(z)_j} = \sum_{i=1}^n \left(\frac{\partial E}{\partial z} \frac{\partial z}{\partial F(z)_i} \right) = \sum_{i=1}^n \left(\frac{\partial E}{\partial F(z)_i} \frac{\partial F(z)_i}{\partial z} w_{ij} \right)$$

$$\frac{\partial z}{\partial w_{jk}} = x_k$$

$$\frac{\partial z}{\partial w_{jk}} = \frac{\partial E}{\partial F(z)_j} \frac{\partial F(z)_j}{z} \frac{\partial z}{\partial w_{jk}} = \left(\sum_{i=1}^n \frac{\partial E}{\partial F(z)_i} \frac{\partial F(z)_i}{\partial z} w_{ij} \right) F(z)_j (1 - F(z)_j) x_k$$

$$F(z) = \max(z, 0)$$

$$\frac{\partial F(z)}{\partial z} = \begin{cases} 1 & \text{if } z > 0 \\ 0 & \text{else} \end{cases}$$

$$F(z) = \max(z, \alpha z)$$
$$\frac{\partial F(z)}{\partial z} = \begin{cases} 1 & \text{if } z > 0 \\ \alpha & \text{else} \end{cases}$$

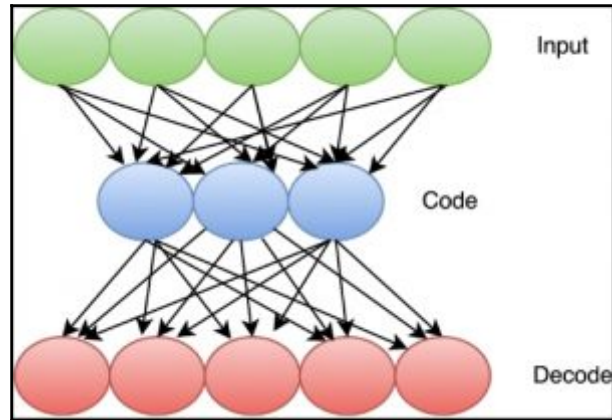
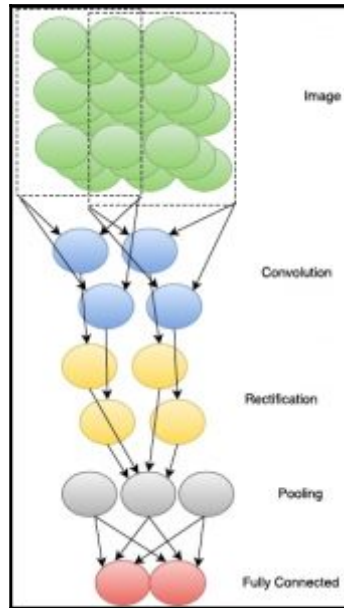
$$\tanh(x) = \frac{e^{2x} - 1}{e^{2x} + 1} = \frac{1 - e^{-2x}}{1 + e^{-2x}}$$

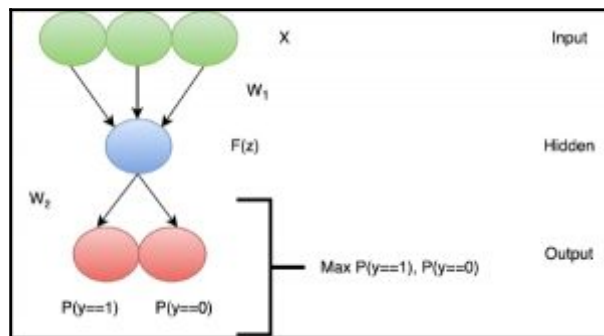
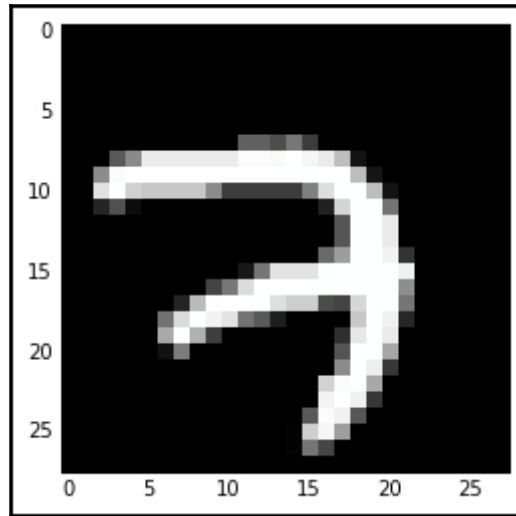
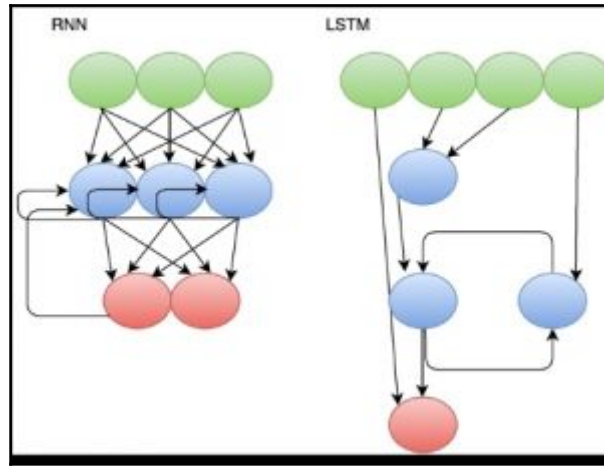
$$w_t = w_{t-1} - \frac{\alpha}{\sqrt{G_t + \varepsilon}} \frac{\partial E}{\partial w}$$

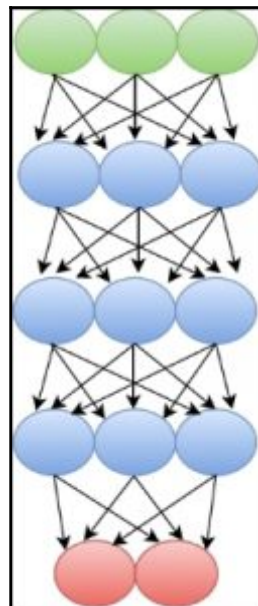
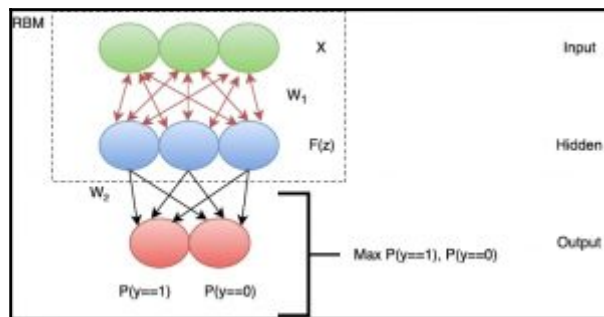
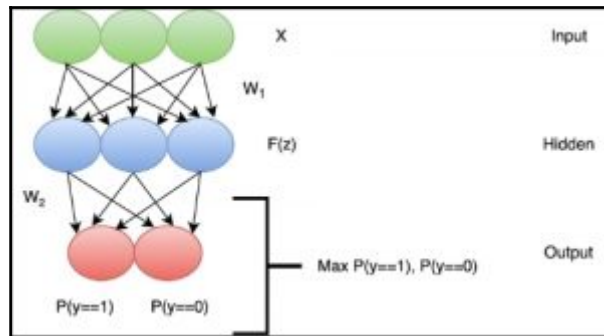
$$\frac{1}{T} \left(\frac{\partial E}{\partial w} \right)_t^2 = \gamma \frac{1}{T} \left(\frac{\partial E}{\partial w} \right)_{t-1}^2 + (1-\gamma) \left(\frac{\partial E}{\partial w} \right)_t^2$$

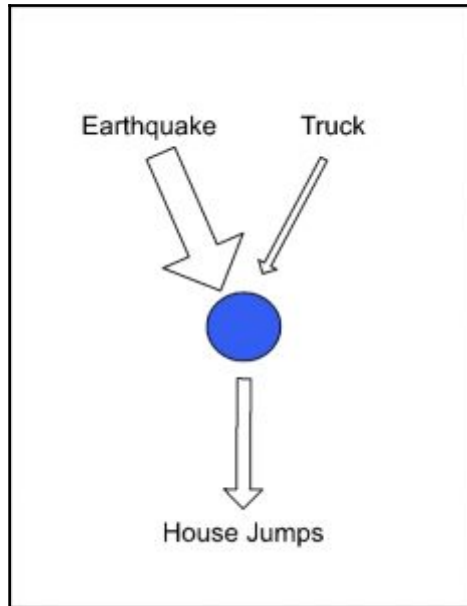
$$w_t = w_{t-1} - \frac{\alpha}{\sqrt{\frac{1}{T} \left(\frac{\partial E}{\partial w} \right)_t^2 (1-\beta_1) + \varepsilon}} \frac{\partial E}{\partial w} \begin{pmatrix} 1 \\ 1-\beta_2 \end{pmatrix}$$

$$e^{-x^2} \quad 2x$$









Chapter 8: Sharing Models with Prediction Services

```
[45689] 29 Jul 00:35:48.207 * Increased maximum number of open files to 1024 (it was originally set to 4096)

Redis 2.8.12 (00000000/0) 64 bit
Running in stand alone mode
Port: 7777
PID: 45689

http://redis.io

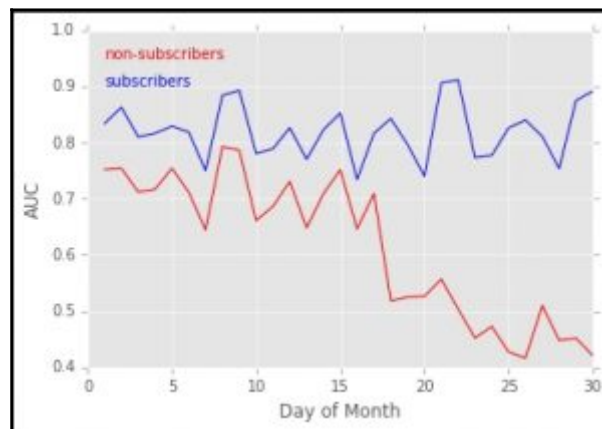
[45689] 29 Jul 00:35:48.209 # Server started, Redis version 2.8.12
[45689] 29 Jul 00:35:48.212 * DB loaded from disk: 0.002 seconds
[45689] 29 Jul 00:35:48.212 * The server is now ready to accept connections on port: 7777
```

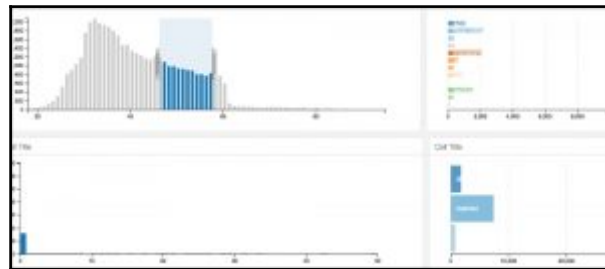
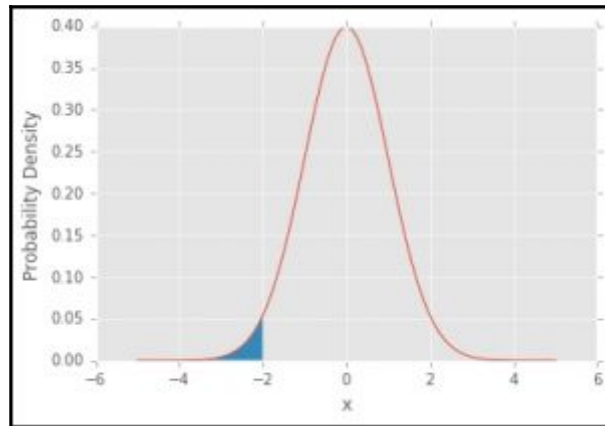
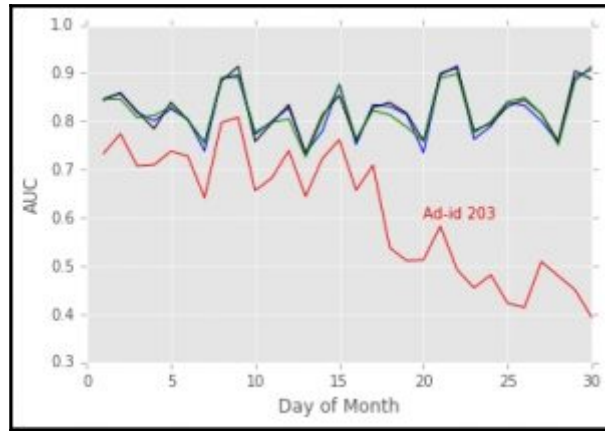
```
[19/Jul/2016:00:52:46] ENGINE Bus STARTING
[19/Jul/2016:00:52:46] ENGINE Started monitor thread 'Autoreloader'.
[19/Jul/2016:00:52:46] ENGINE Started monitor thread '_TimeoutMonitor'.
[19/Jul/2016:00:52:47] ENGINE Serving on http://0.0.0.0:5000
[19/Jul/2016:00:52:47] ENGINE Bus STARTED
```

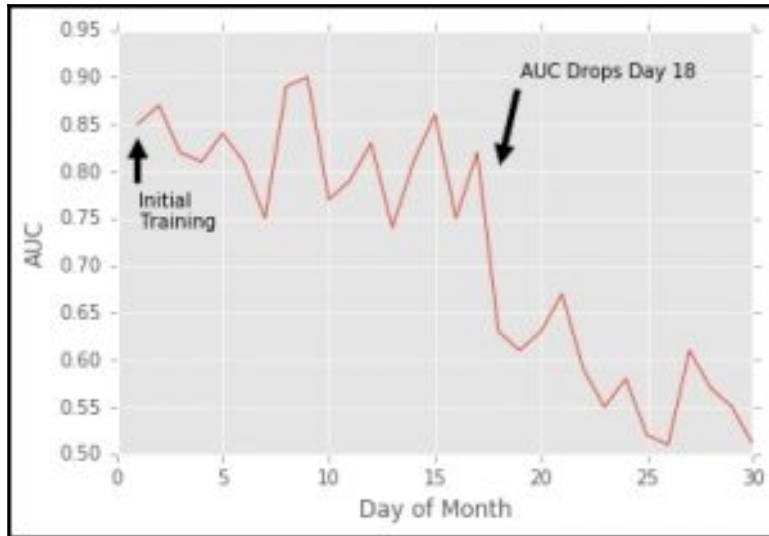
```
----- celery@lgnl-jbabcockH04 v3.1.22 (Cipater)
---- * * * * ----
-- * * * * -- Darwin-15.5.0-x86_64-1386-64bit
- * - * * * -
- ** ----- [config]
- ** ----- .> app:      modelservice:0x110cc87d0
- ** ----- .> transport: redis://localhost:6379//
- ** ----- .> results:  redis://localhost:6379/
- *** --- * --- .> concurrency: 4 (prefork)
- ***** ---
- ***** --- [queues]
- ----- .> celery      exchange=celery(direct) key=celery

[2016-07-19 01:14:10,739: WARNING/MainProcess] celery@lgnl-jbabcockH04 ready.
```

Chapter 9: Reporting and Testing – Iterating on Analytic Systems







$$T = \frac{Y_1 - Y_2}{S_{Y_1 - Y_2}}$$

$$S_{Y_1 - Y_2} = \sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}$$

$$1.64 \leq \frac{10}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}}$$

$$\frac{100}{2.69} \geq \frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}$$

$$S_{Y_1 - Y_2} = \sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}$$

$$1.64 \leq \frac{10}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}}$$
$$37.17 \geq \frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}$$

$$\frac{(\text{predicted} - \text{observed})^2}{n}$$

$$s(i) = \frac{d'(i) - d(i)}{\max(d(i), d'(i))}$$

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