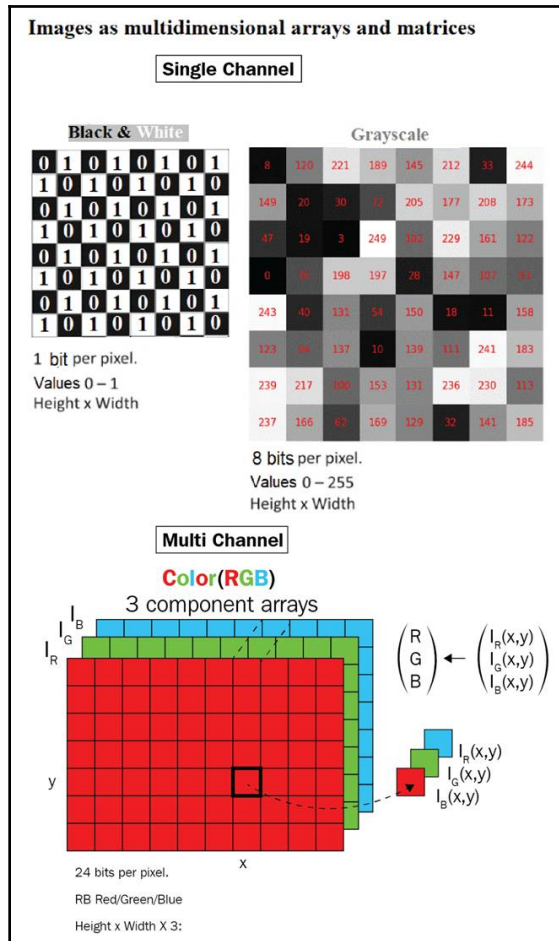


Graphics

Chapter 1: Getting Started with Image Processing



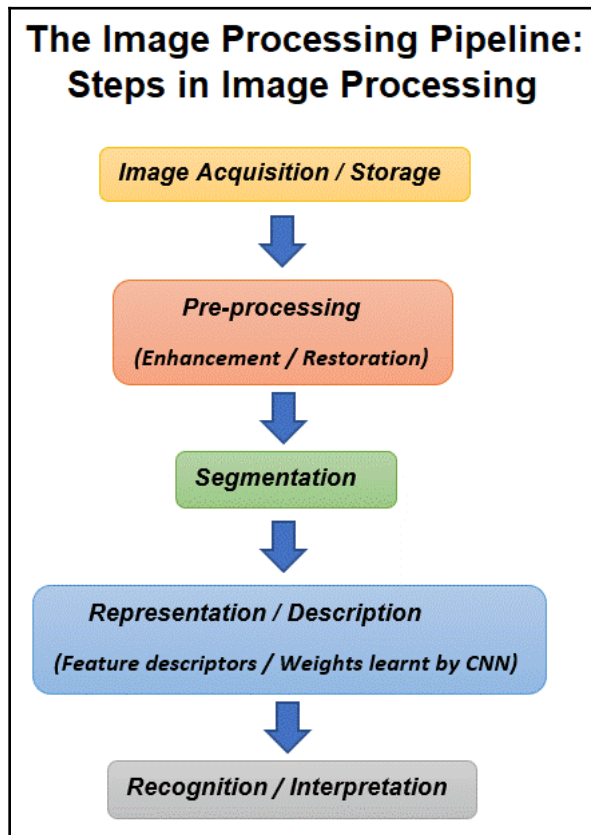
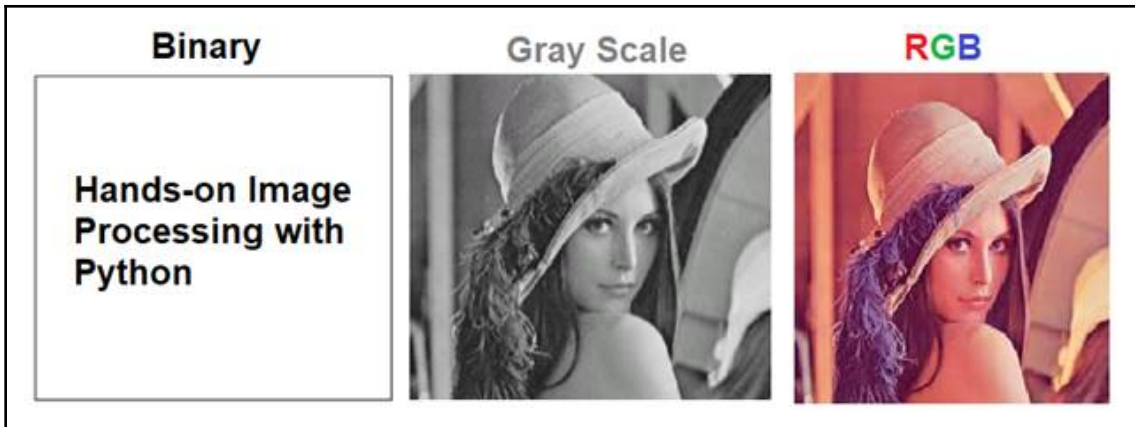


Image I/O, Display, Draw, Mode, Stats

(scikit-image io, external, util, viewer, color, exposure, draw, measure modules,
PIL Image, ImageFile, ImageColor, ImageDraw, ImageMath, ImageStat modules,
Matplotlib image module)

Image Manipulation/Transformation /Morphology

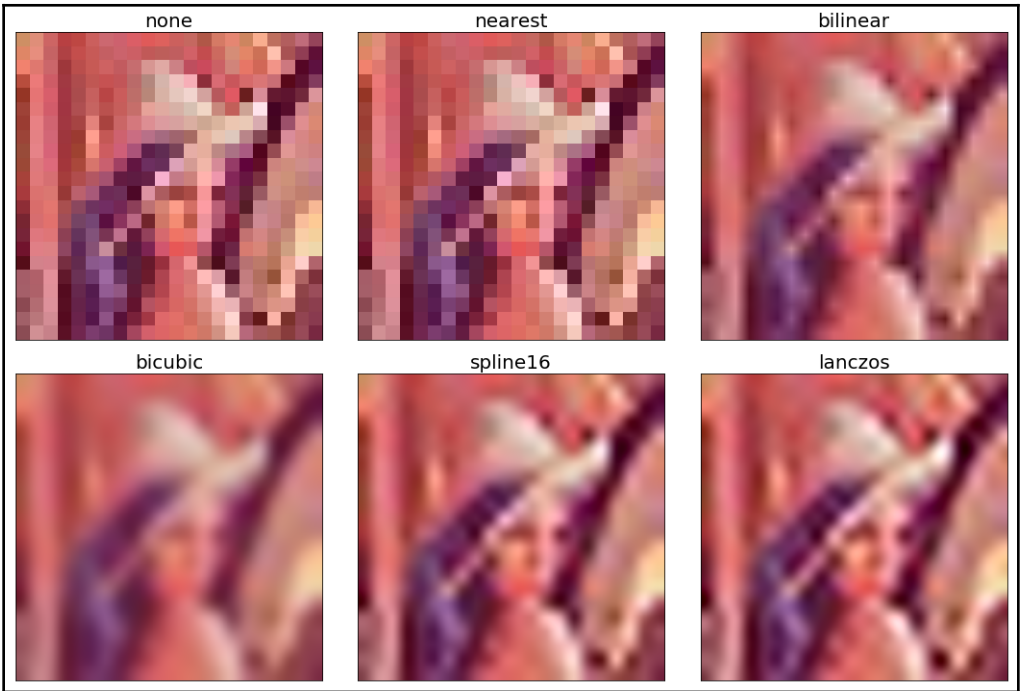
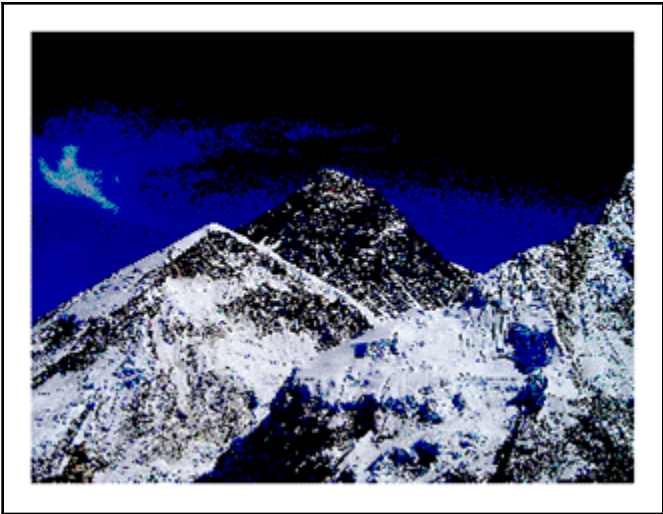
(scikit-image transform, util, morphology modules,
PIL Image, ImageMorph, ImageChops modules)

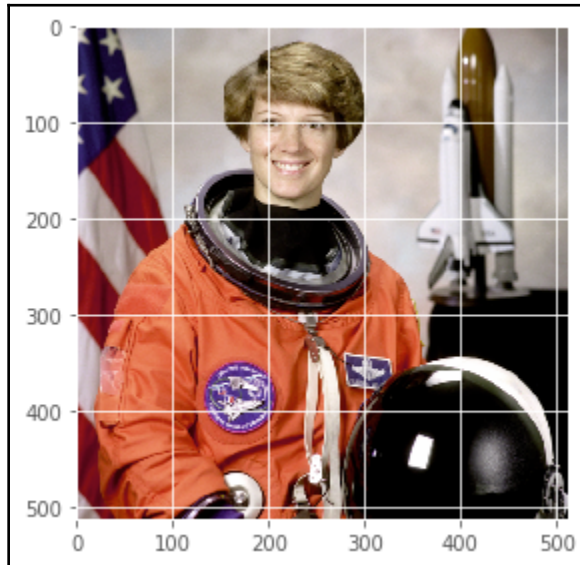
Image Enhancement/Filter/Restoration/Segmentation / Feature extraction

(scikit-image filters, filters.rank, restoration, segmentation, graph, future.graph, feature modules,
PIL ImageEnhance, ImageFilter modules)

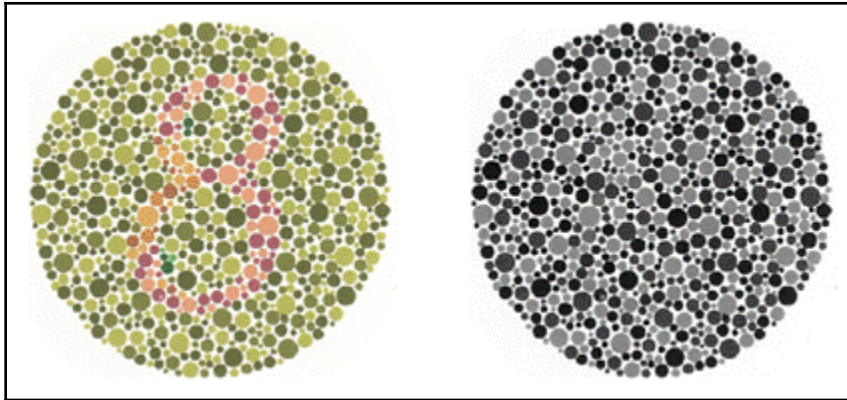










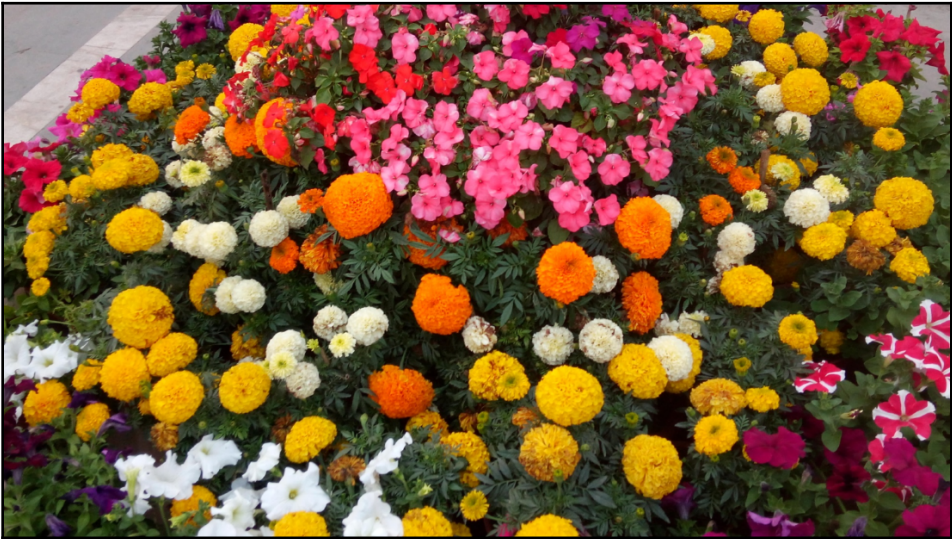
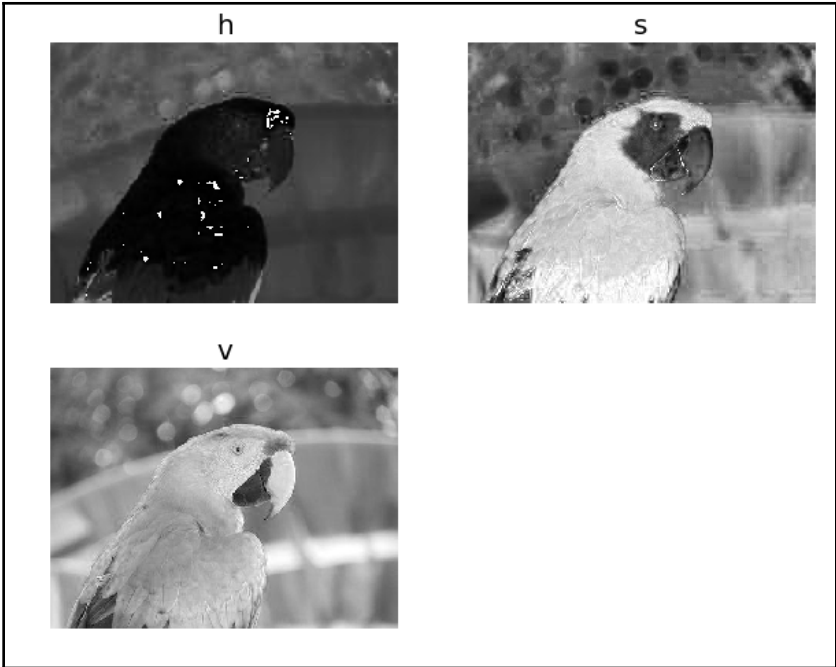


RGB to YIQ

$$\begin{bmatrix} Y \\ I \\ Q \end{bmatrix} = \begin{bmatrix} 0.299 & 0.587 & 0.114 \\ 0.596 & -0.274 & -0.322 \\ 0.211 & -0.523 & 0.312 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

YIQ to RGB

$$\begin{bmatrix} R \\ G \\ B \end{bmatrix} = \begin{bmatrix} 1 & 0.956 & 0.621 \\ 1 & -0.272 & -0.647 \\ 1 & -1.106 & 1.703 \end{bmatrix} \begin{bmatrix} Y \\ I \\ Q \end{bmatrix}$$



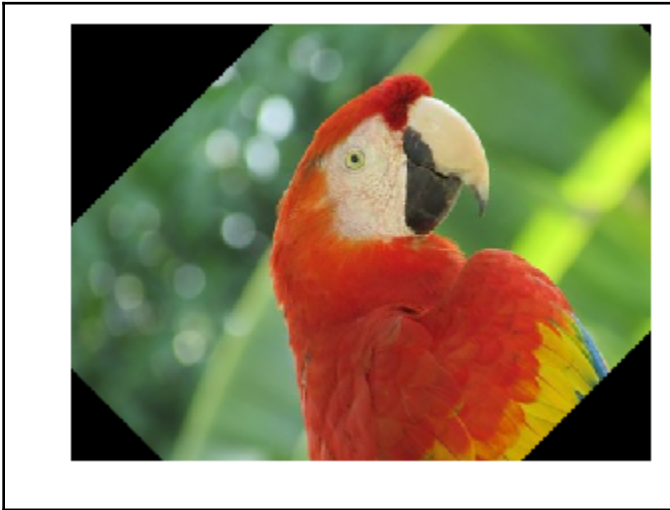






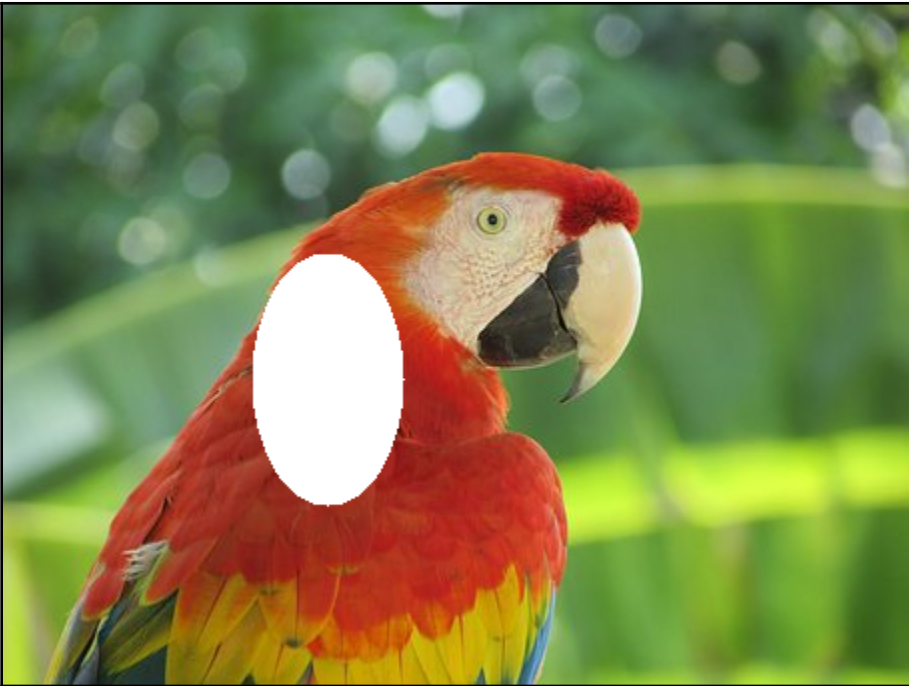




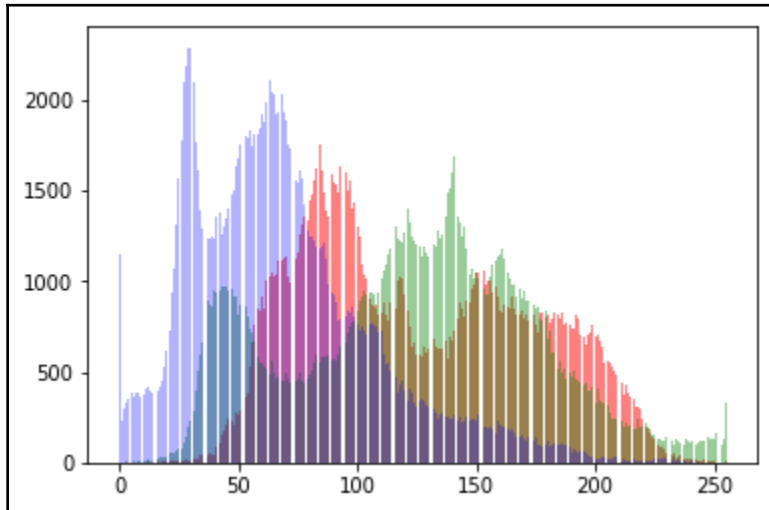






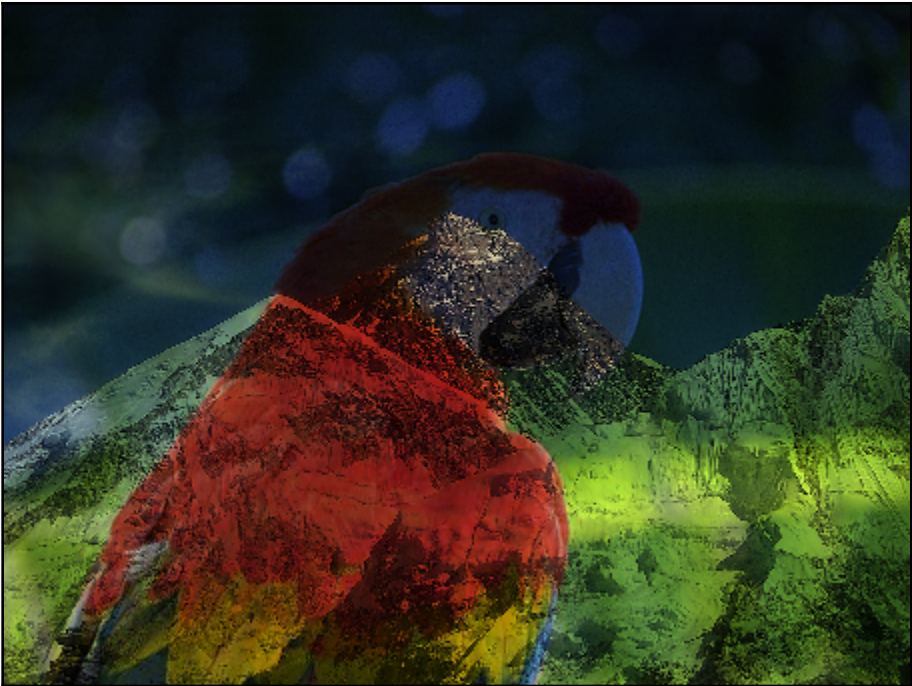












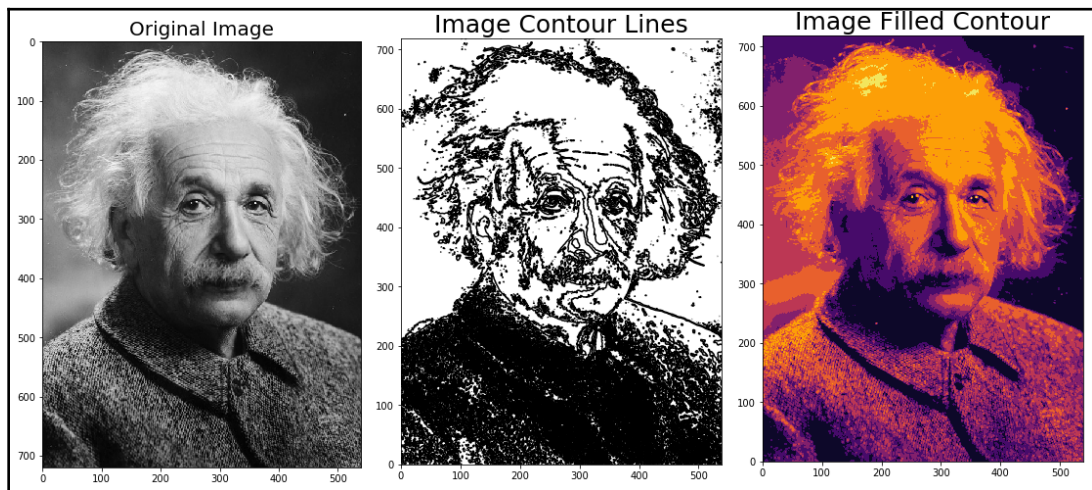
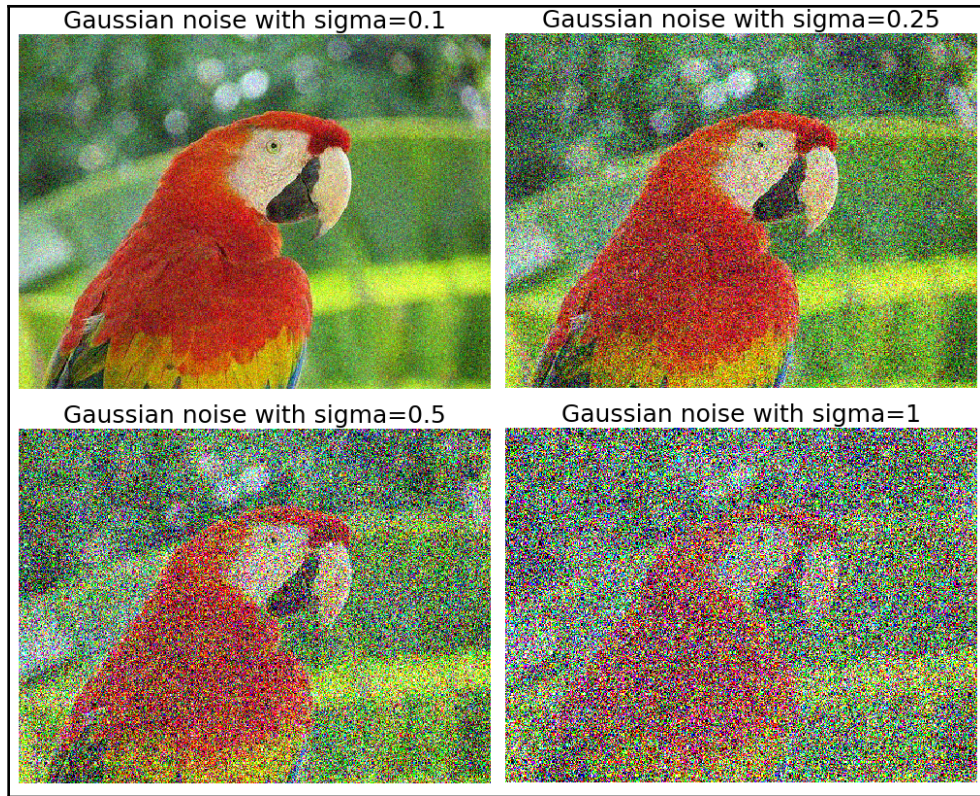


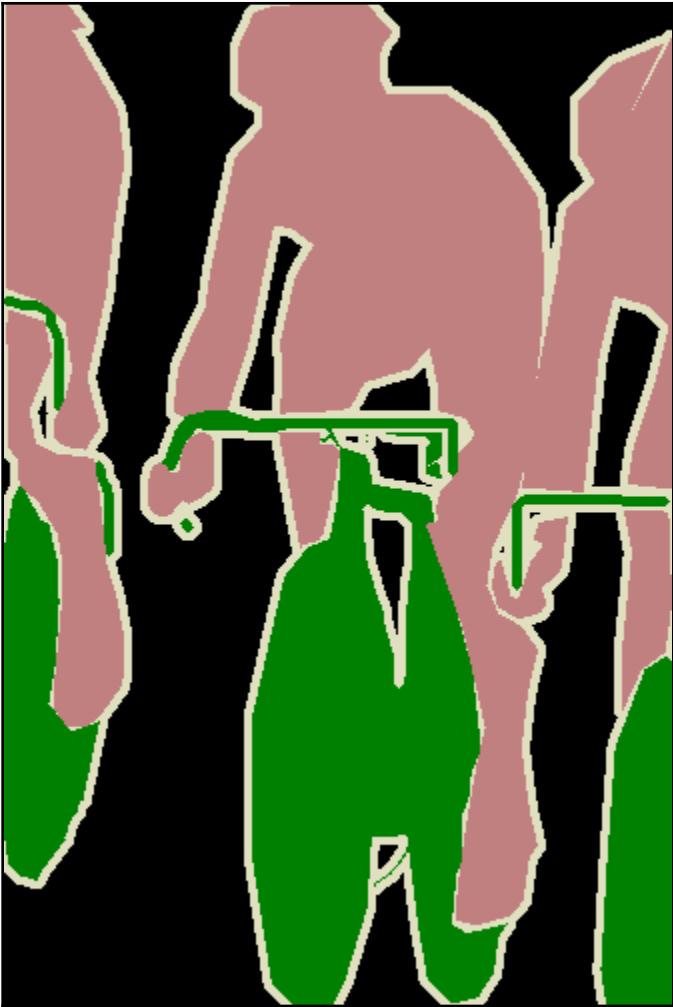








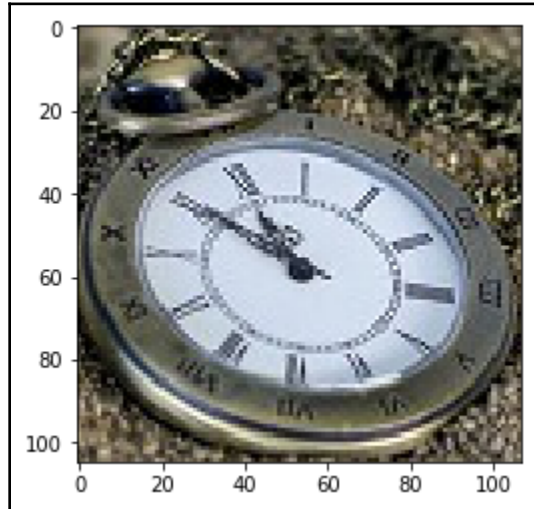








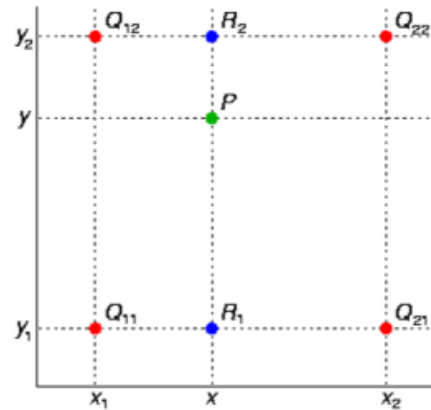
Chapter 2: Sampling, Fourier Transform, and Convolution





Bilinear interpolation

$$\begin{aligned} f(x, y) \approx & \frac{f(Q_{11})}{(x_2 - x_1)(y_2 - y_1)}(x_2 - x)(y_2 - y) \\ & + \frac{f(Q_{21})}{(x_2 - x_1)(y_2 - y_1)}(x - x_1)(y_2 - y) \\ & + \frac{f(Q_{12})}{(x_2 - x_1)(y_2 - y_1)}(x_2 - x)(y - y_1) \\ & + \frac{f(Q_{22})}{(x_2 - x_1)(y_2 - y_1)}(x - x_1)(y - y_1). \end{aligned}$$



http://en.wikipedia.org/wiki/Bilinear_interpolation









image size = 811x541



image size = 406x270



image size = 203x135



image size = 102x68



image size = 811x541



image size = 406x270



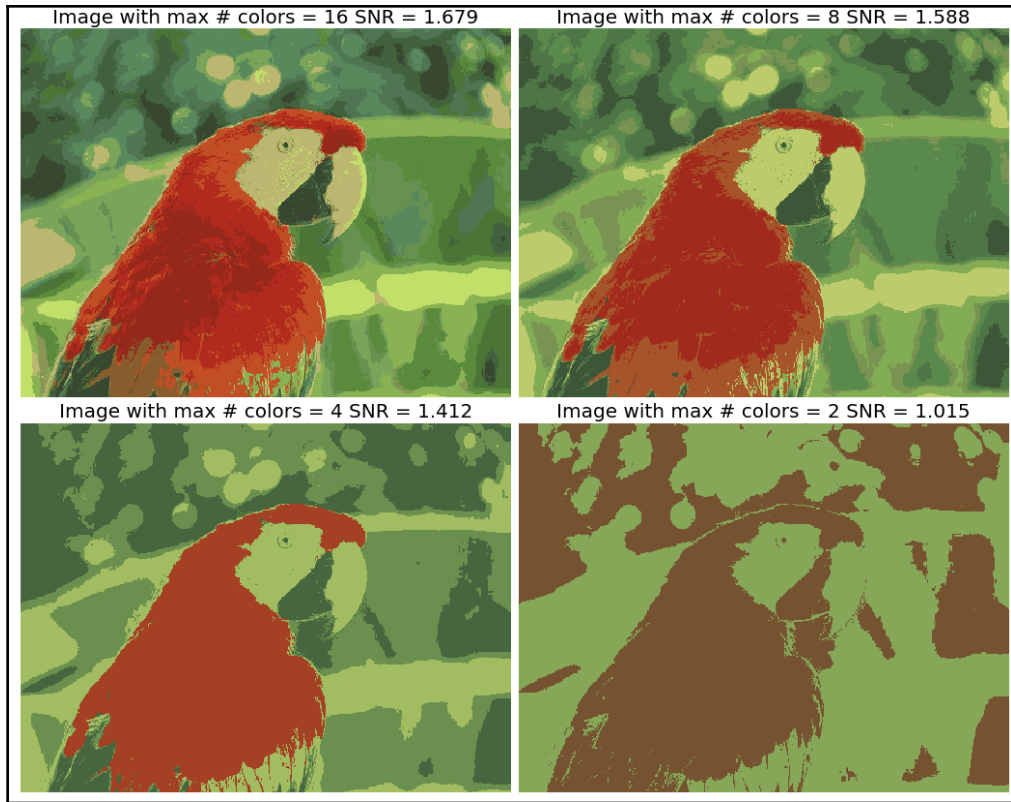
image size = 203x135

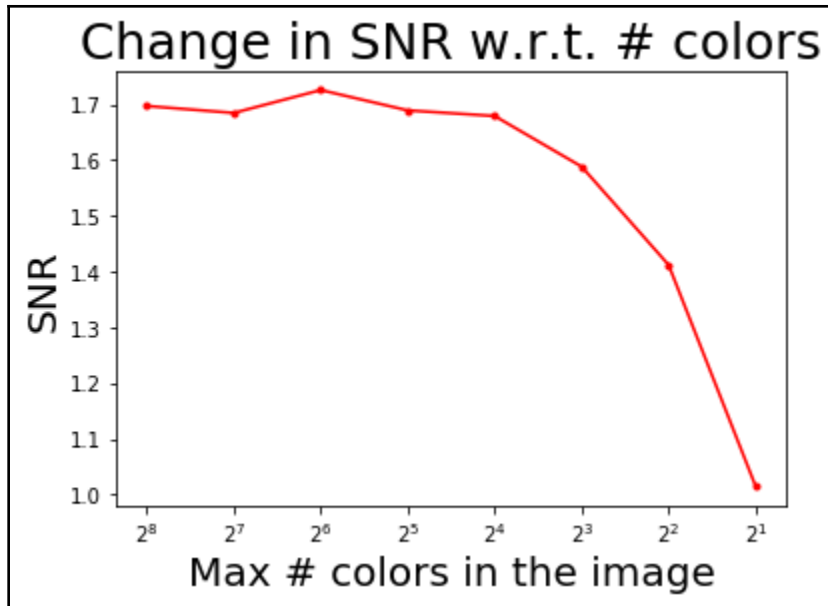


image size = 102x68









2D Discrete Fourier Transform (DFT)

$$F[u, v] = \frac{1}{MN} \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f[x, y] e^{-2\pi i \left(\frac{ux}{M} + \frac{vy}{N} \right)}$$



frequencies (frequency domain)



image (time domain)

$$u = 0, 1, \dots, M-1$$

$$v = 0, 1, \dots, N-1$$

2D Inverse Discrete Fourier Transform (IDFT)

$$f[x, y] = \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} F[u, v] e^{2\pi i \left(\frac{ux}{M} + \frac{vy}{N} \right)}$$



image (time domain)



frequencies (frequency domain)

$$x = 0, 1, \dots, M-1$$

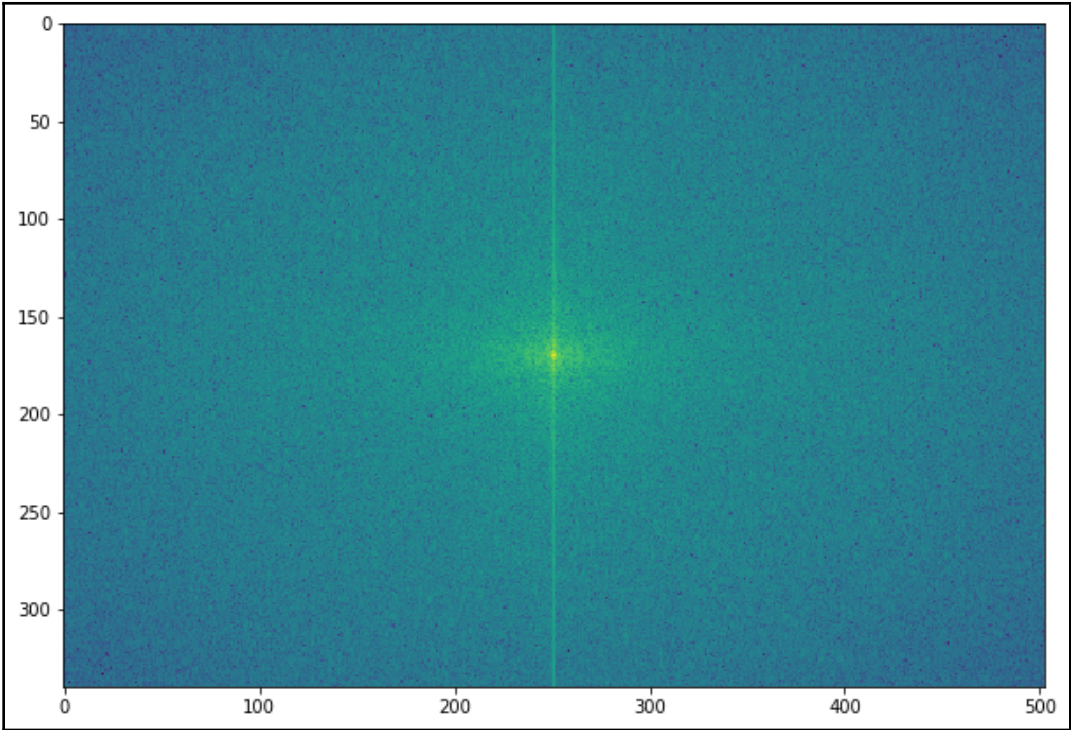
$$y = 0, 1, \dots, N-1$$

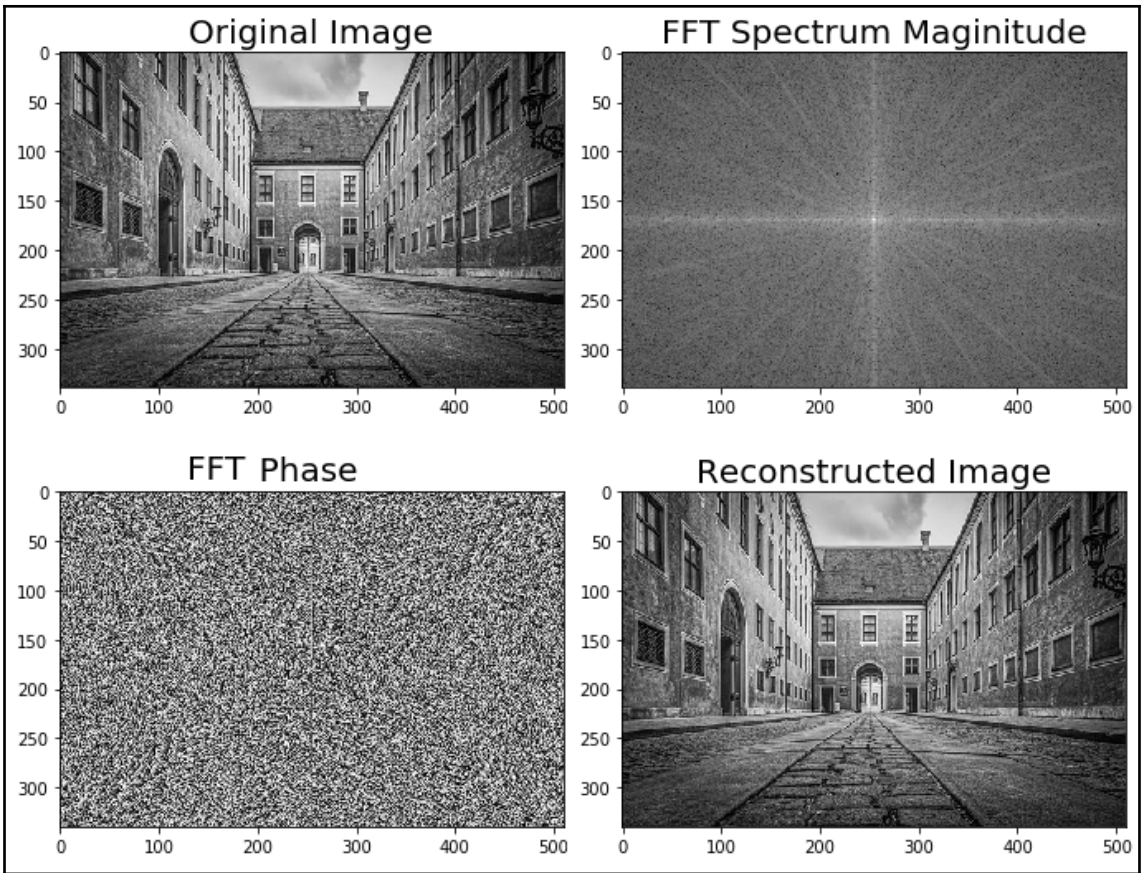
Original Image

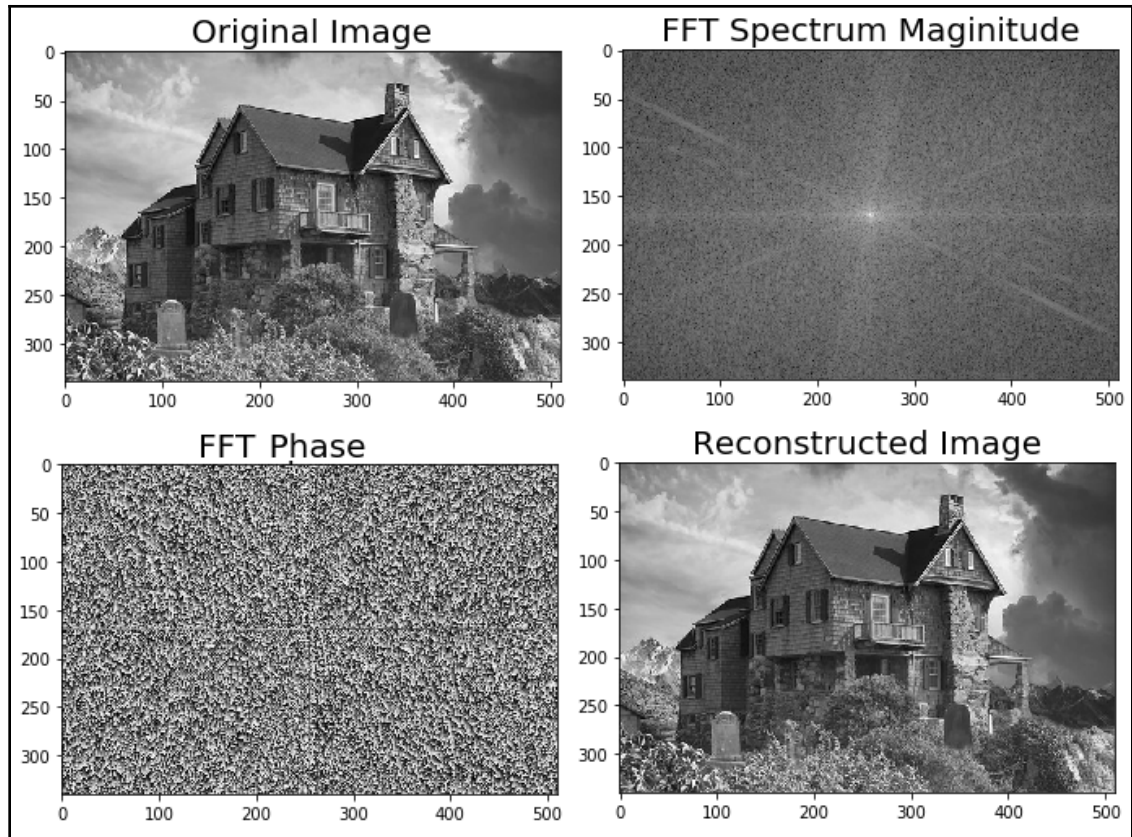


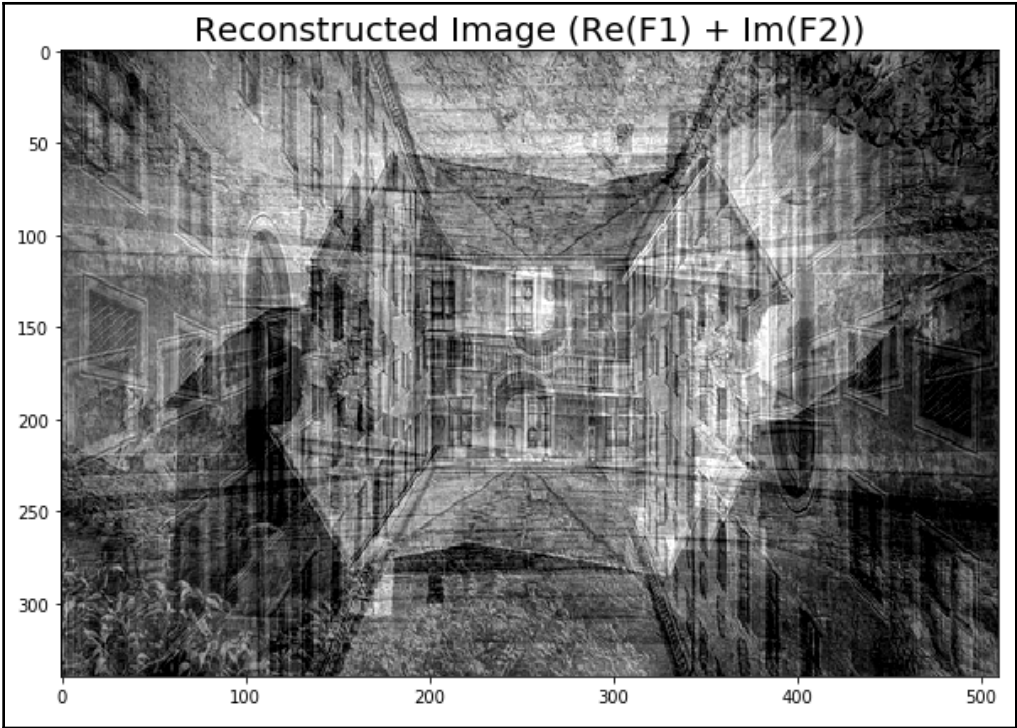
Image obtained after reconstruction

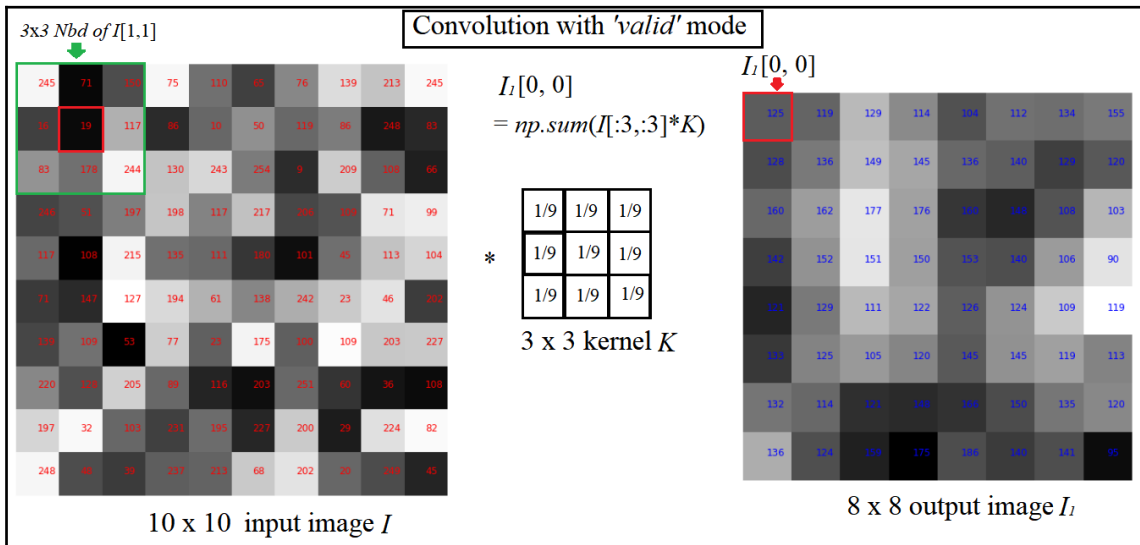
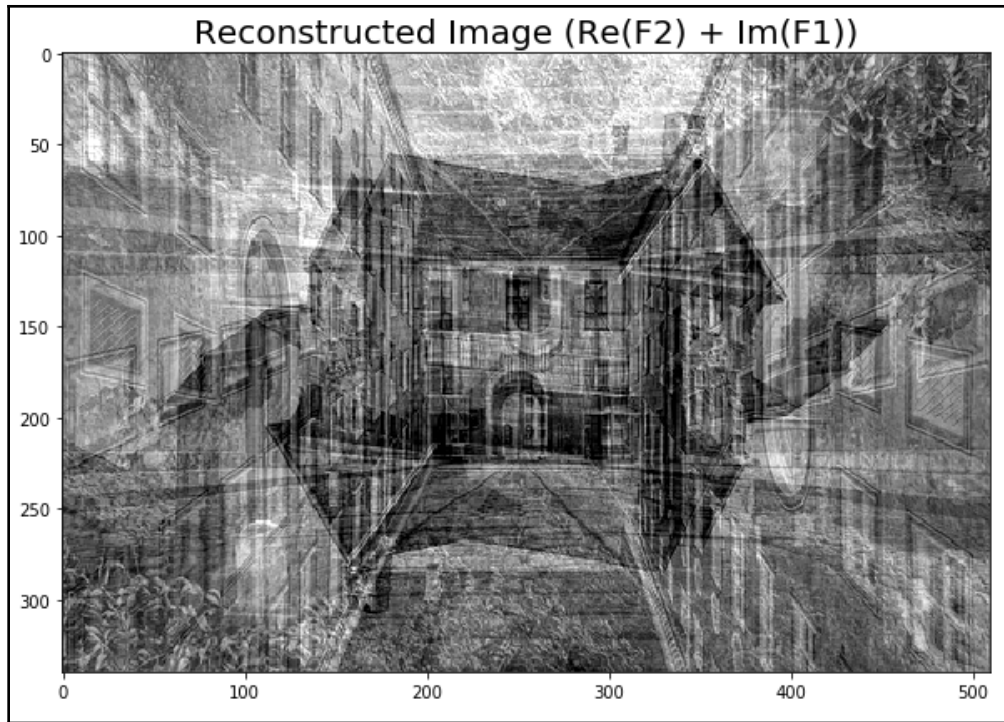










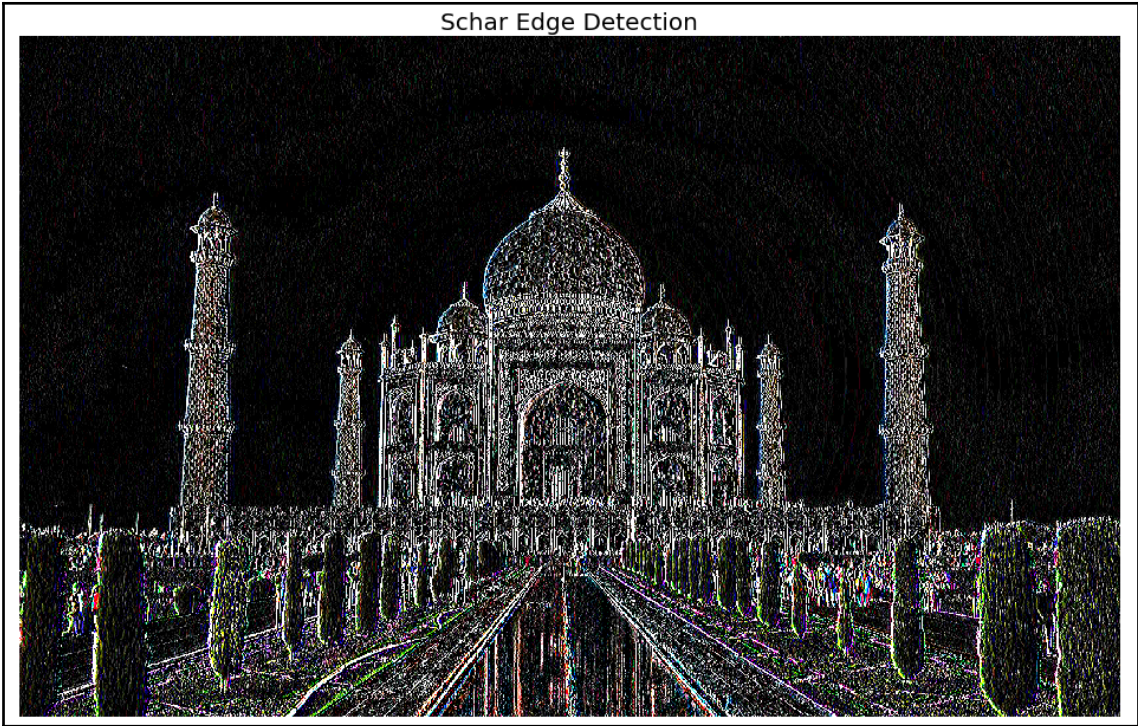




Embossed Image



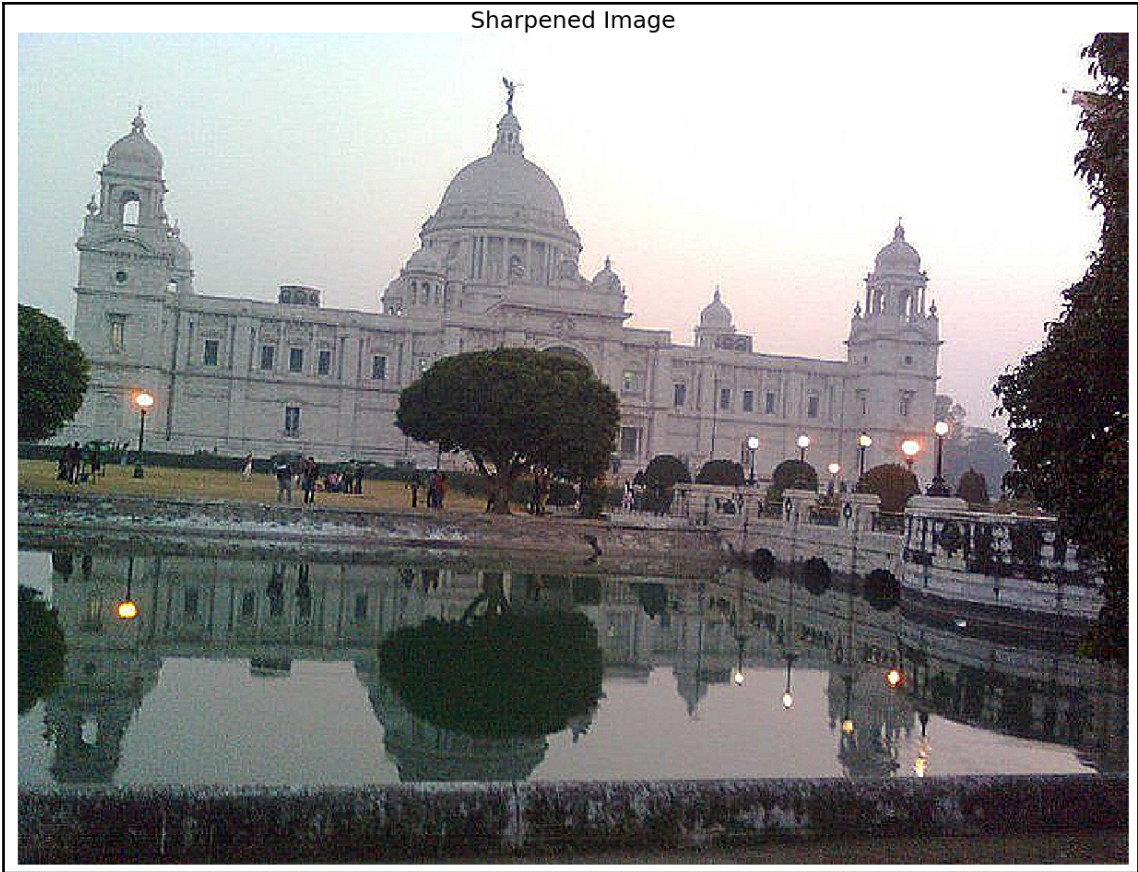
Schar Edge Detection



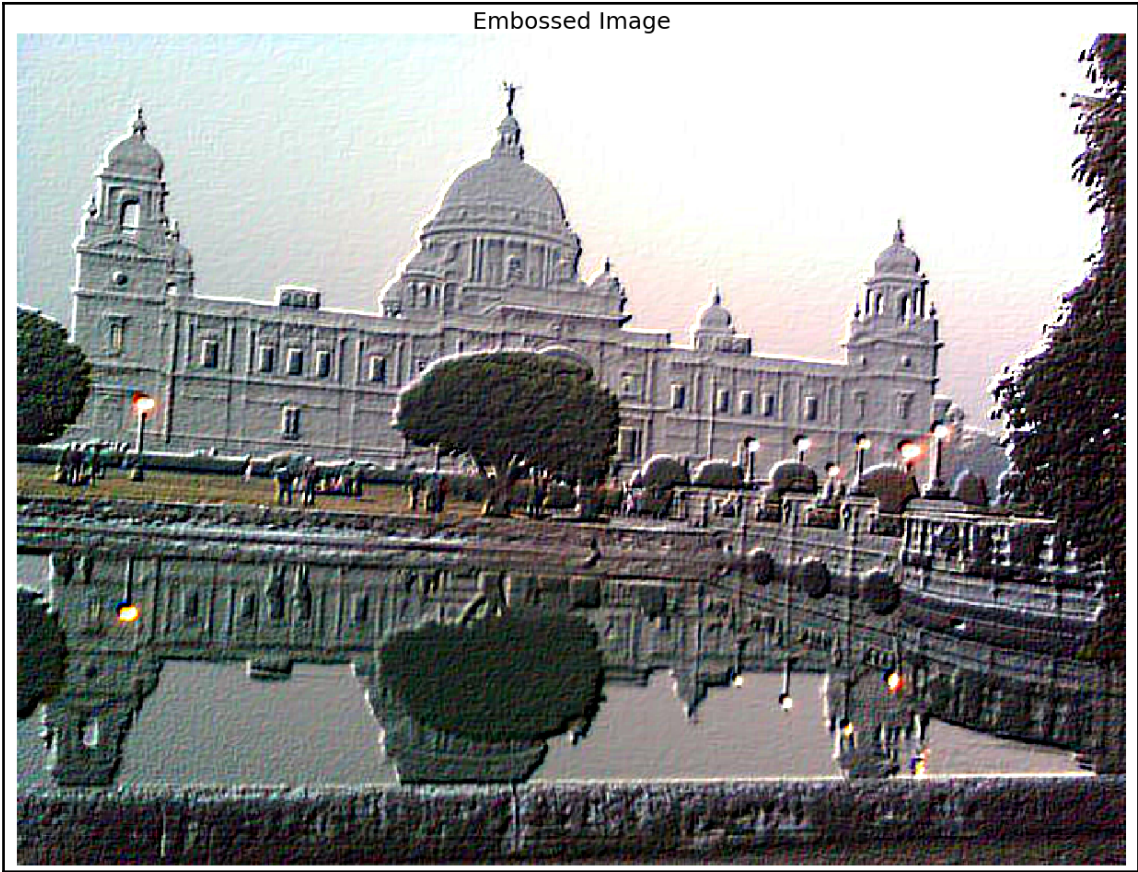
Original Image



Sharpened Image



Embossed Image



Correlation

$$\mathbf{g}(x, y) = \mathbf{f} \star \mathbf{K} = \sum_{u=-h}^h \sum_{v=-h}^h \mathbf{f}(x+u, y+v) \mathbf{K}(u, v)$$

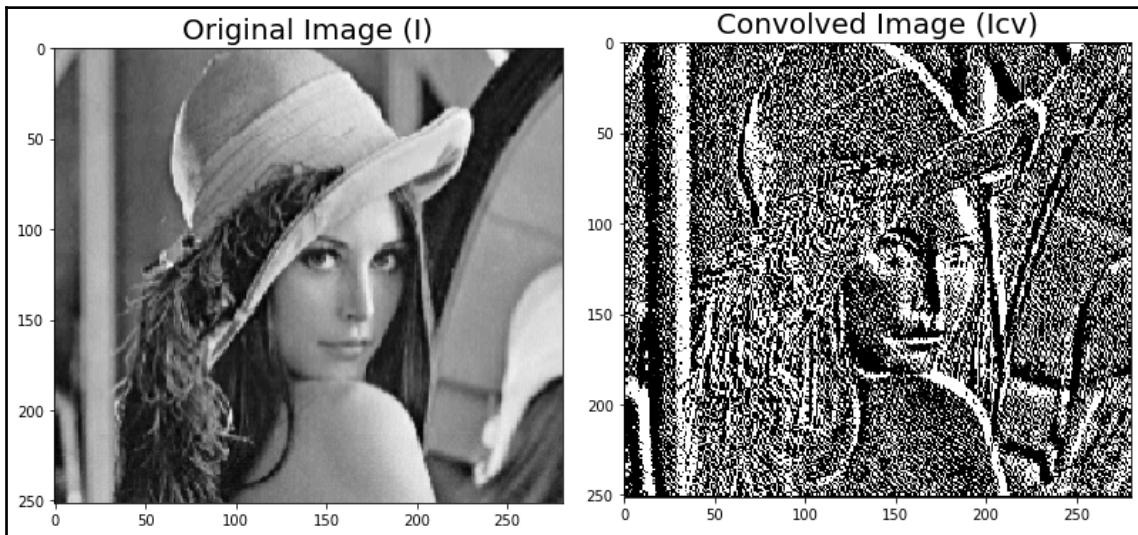


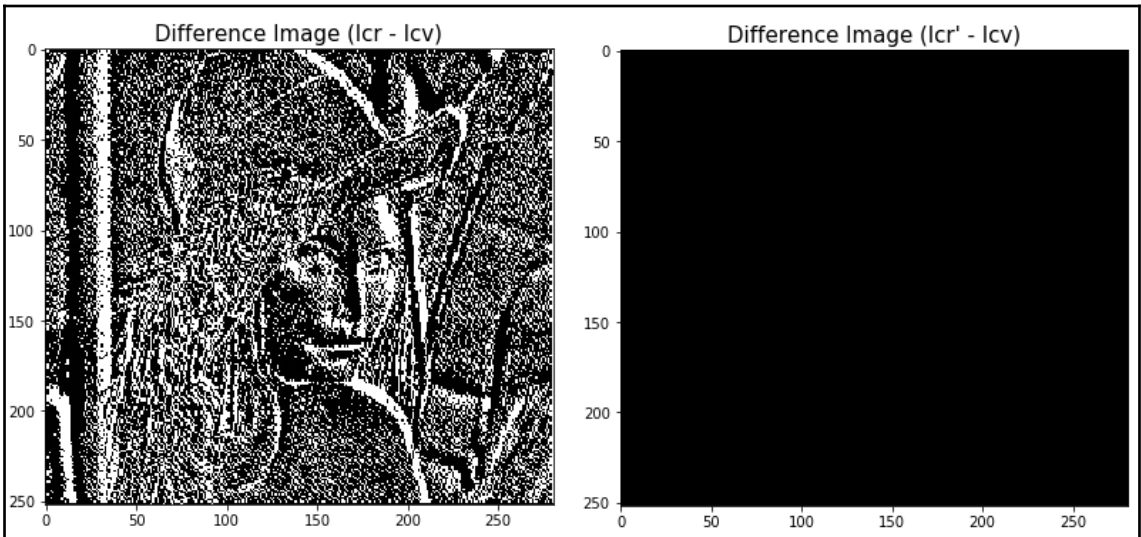
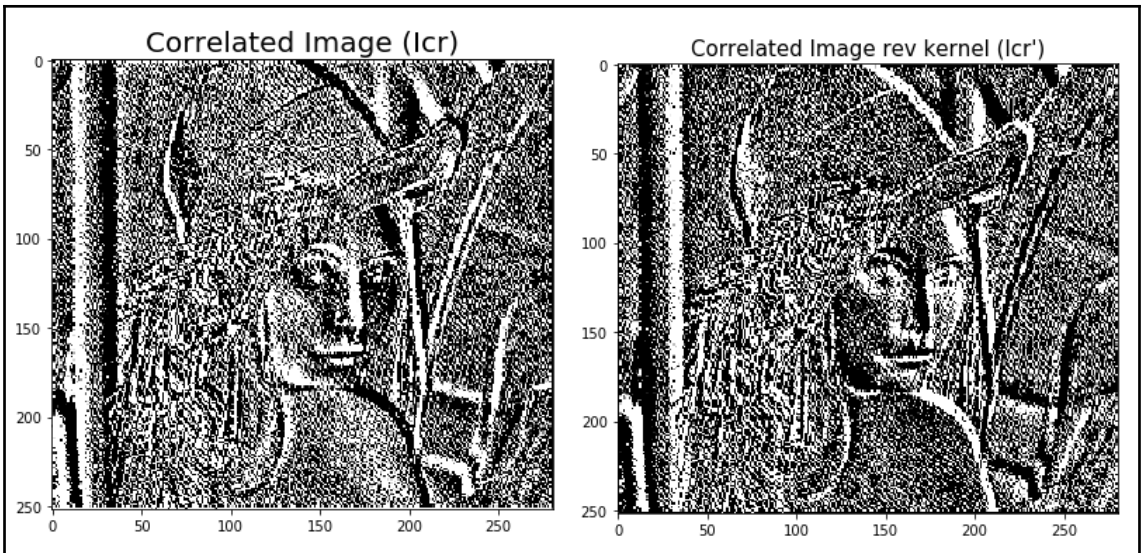
Convolution

$h \times h$ kernel \mathbf{K}



$$\mathbf{g}(x, y) = \mathbf{f} * \mathbf{K} = \sum_{u=-h}^h \sum_{v=-h}^h \mathbf{f}(x-u, y-v) \mathbf{K}(u, v)$$





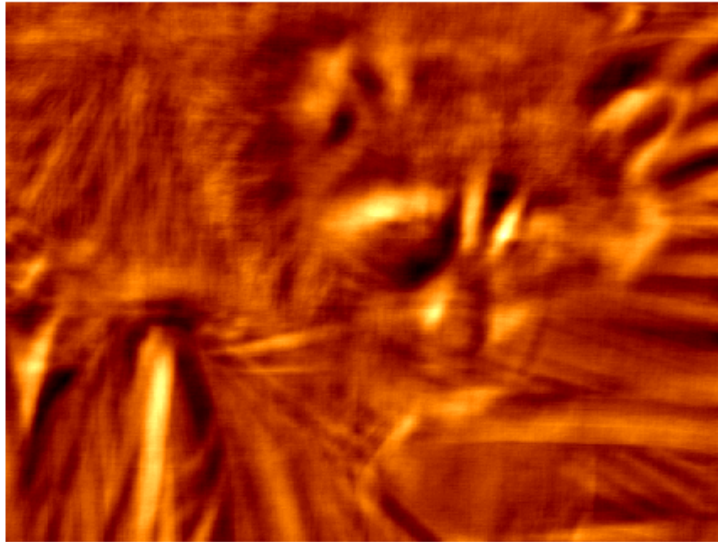
Original



Template



Cross-correlation

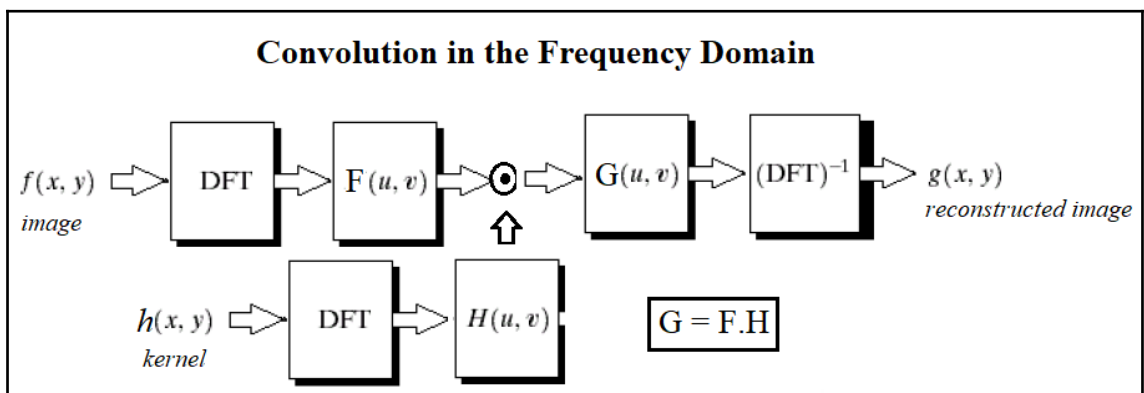
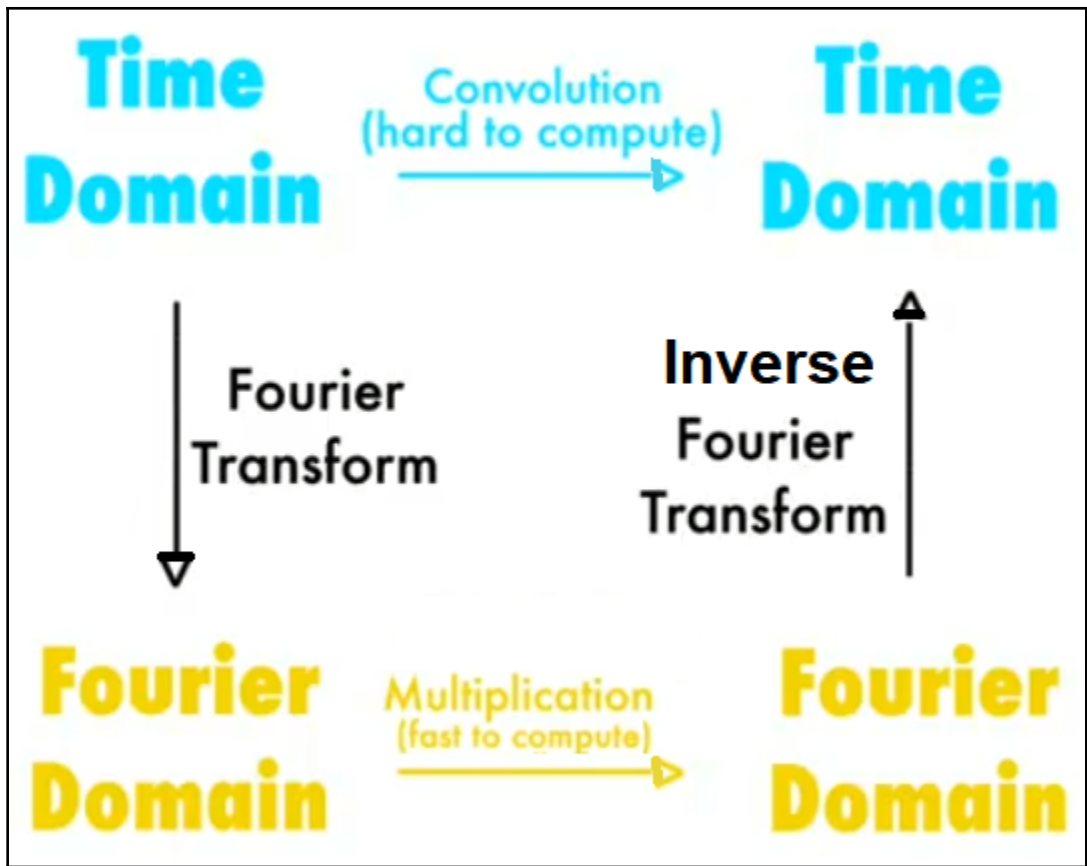


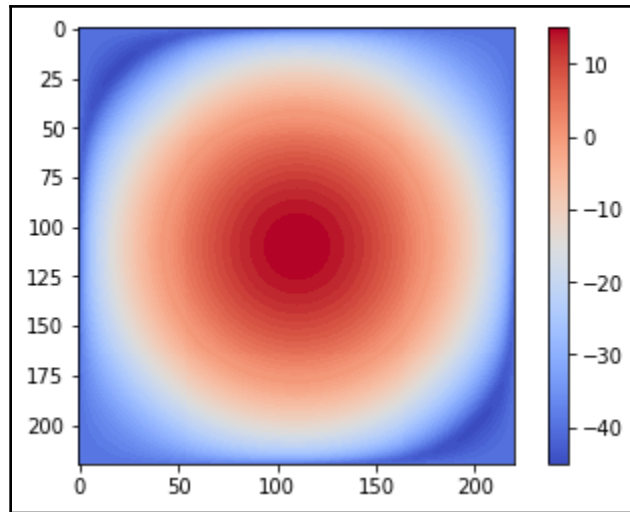
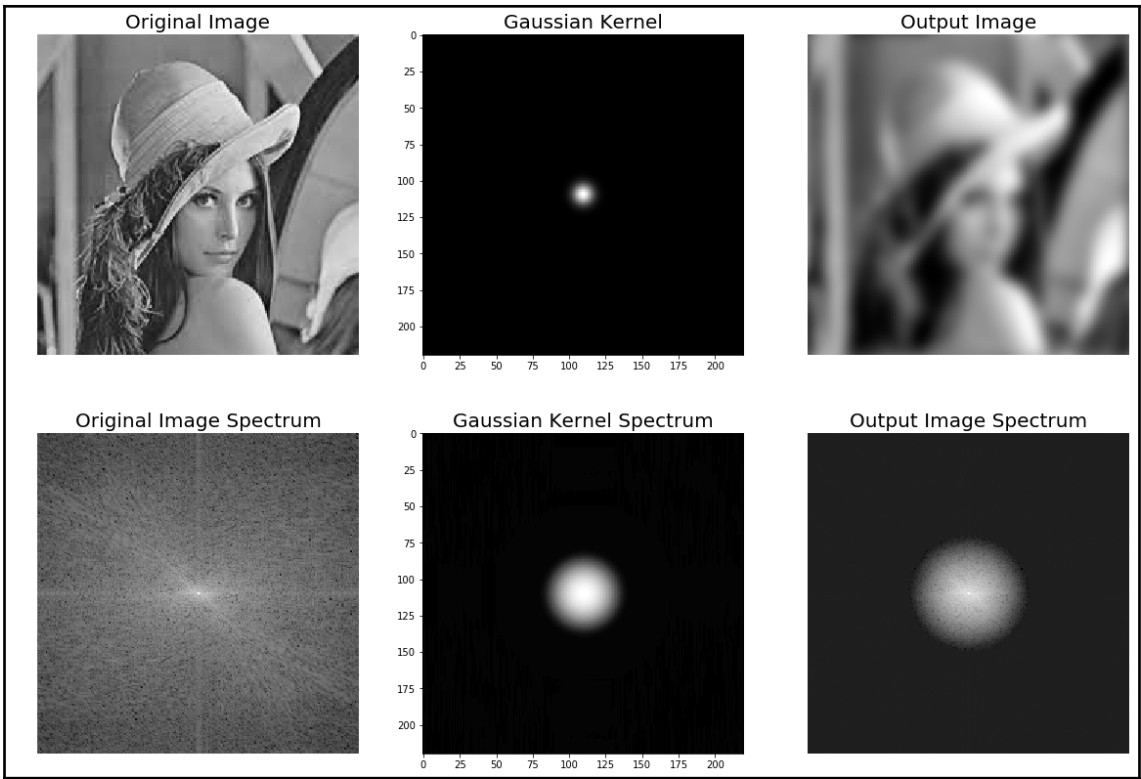
Chapter 3: Convolution and Frequency Domain Filtering

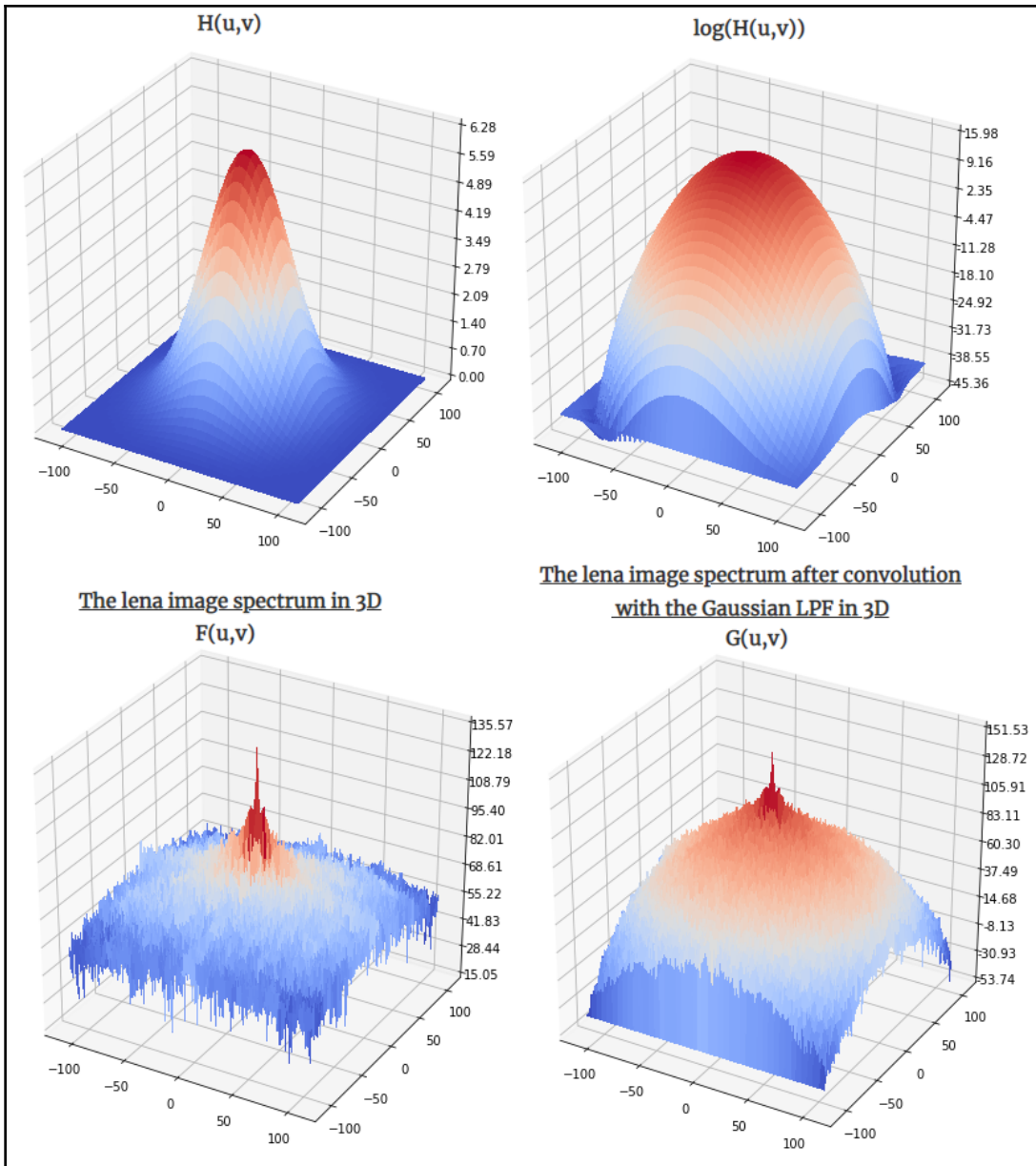
Convolution theorem

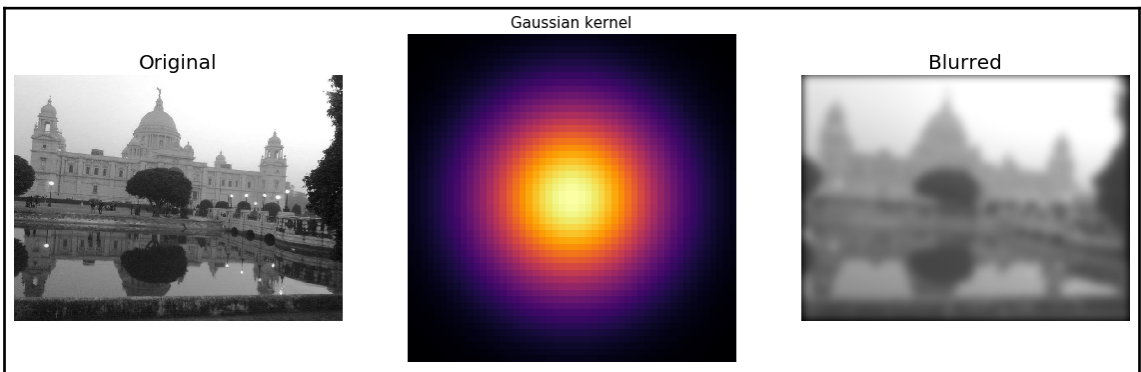
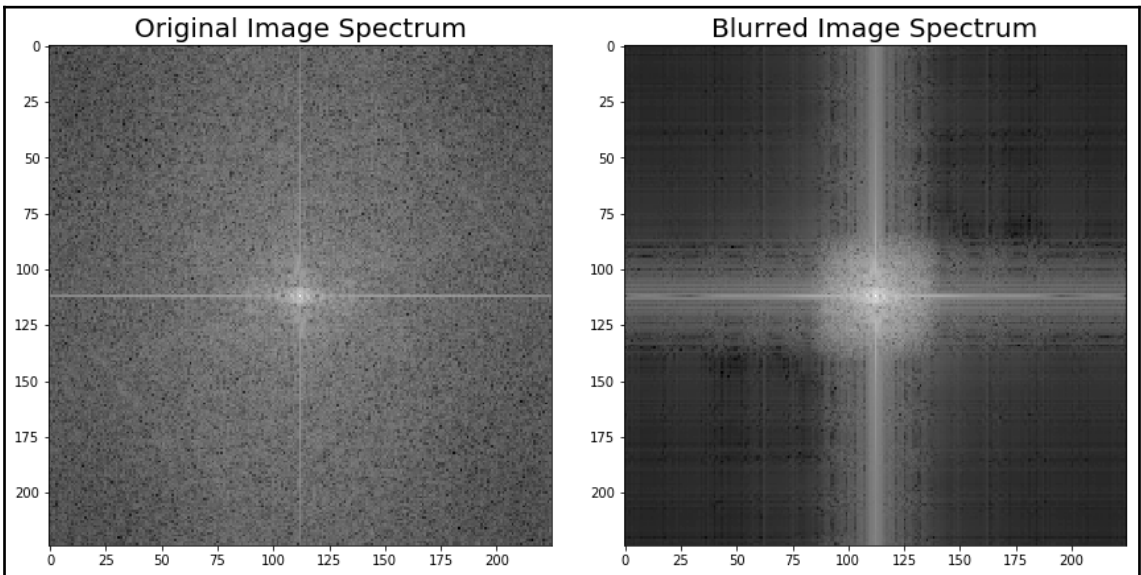
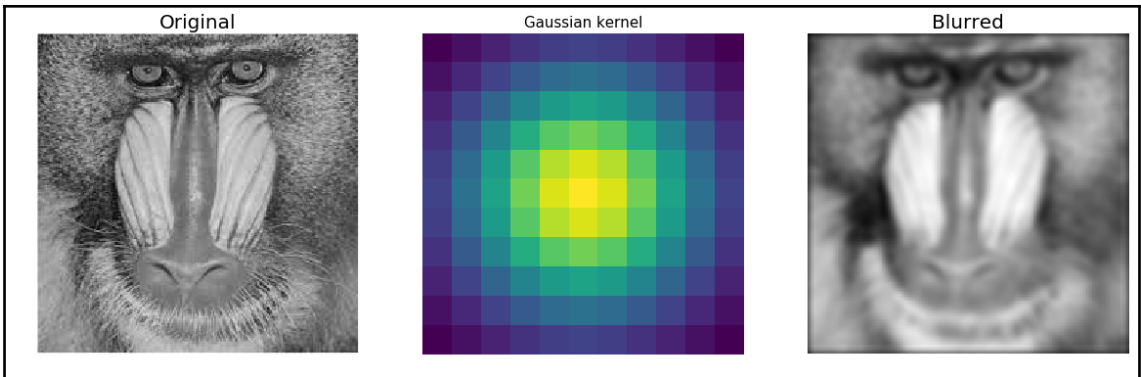
$$f(x, y) * h(x, y) \Leftrightarrow F(u, v)H(u, v)$$

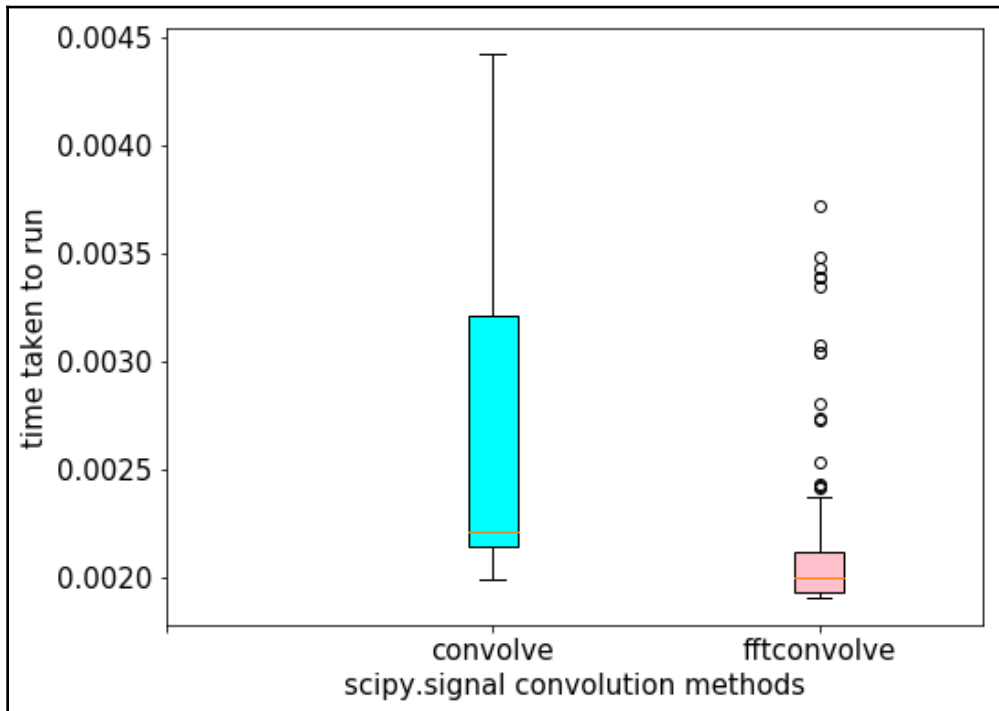
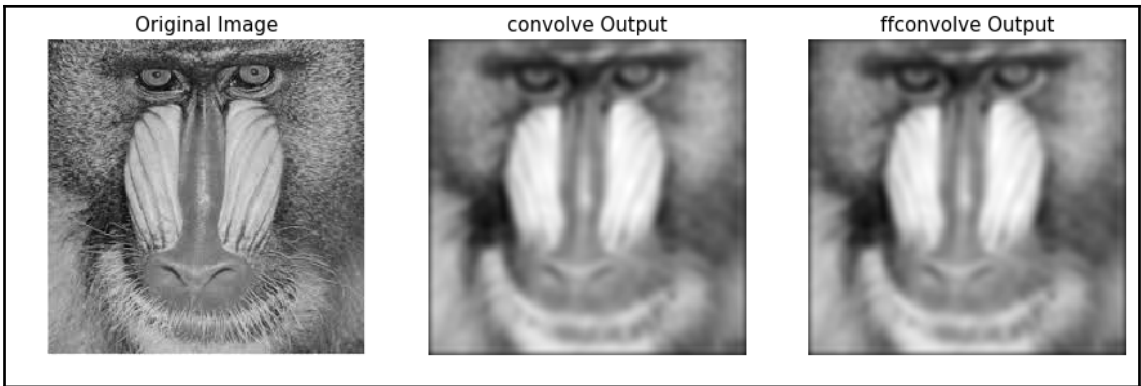
Space convolution = frequency multiplication



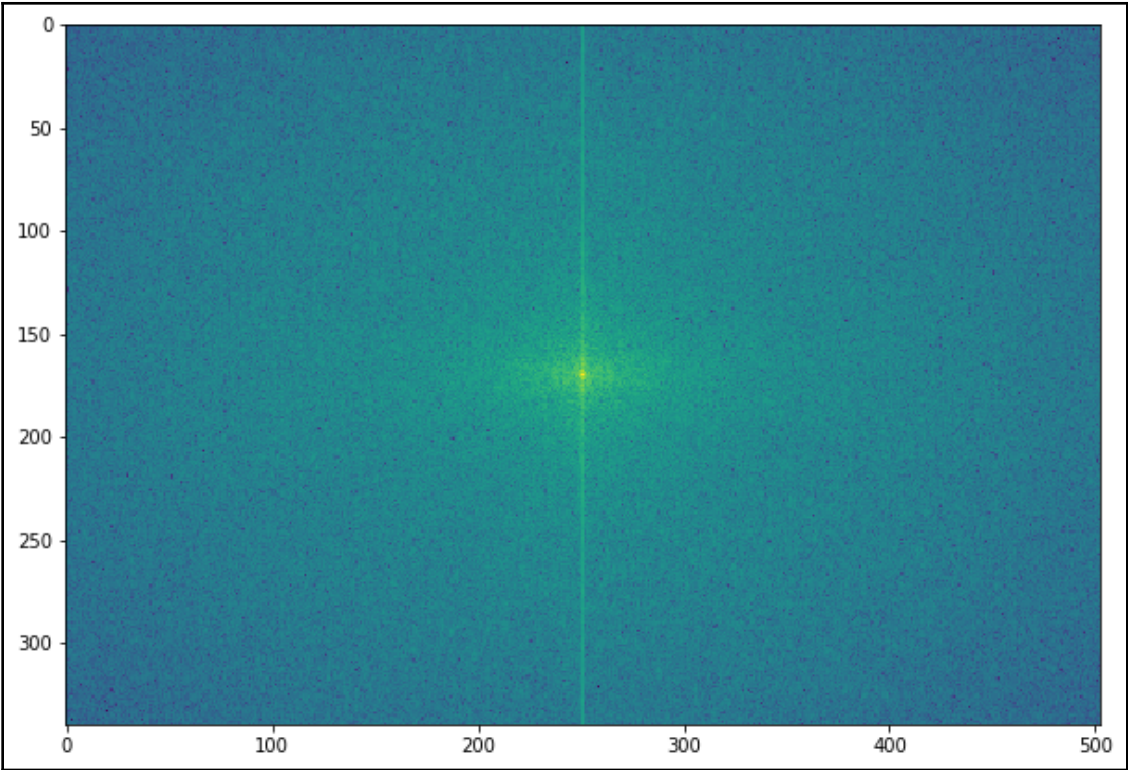


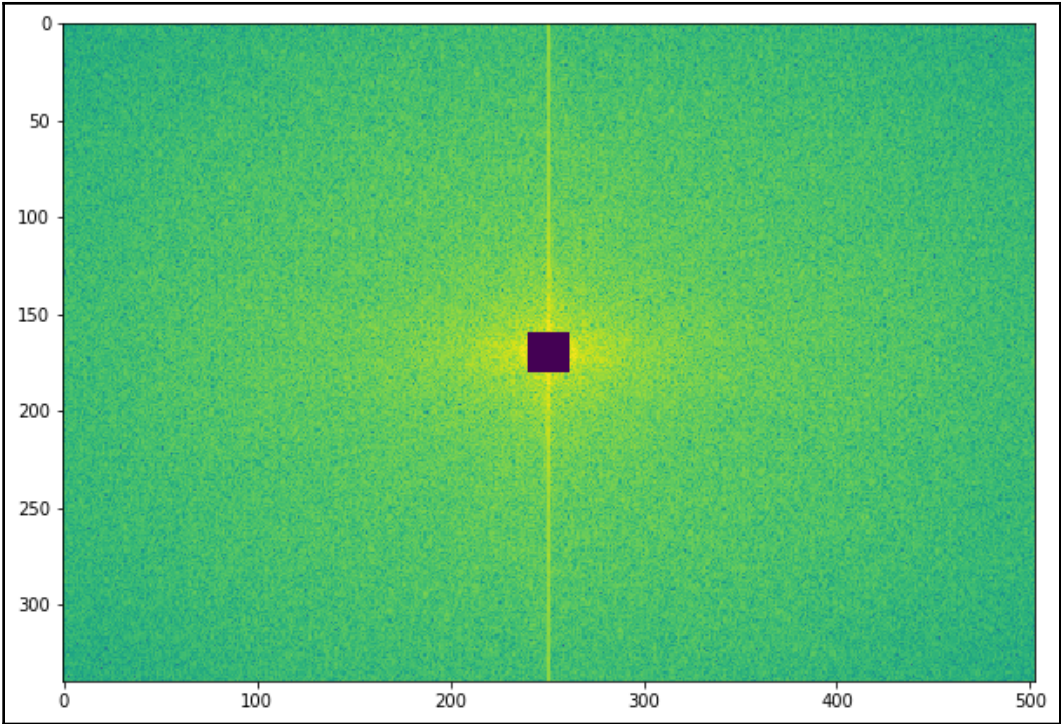


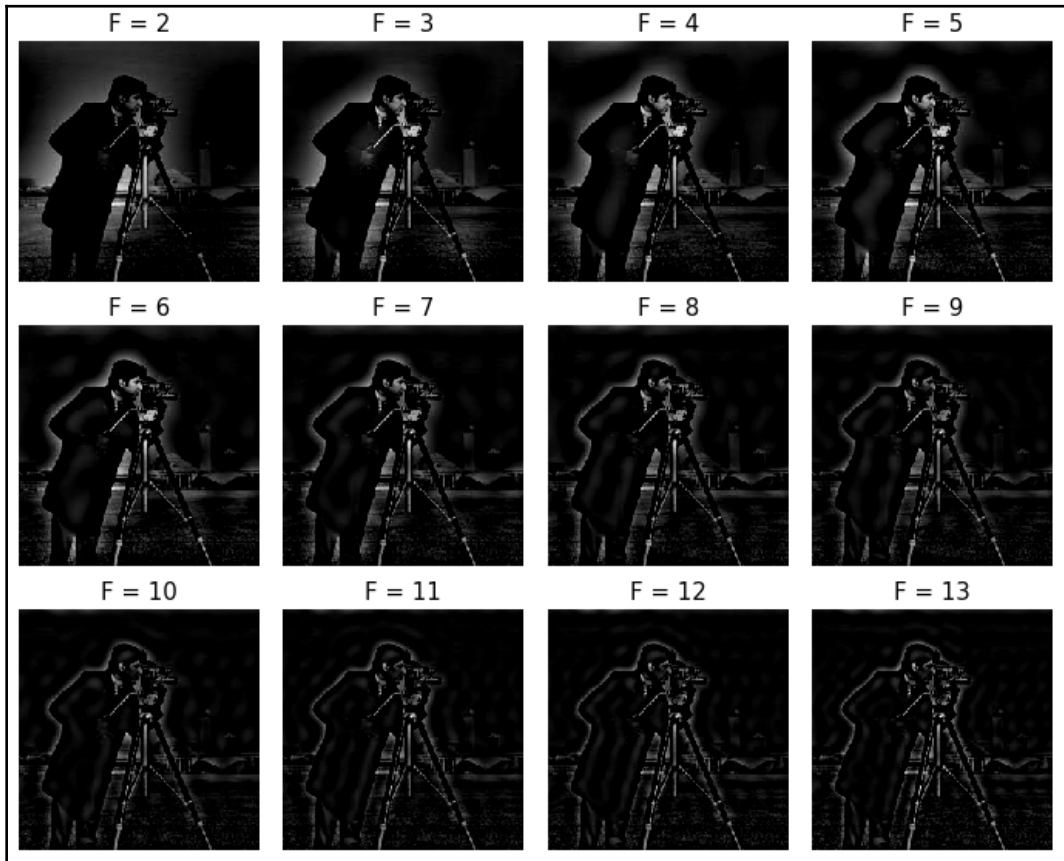


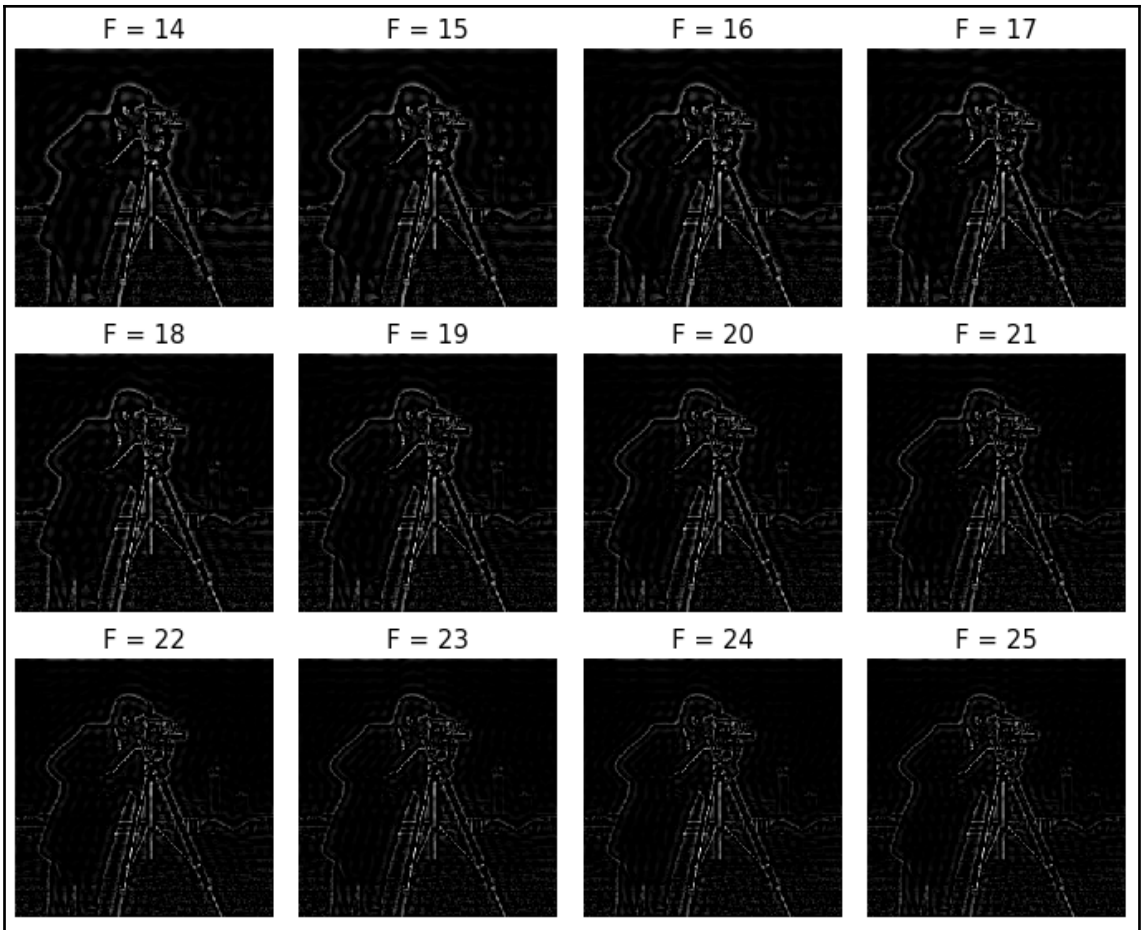


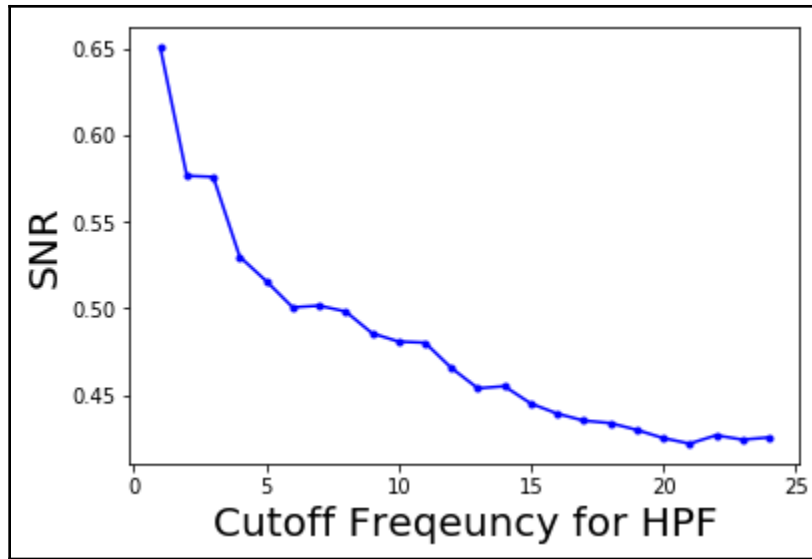


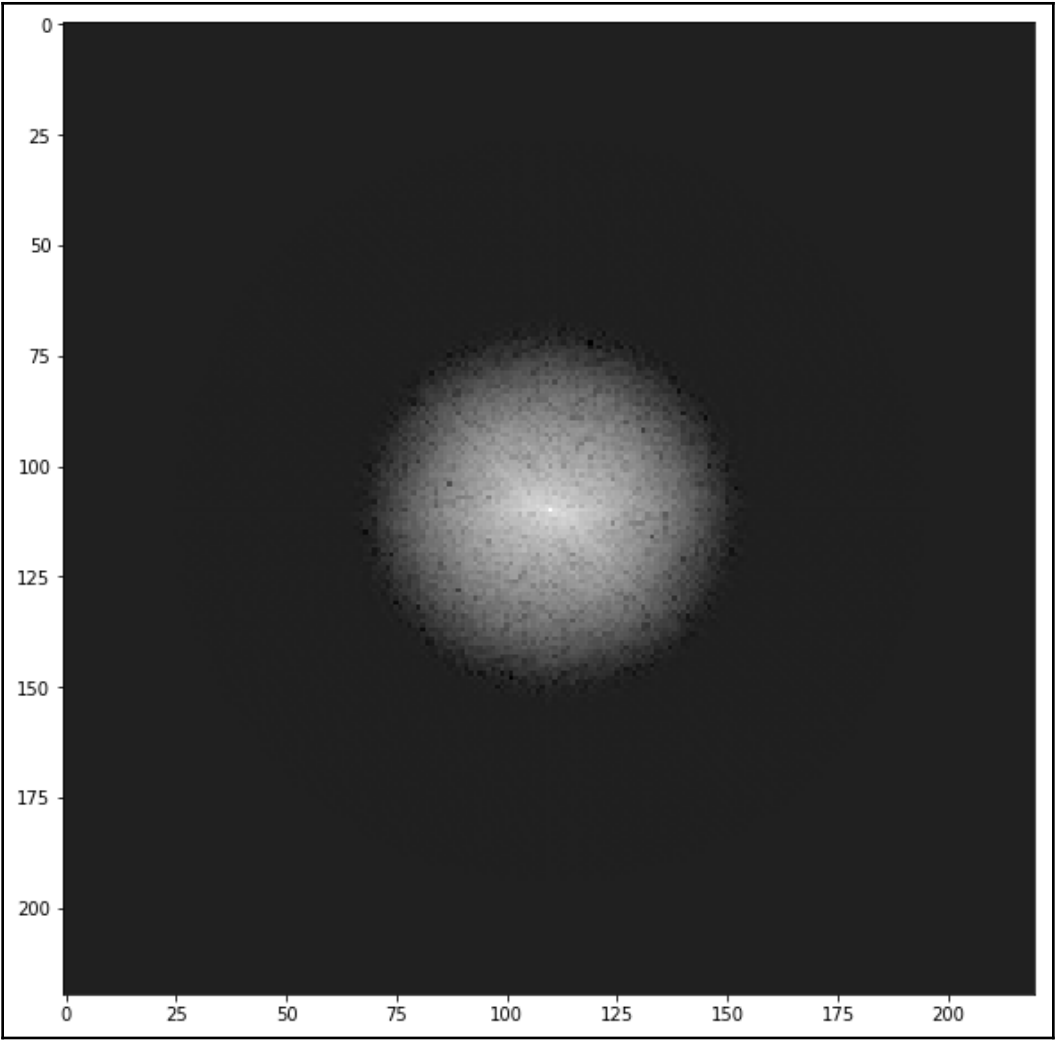


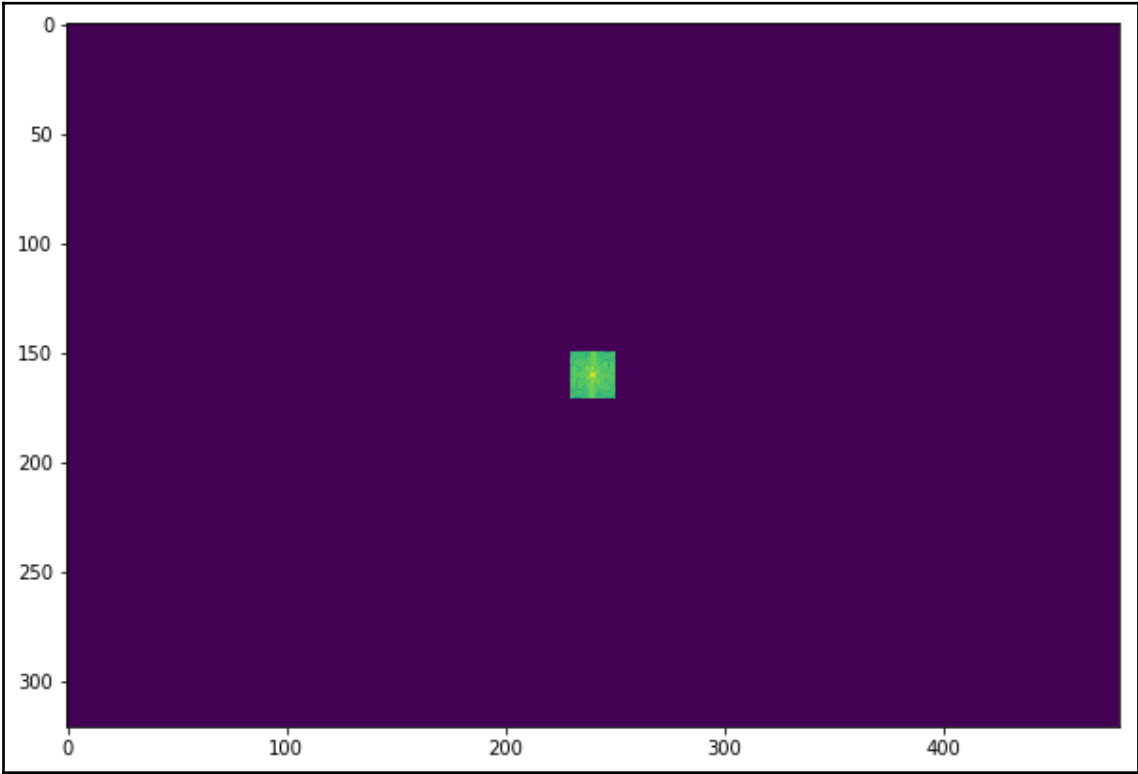


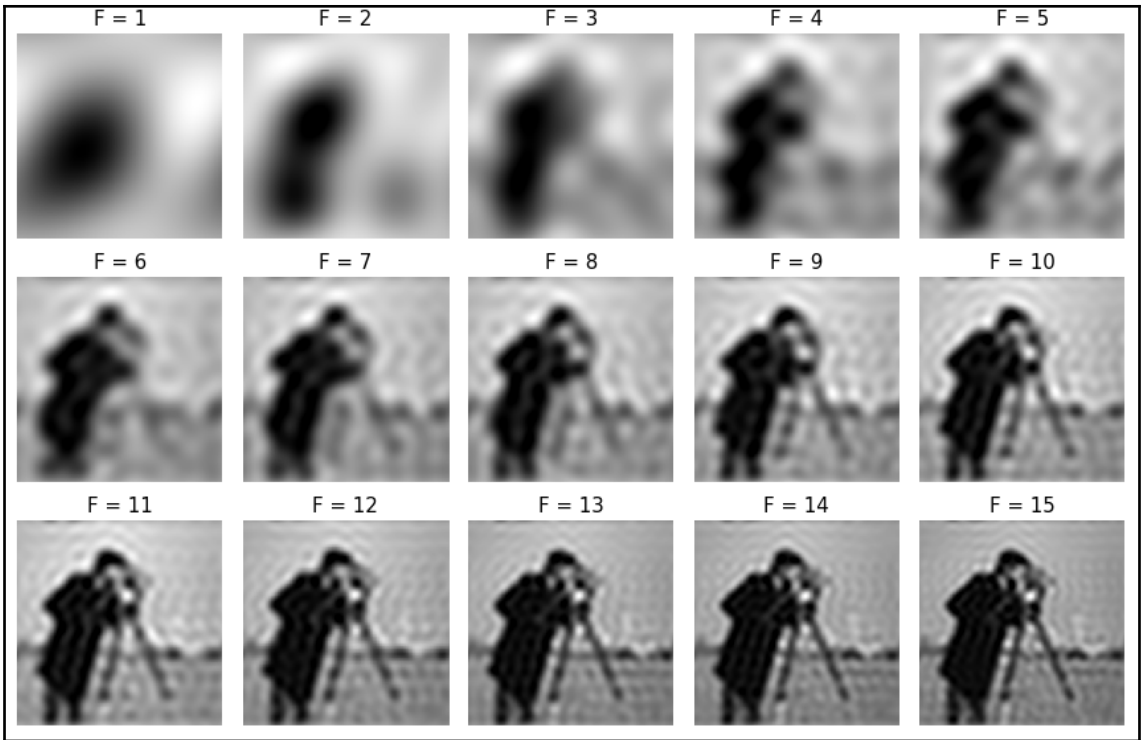


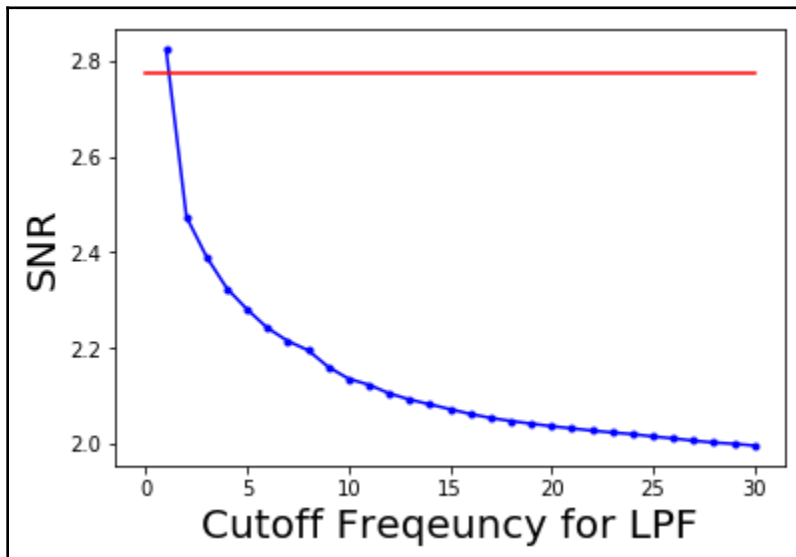
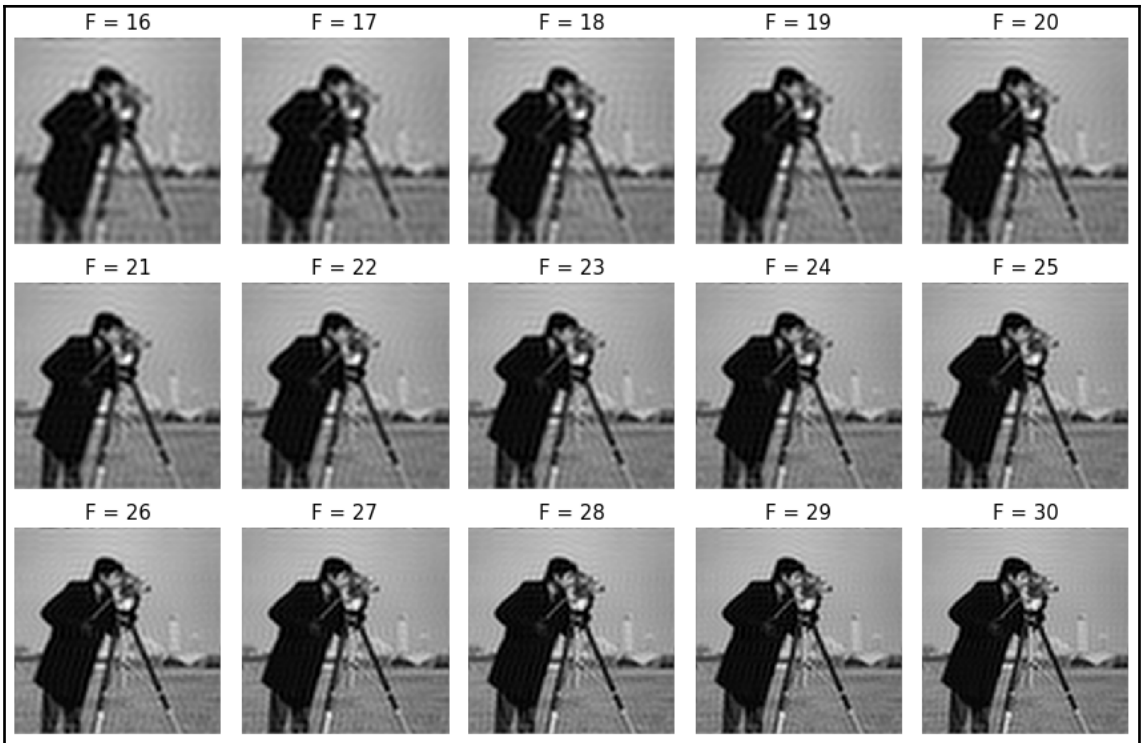


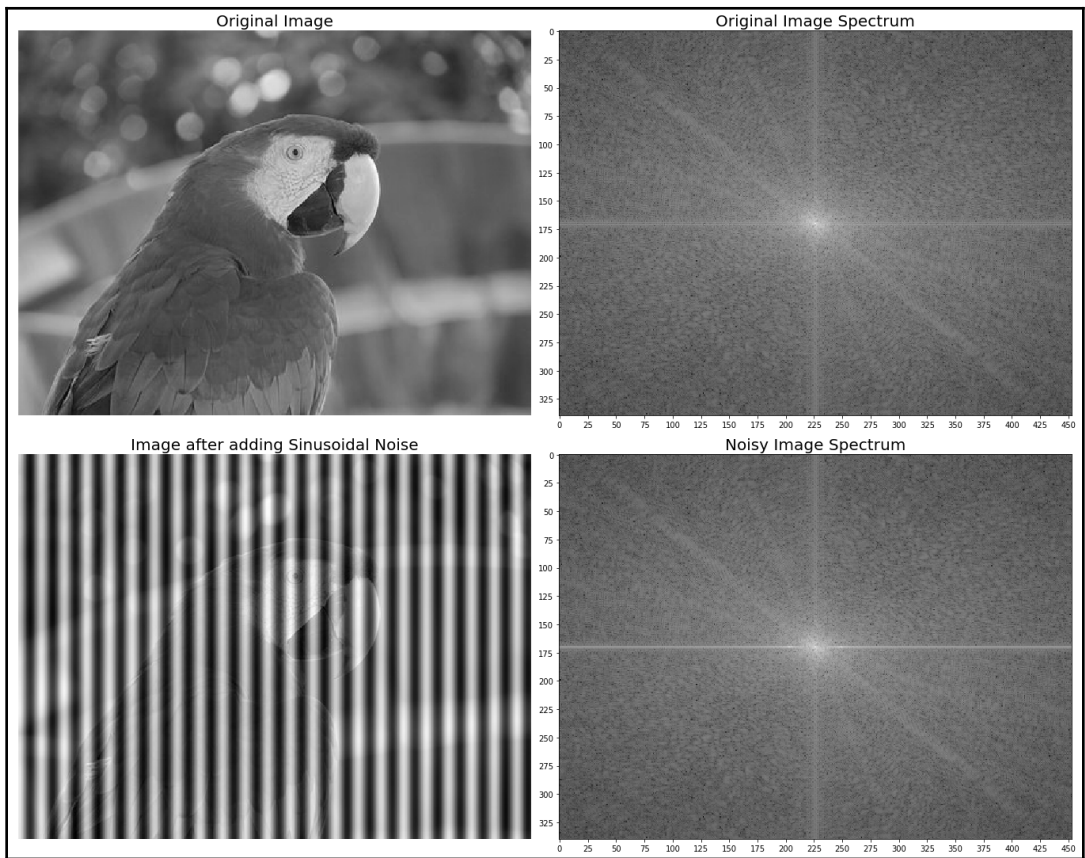
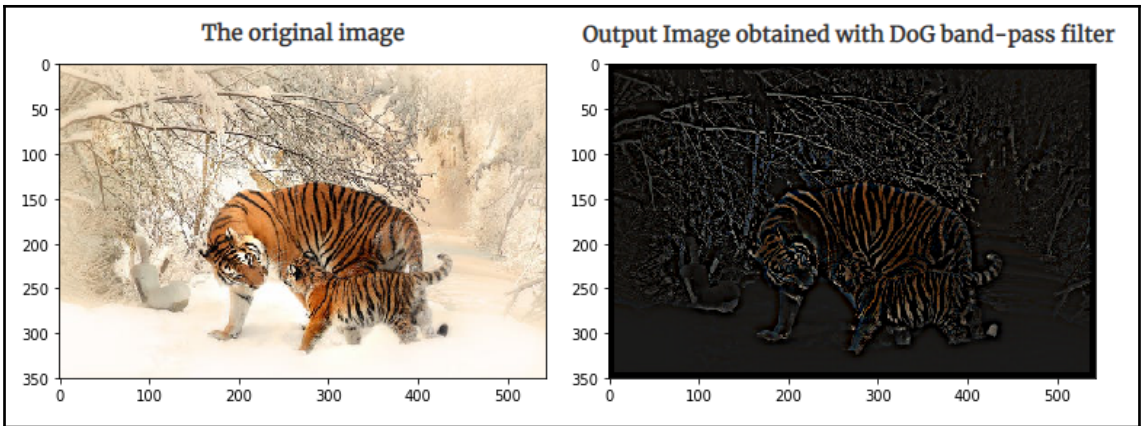


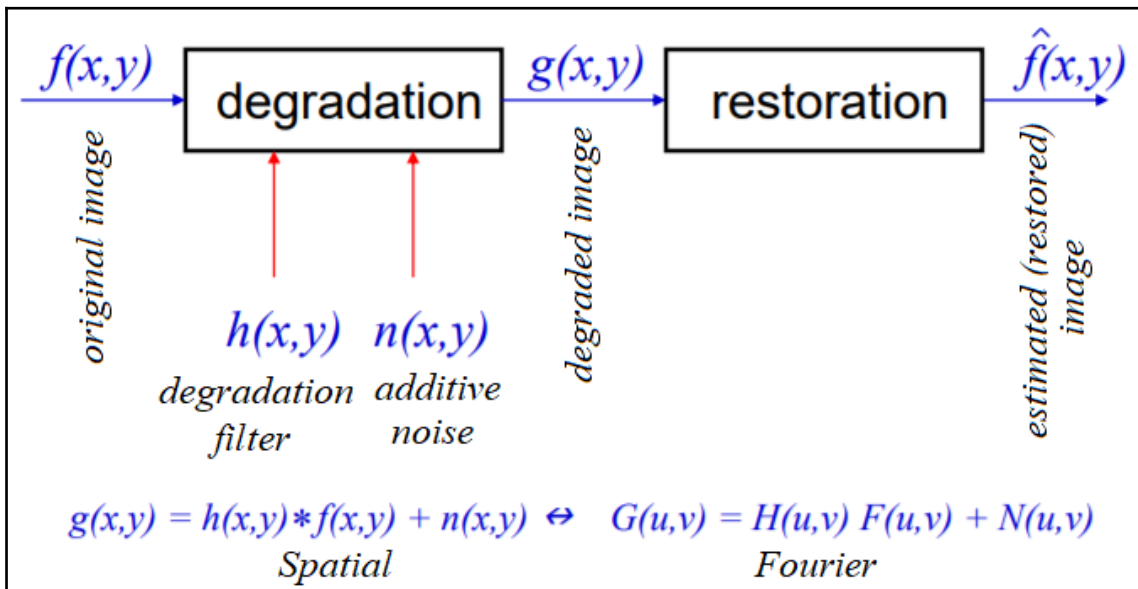






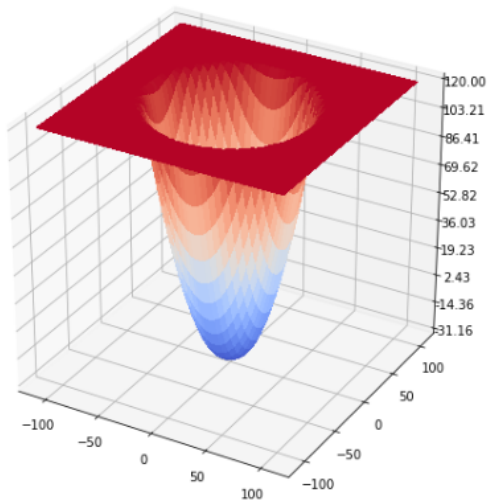




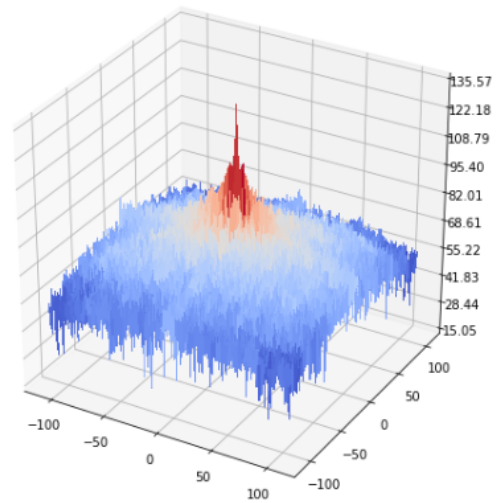




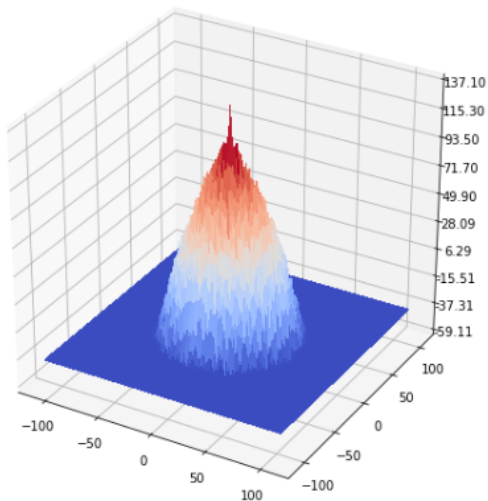
The frequency spectrum of the inverse filter (H)



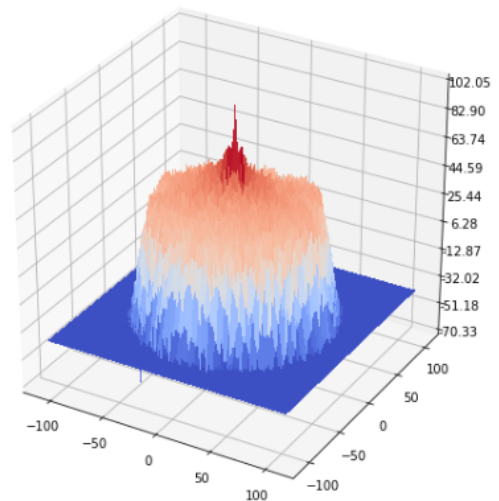
The frequency spectrum of the original Lena image

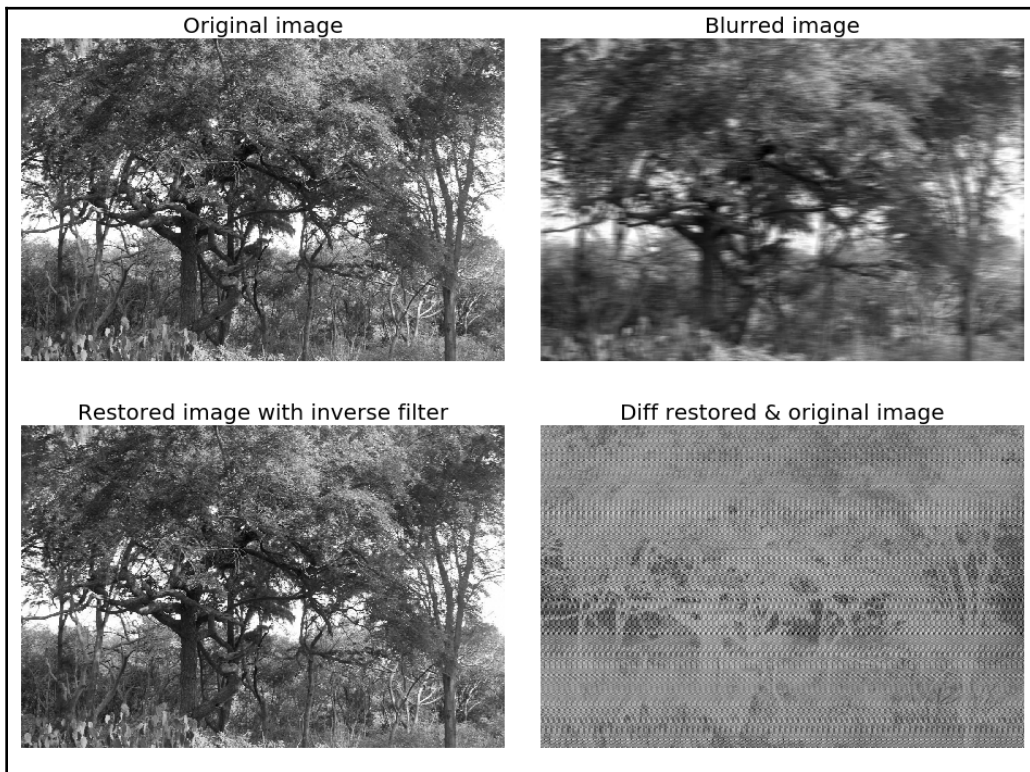
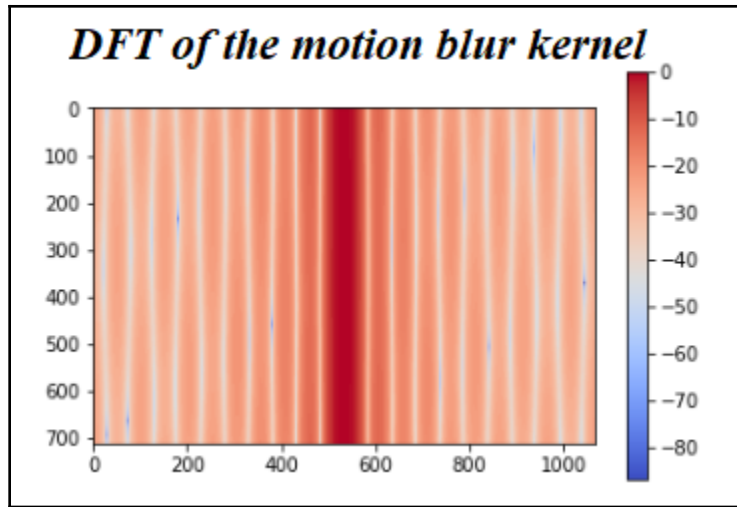


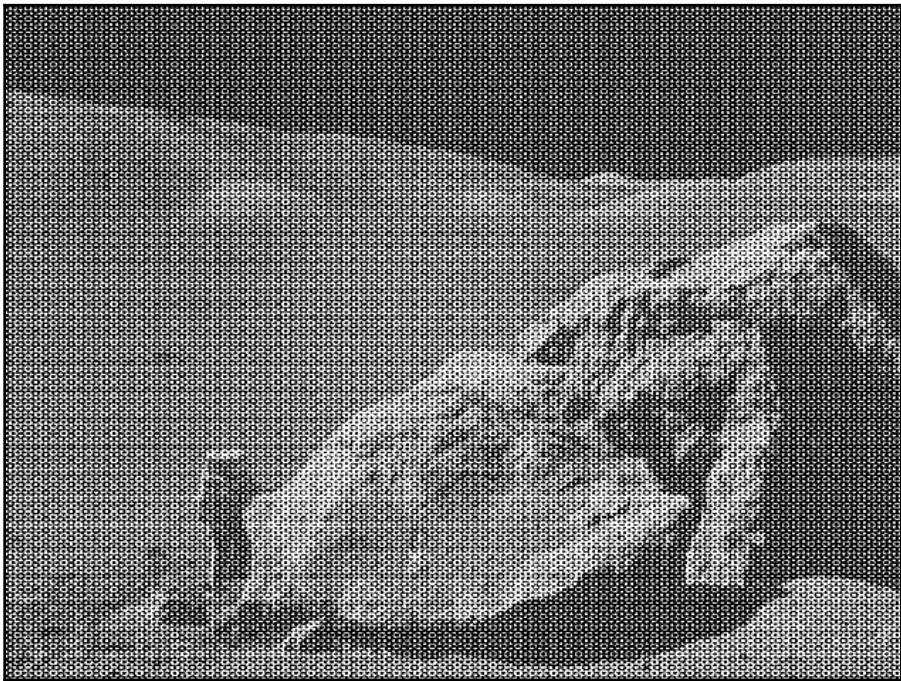
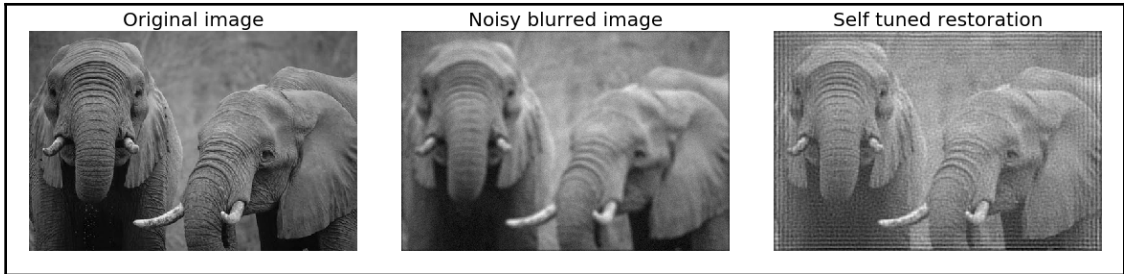
The frequency spectrum of the blurred Lena image
(with Gaussian LPF)

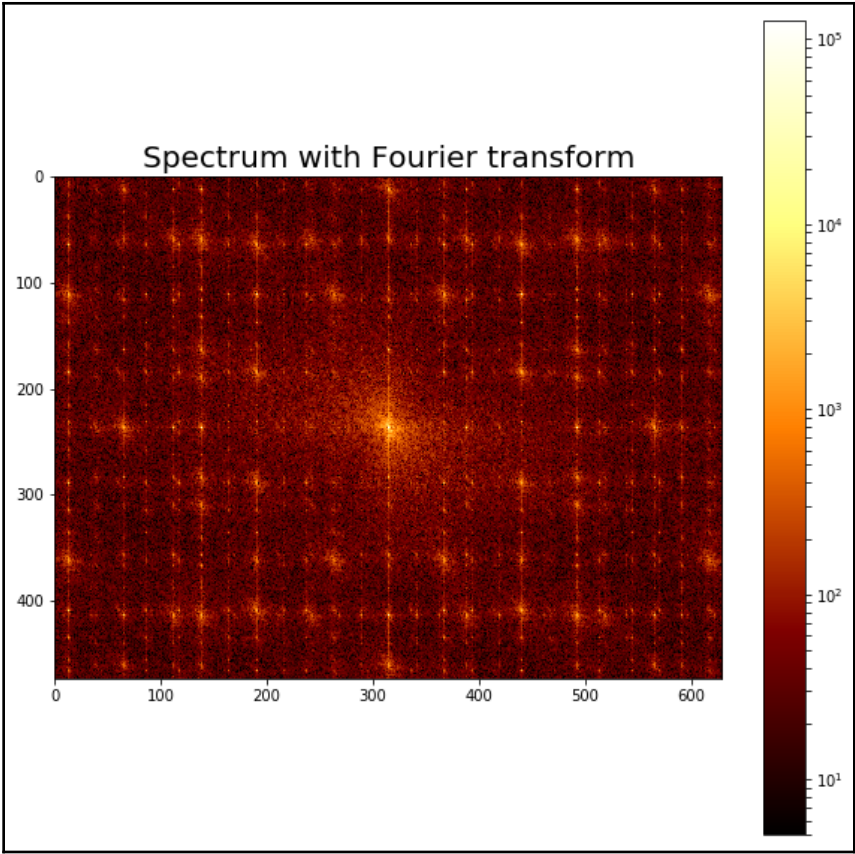


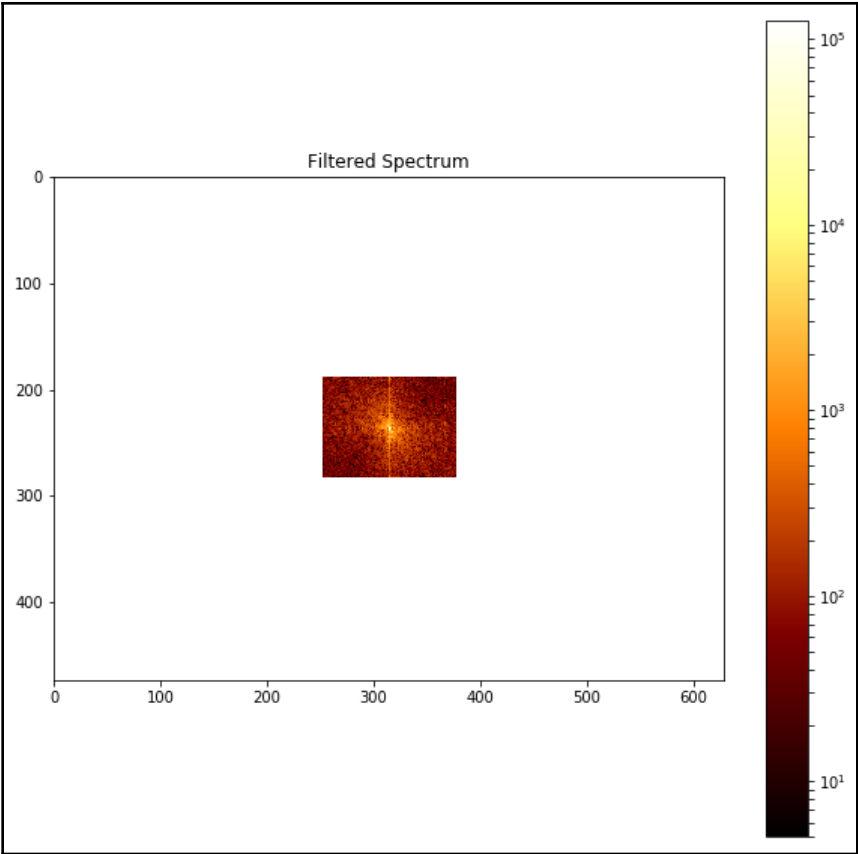
The frequency spectrum of the restored Lena image
(with inverse filter)







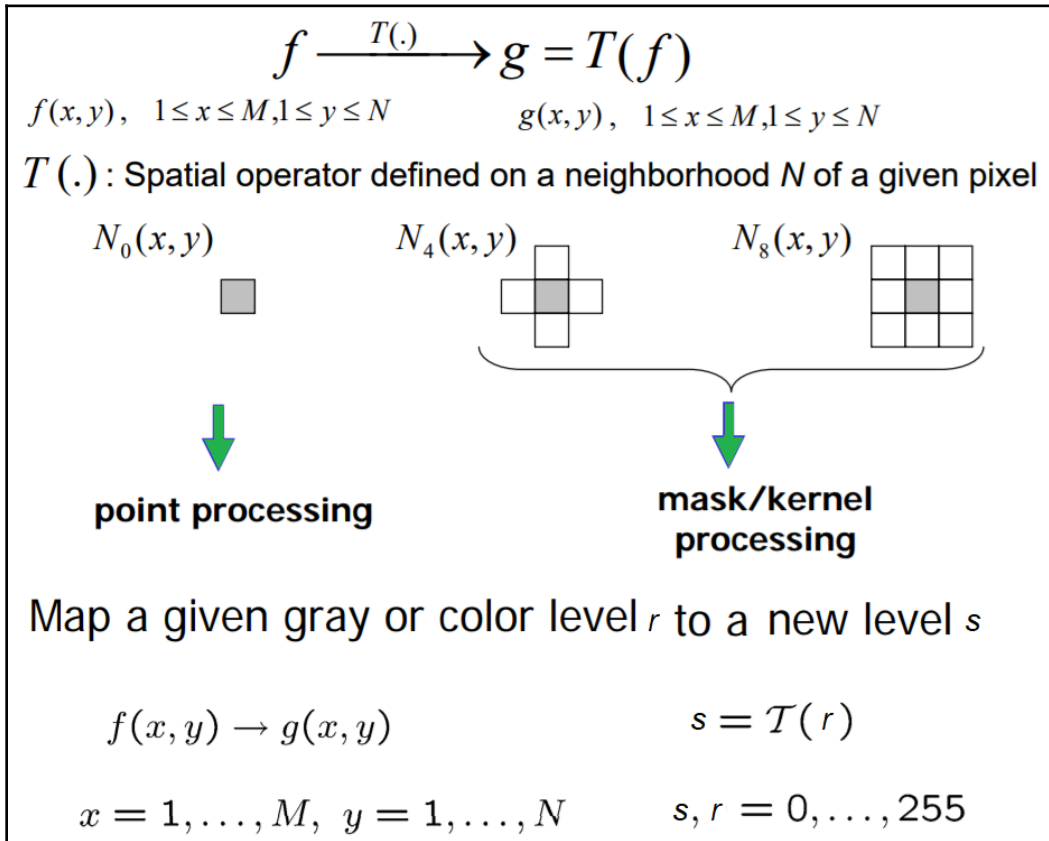




Reconstructed Image



Chapter 4: Image Enhancement



original image



histogram for RGB channels

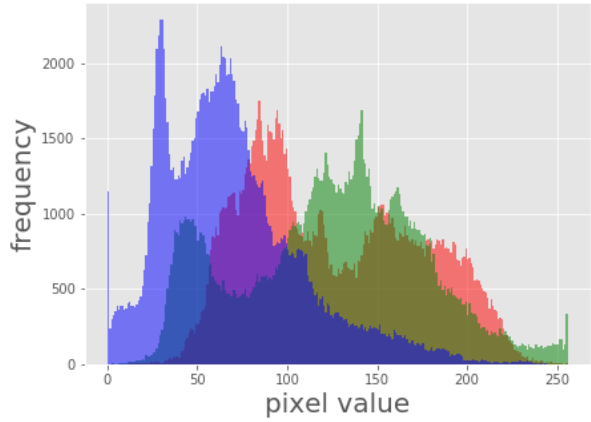
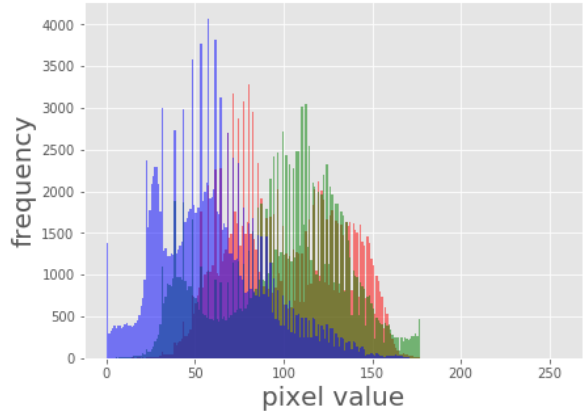


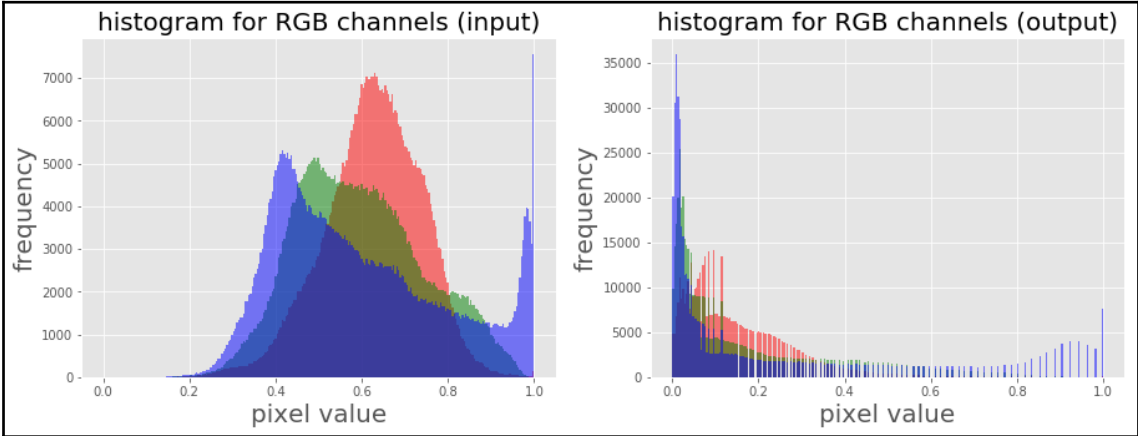
image after log transform



histogram of RGB channels log transform

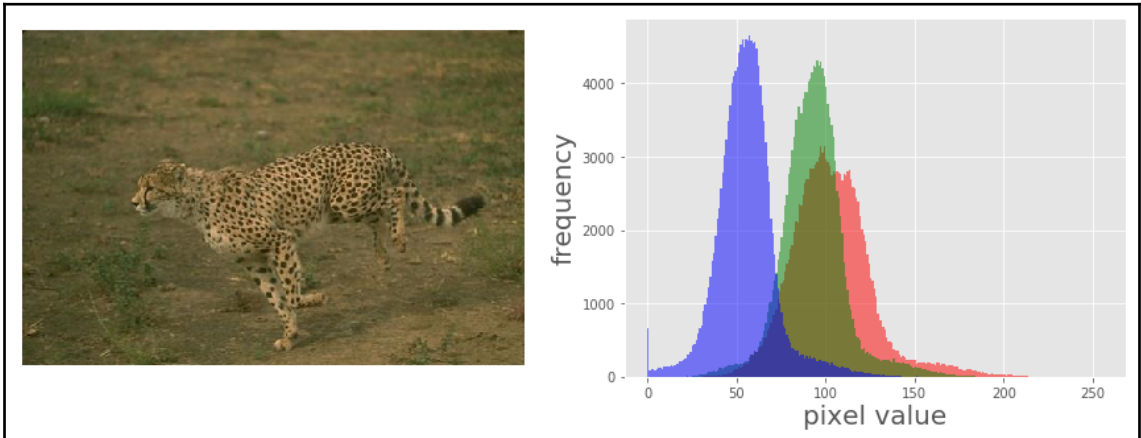
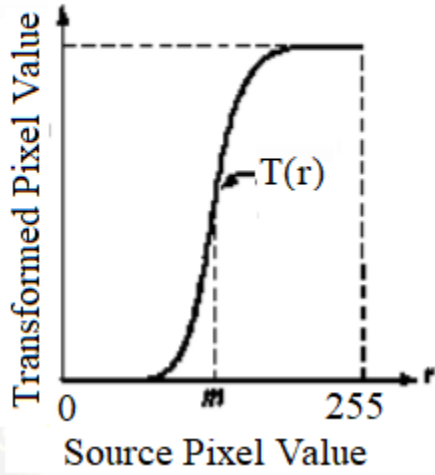


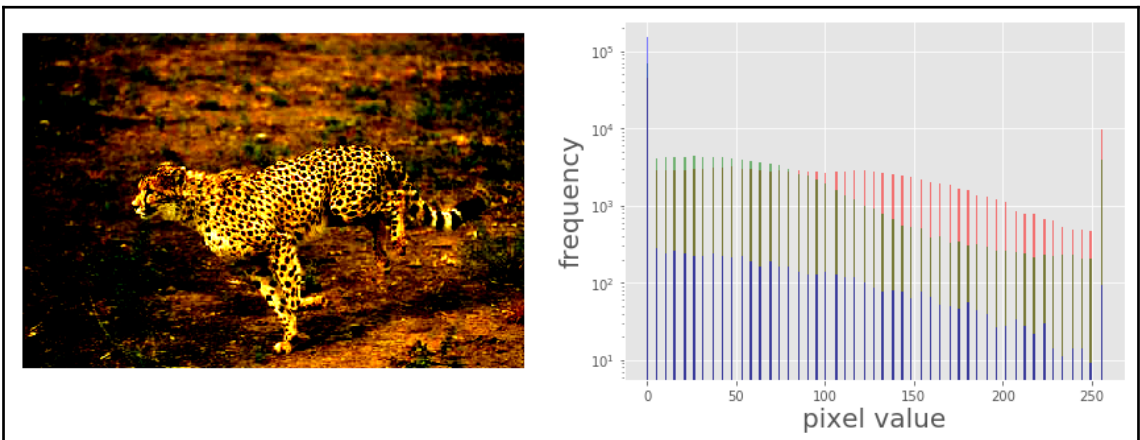
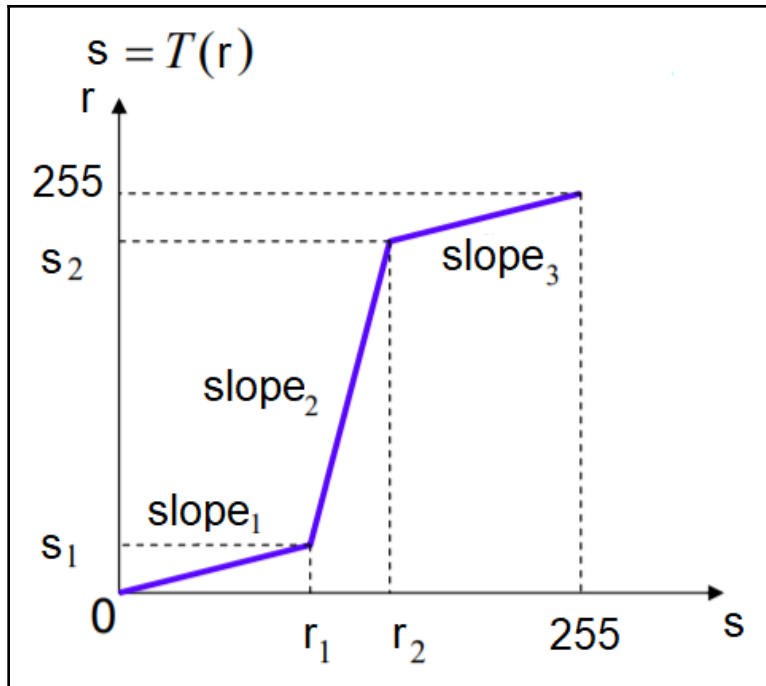


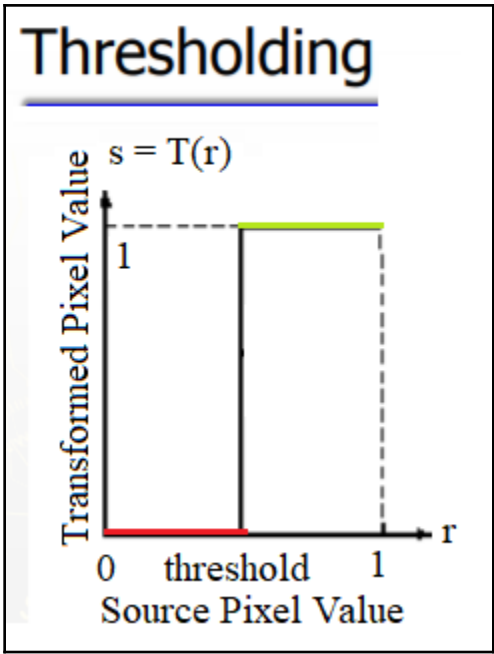
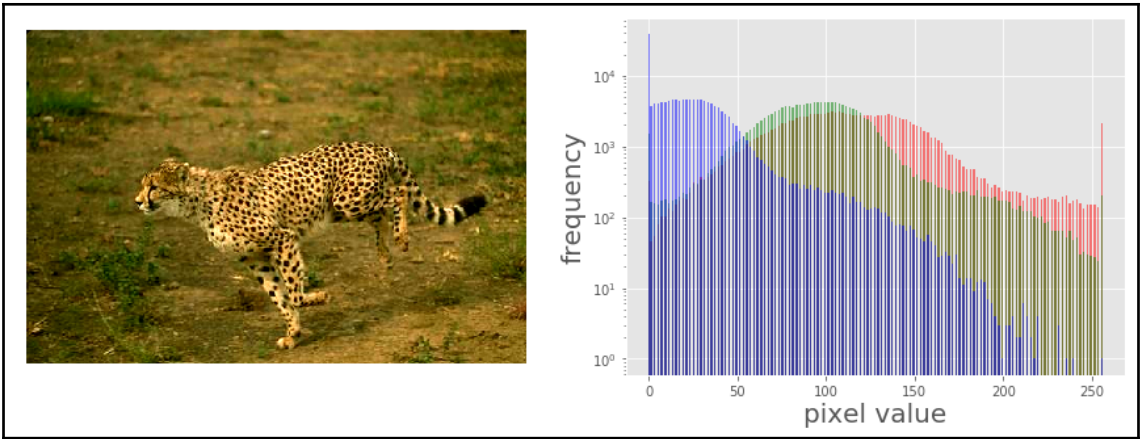


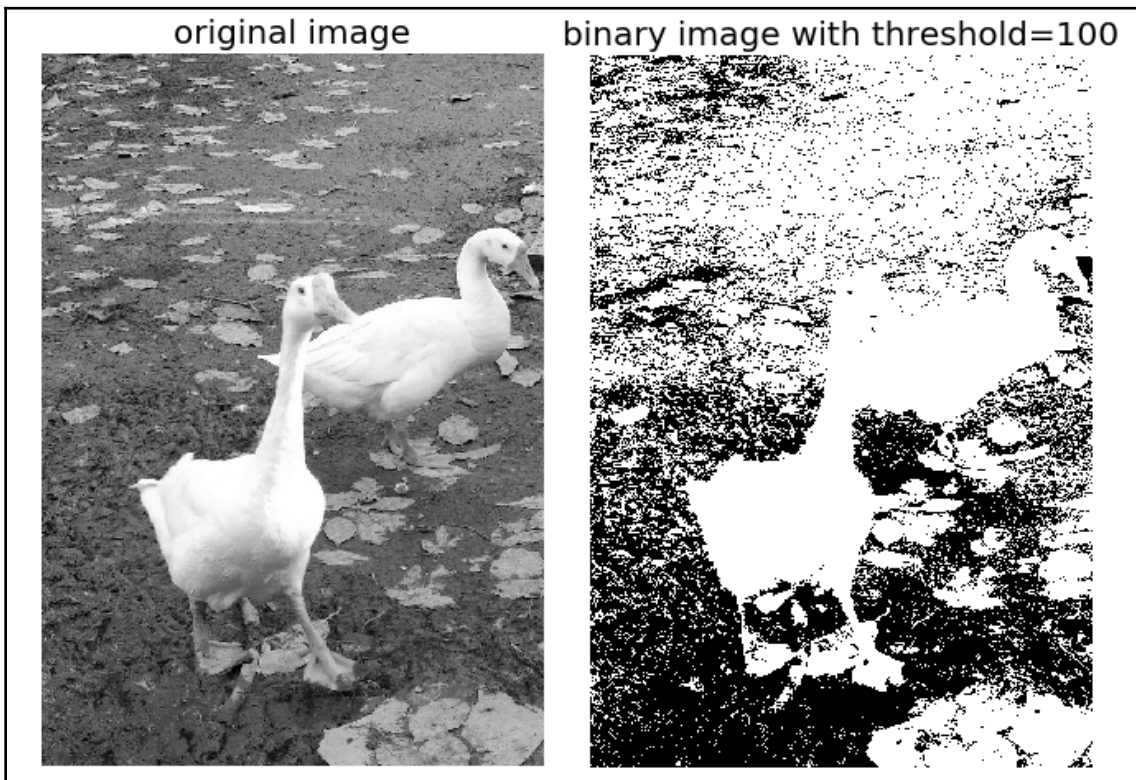
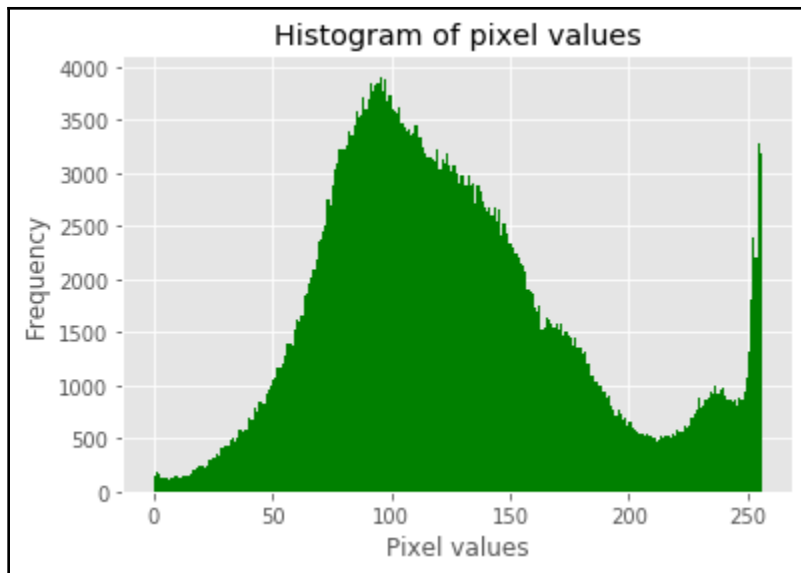
Contrast Stretching

$$s = T(r)$$



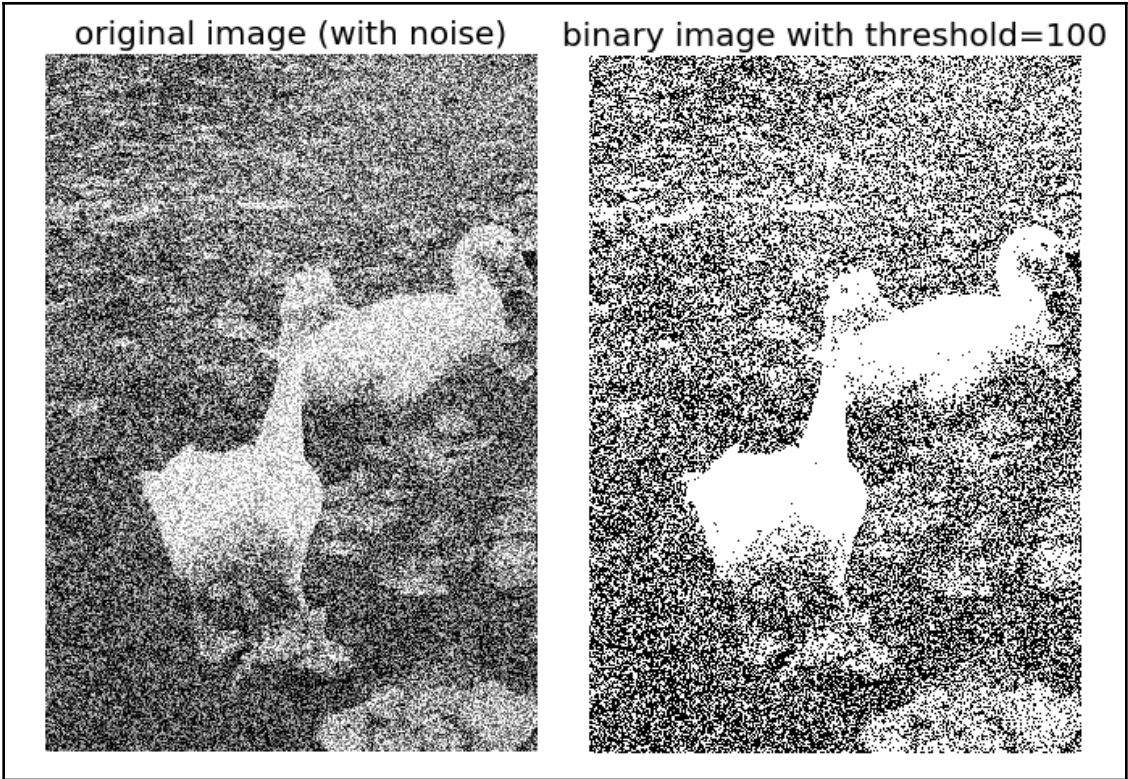






binary image with threshold=150 binary image with threshold=200



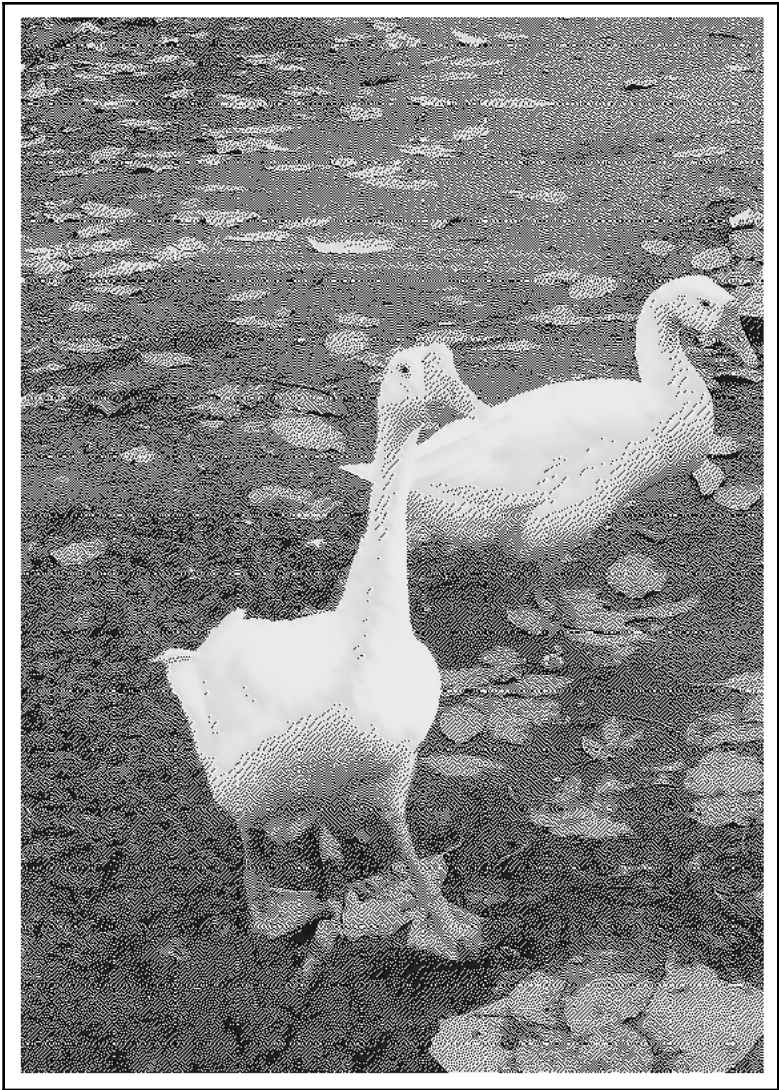


binary image with threshold=150 binary image with threshold=200



$$\begin{bmatrix} & & * & \frac{7}{16} & \dots \\ \dots & \frac{3}{16} & \frac{5}{16} & \frac{1}{16} & \dots \end{bmatrix}$$


```
for each y from top to bottom
  for each x from left to right
    oldpixel := pixel[x][y]
    newpixel := find_closest_palette_color(oldpixel)
    pixel[x][y] := newpixel
    quant_error := oldpixel - newpixel
    pixel[x + 1][y] := pixel[x + 1][y] + quant_error * 7 / 16
    pixel[x - 1][y + 1] := pixel[x - 1][y + 1] + quant_error * 3 / 16
    pixel[x][y + 1] := pixel[x][y + 1] + quant_error * 5 / 16
    pixel[x + 1][y + 1] := pixel[x + 1][y + 1] + quant_error * 1 / 16
```



$$s_k = T(r_k) = \sum_{j=0}^k P_r(r_j) = \sum_{j=0}^k n_j / N$$

$$0 \leq r_k \leq 1, \quad k = 0, 1, 2, \dots, 255$$

N: total number of pixels

n_j : frequency of pixel with gray-level j

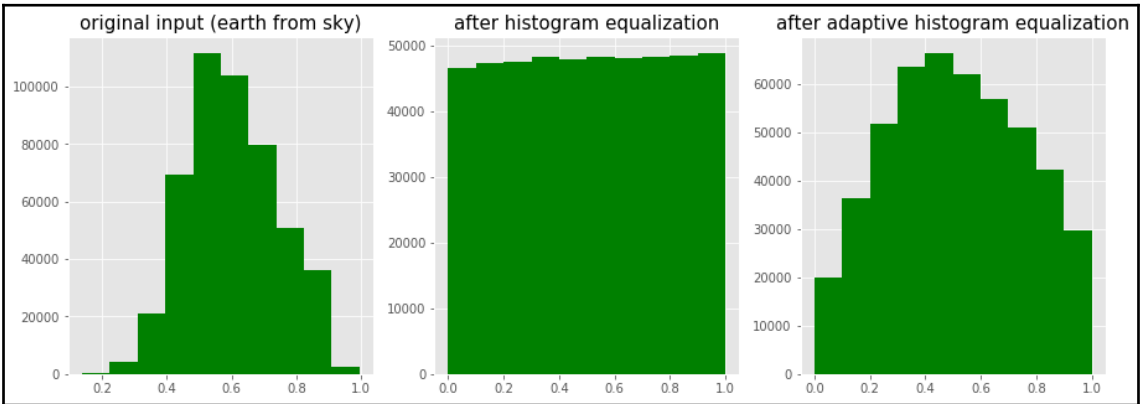
original input (earth from sky)

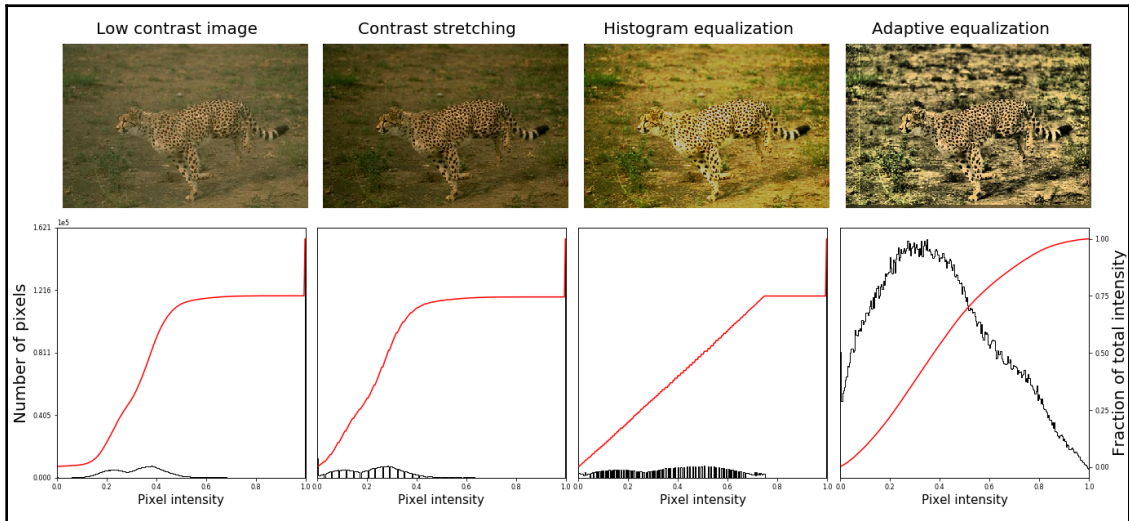
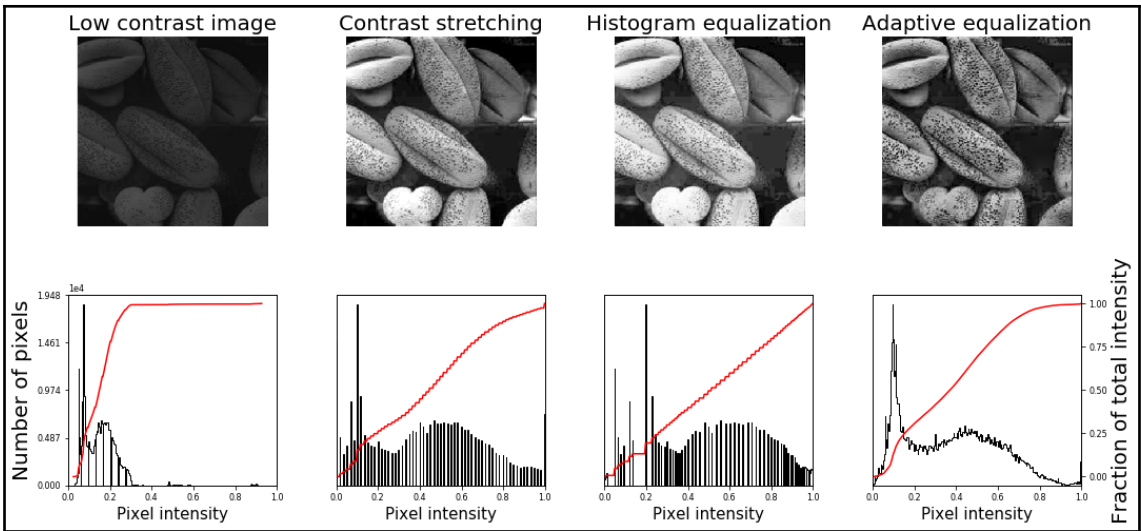


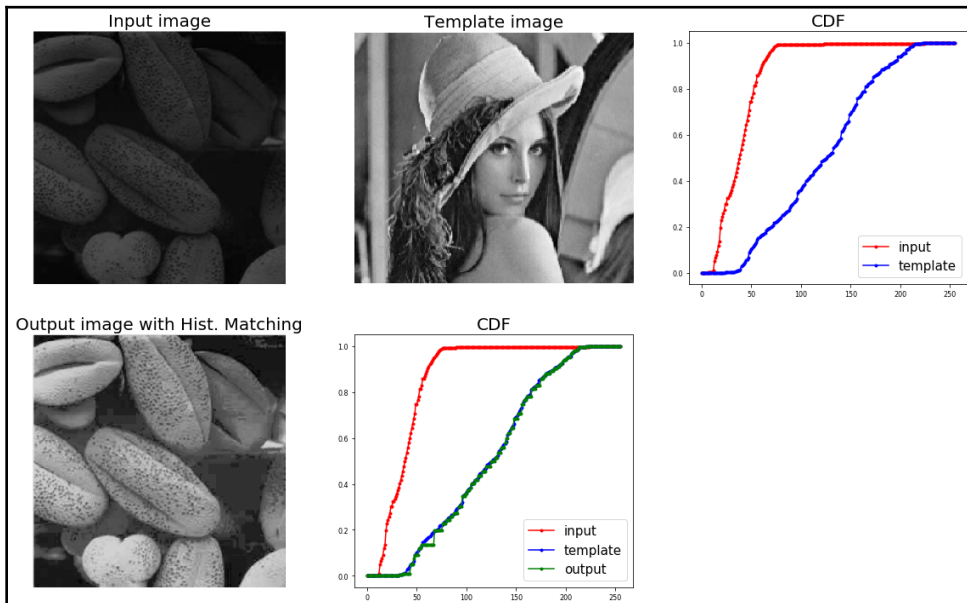
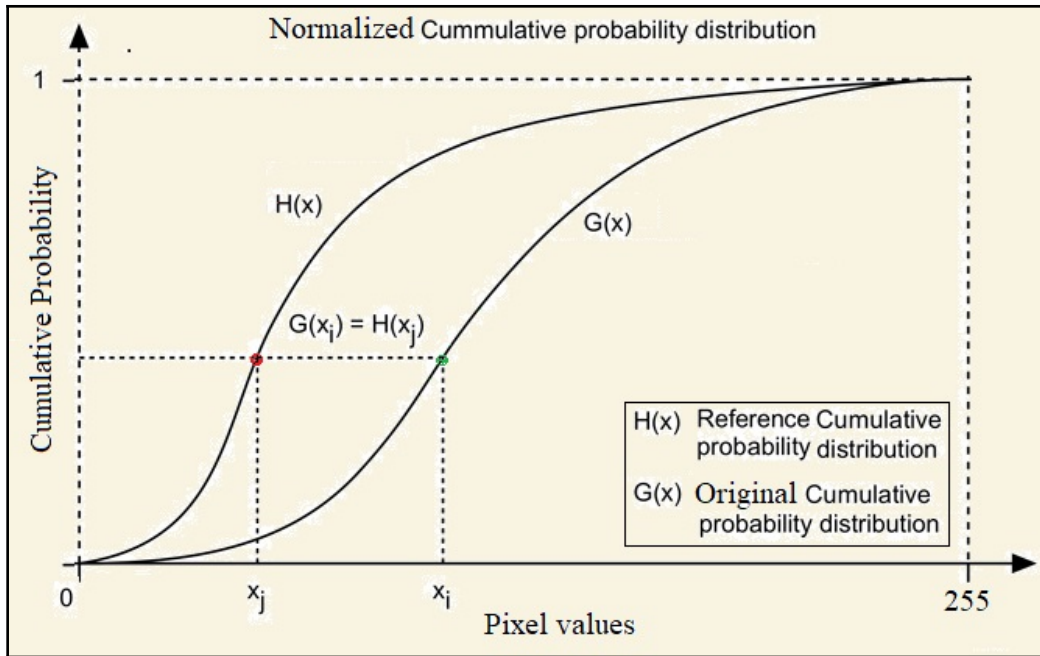
after histogram equalization



after adaptive histogram equalization



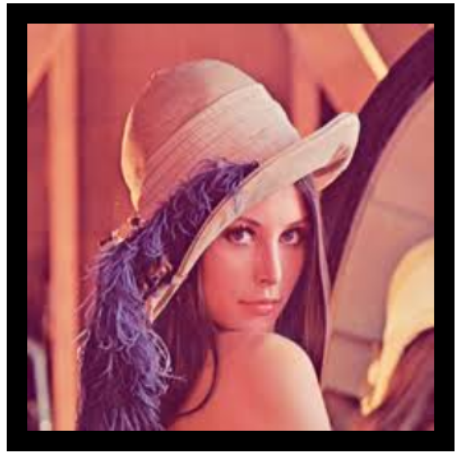


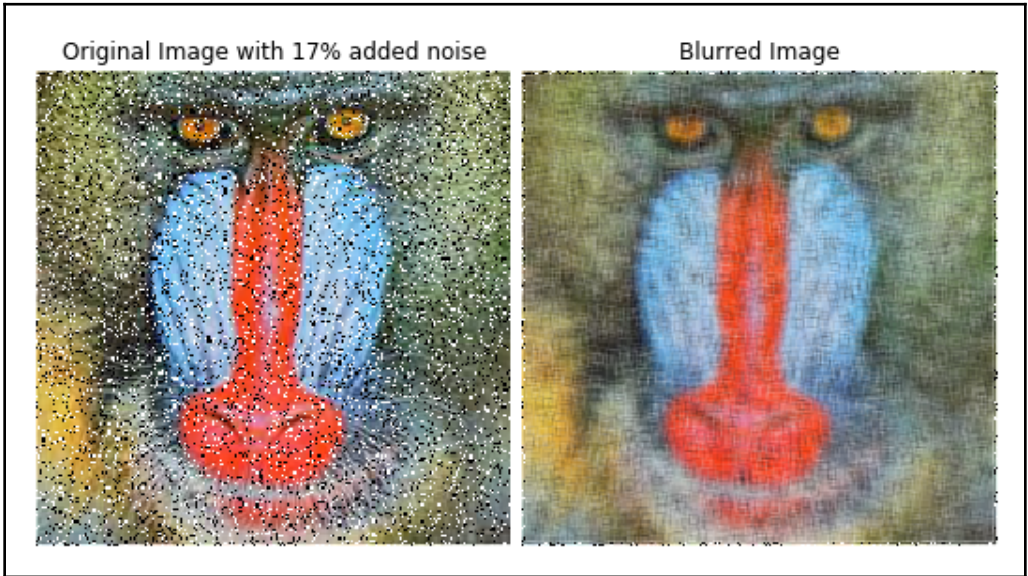
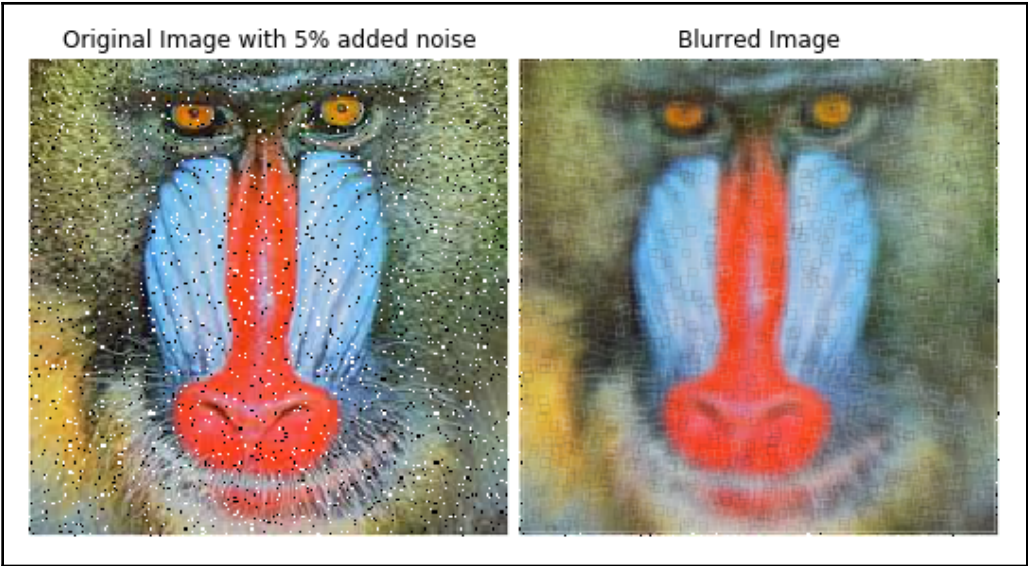


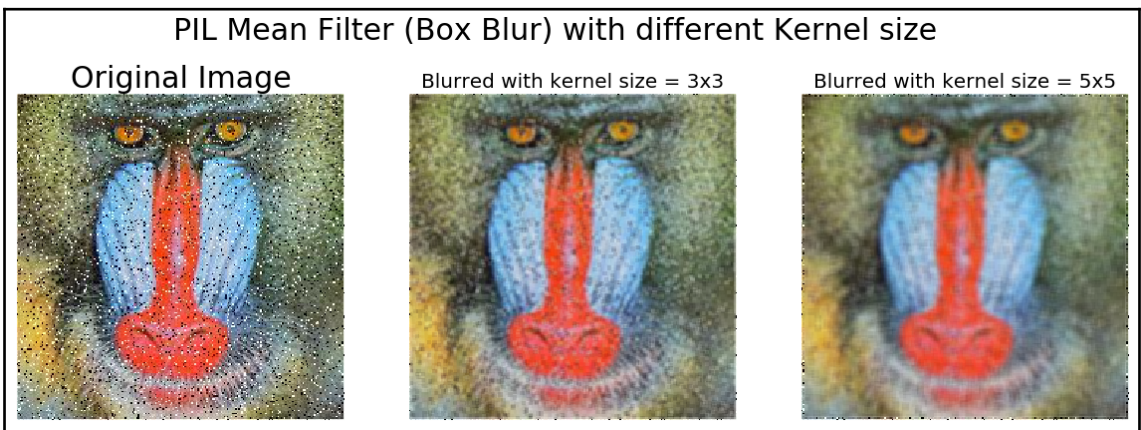
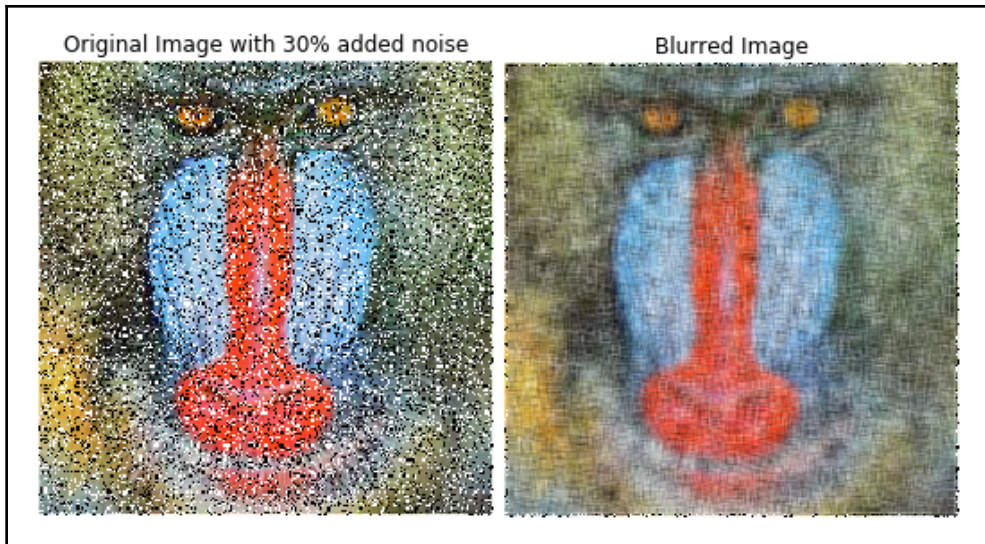
Input Image

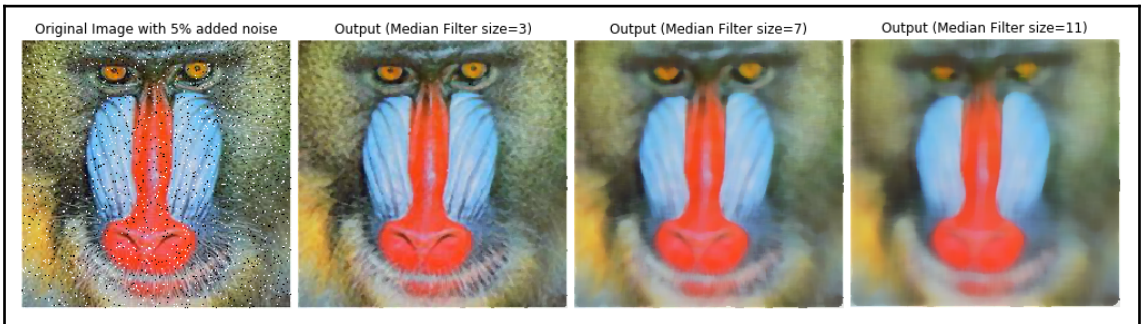
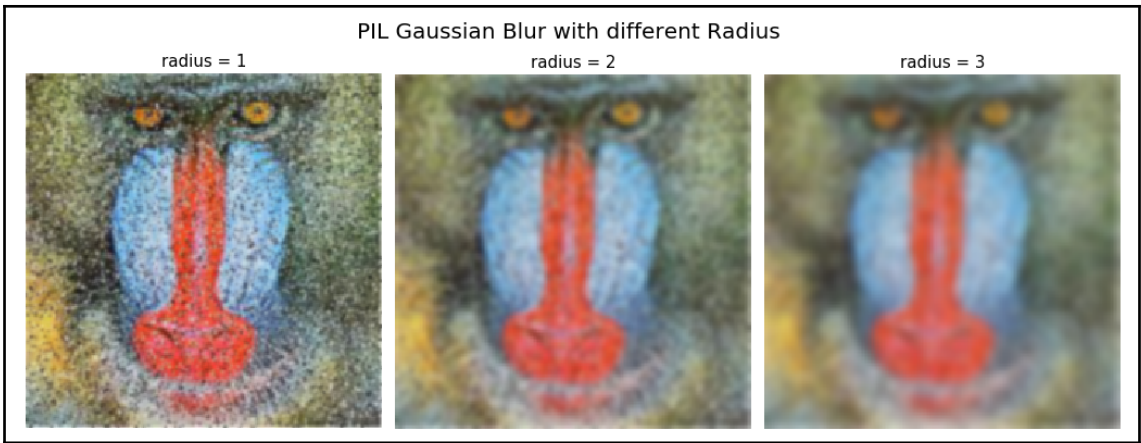


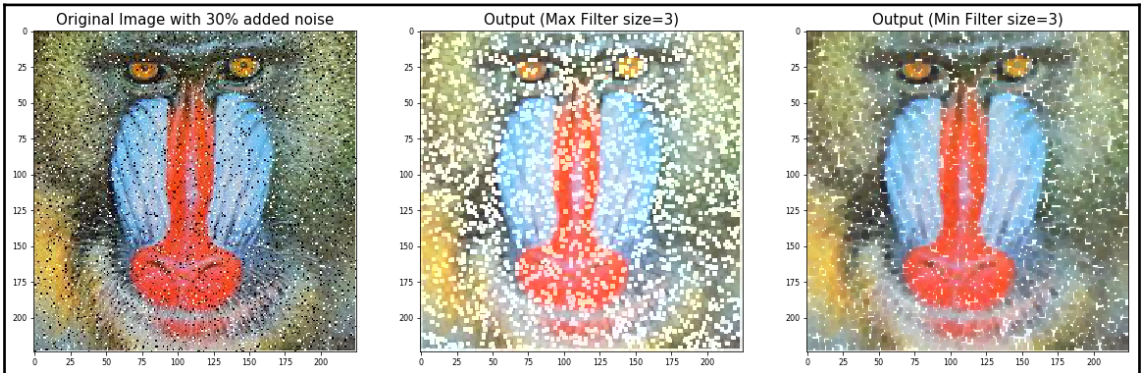
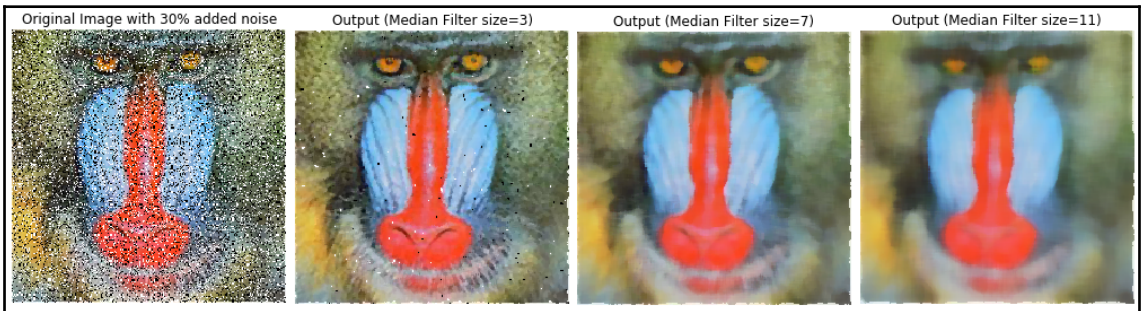
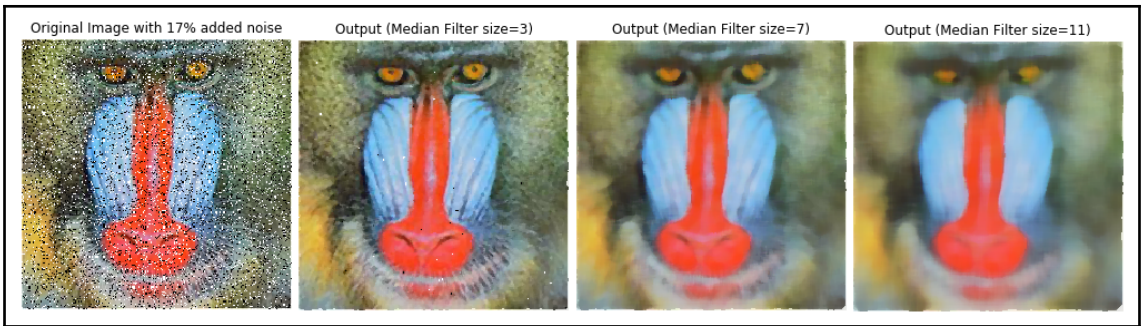
Template Image

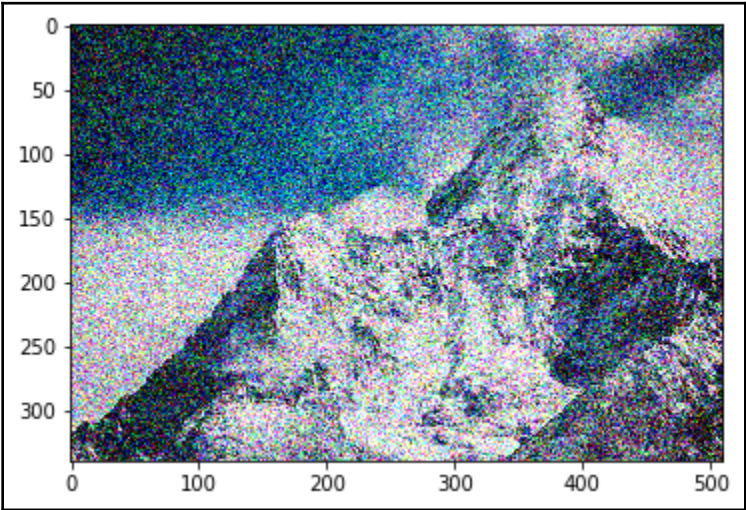


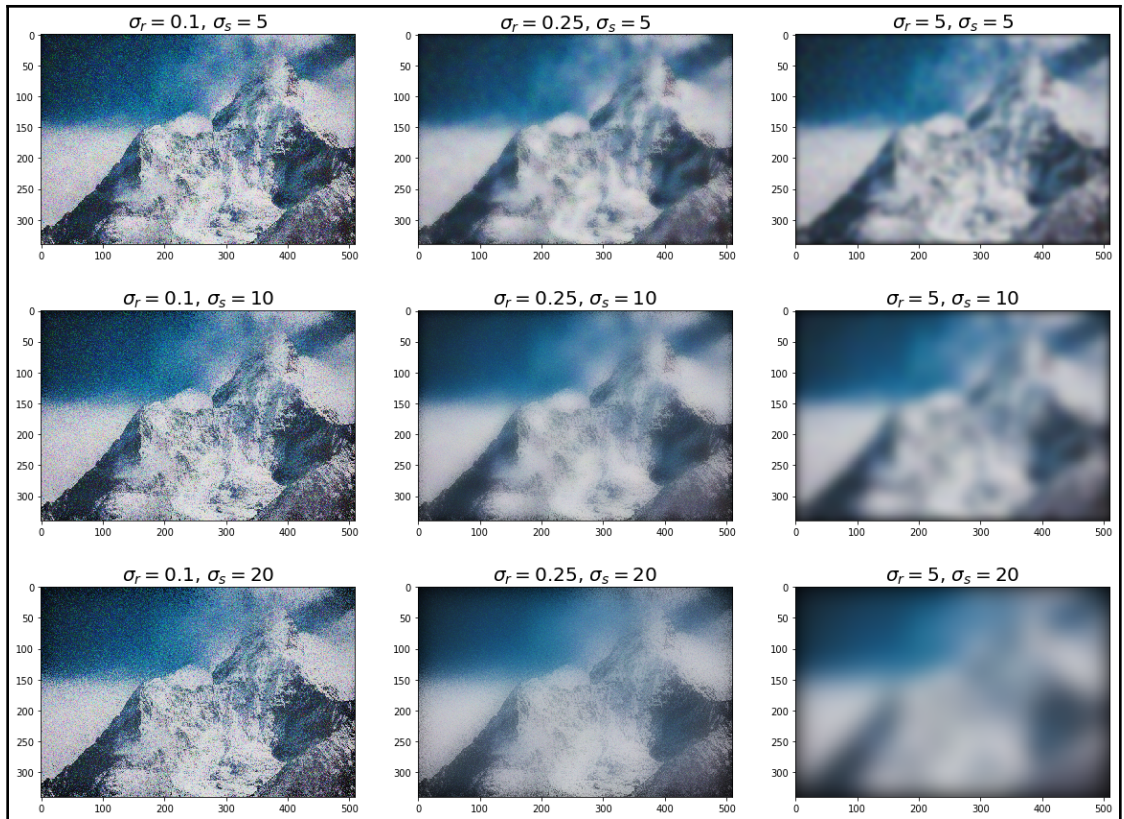


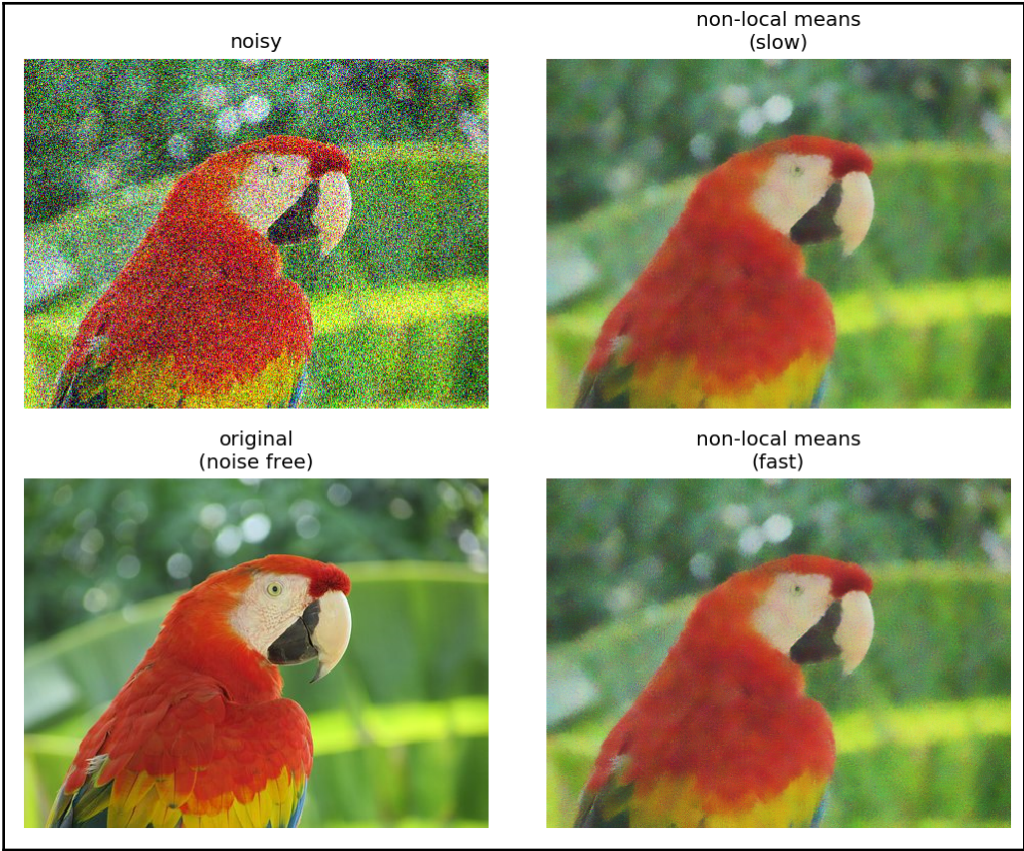


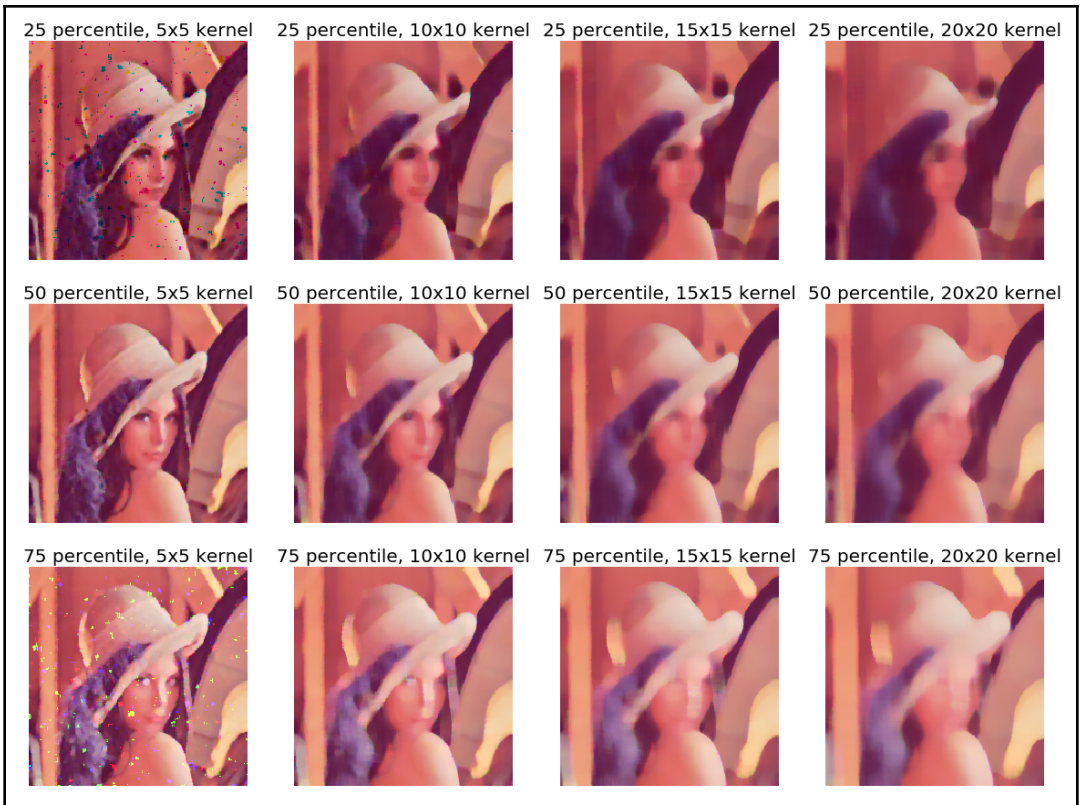






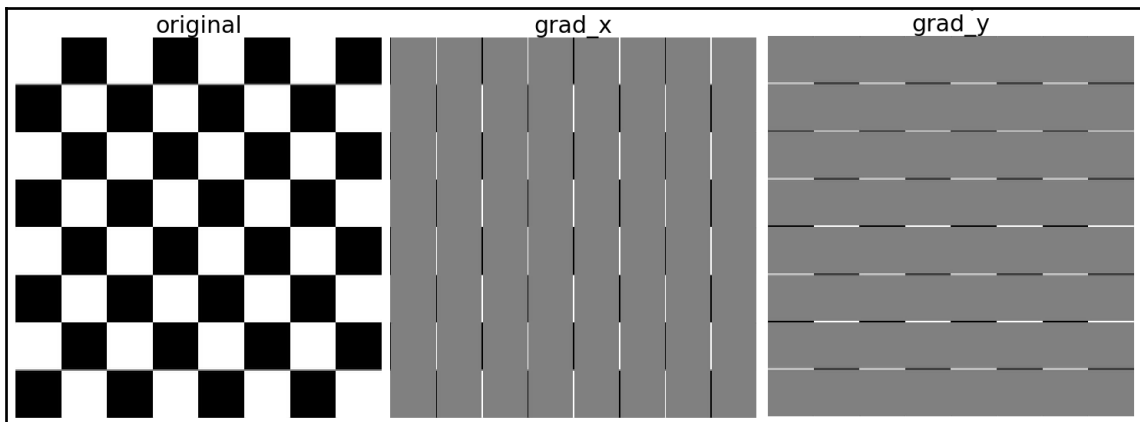


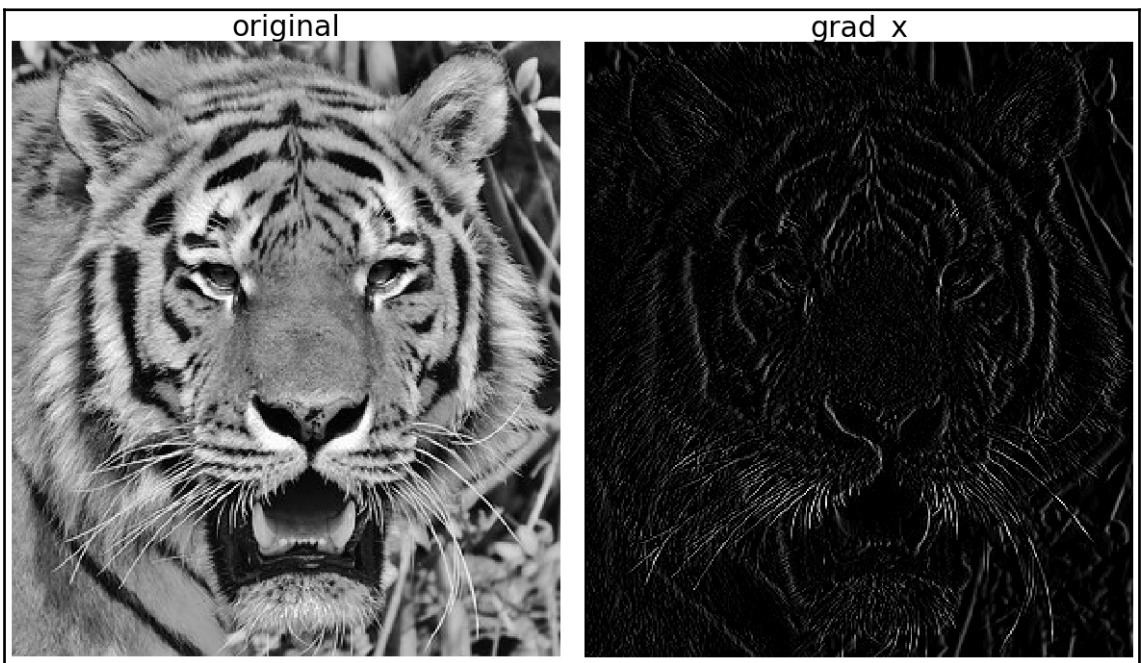
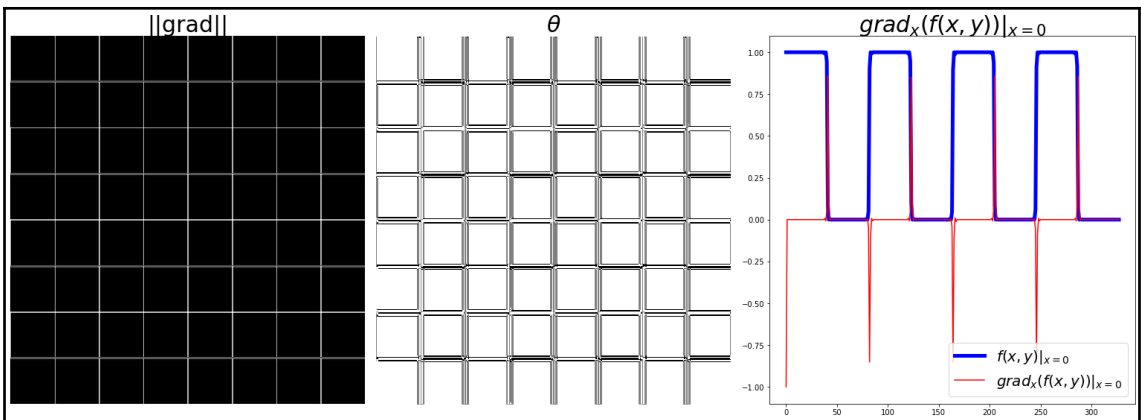


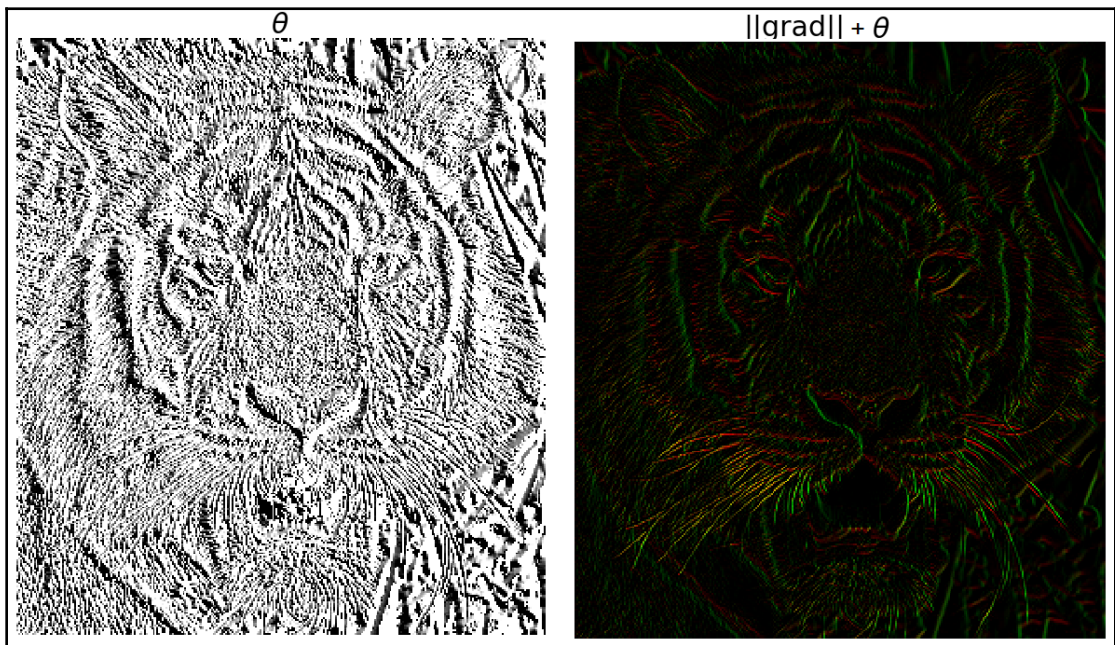
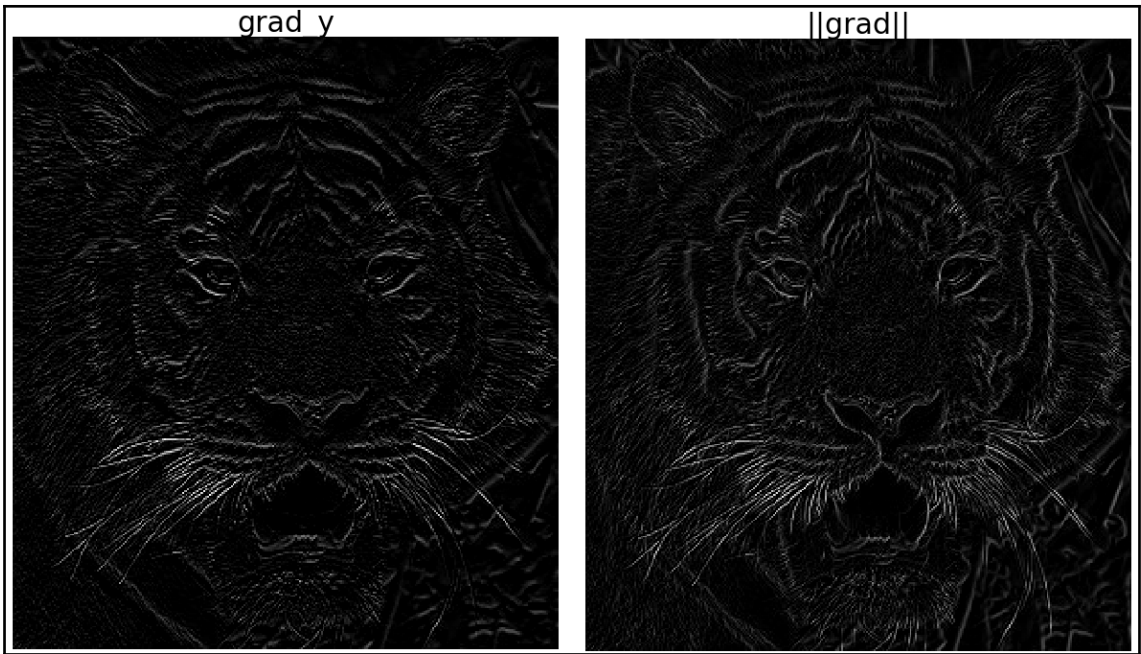


Chapter 5: Image Enhancement Using Derivatives

<div style="border: 1px solid red; padding: 2px; display: inline-block; margin-bottom: 5px;">1st order derivatives</div> <p>forward difference</p> $\frac{\partial f}{\partial x} = f(x+1) - f(x)$ $\frac{\partial f}{\partial y} = f(y+1) - f(y)$ <p>central difference</p> $\frac{\partial f}{\partial x} = \frac{f(x+1) - f(x-1)}{2}$	<p>Convolution Kernels</p>	<div style="border: 1px solid blue; padding: 2px; display: inline-block; margin-bottom: 5px;">Gradient</div> $\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$ <p>magnitude $\ \nabla f\ = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$</p> <p>direction $\theta = \tan^{-1} \left(\frac{\partial f}{\partial y} / \frac{\partial f}{\partial x} \right)$</p>
<div style="display: flex; justify-content: space-around; align-items: center;"> <div style="border: 1px solid gray; padding: 2px; margin: 2px;">-1 1</div> <div style="border: 1px solid gray; padding: 2px; margin: 2px;">-1 1</div> <div style="border: 1px solid gray; padding: 2px; margin: 2px;">-1 0 1</div> </div>		





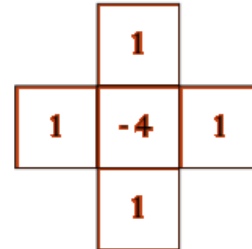


2nd order derivative

$$\frac{\partial^2 f}{\partial x^2} = f(x+1) + f(x-1) - 2f(x)$$

$$\frac{\partial^2 f}{\partial y^2} = f(y+1) + f(y-1) - 2f(y)$$

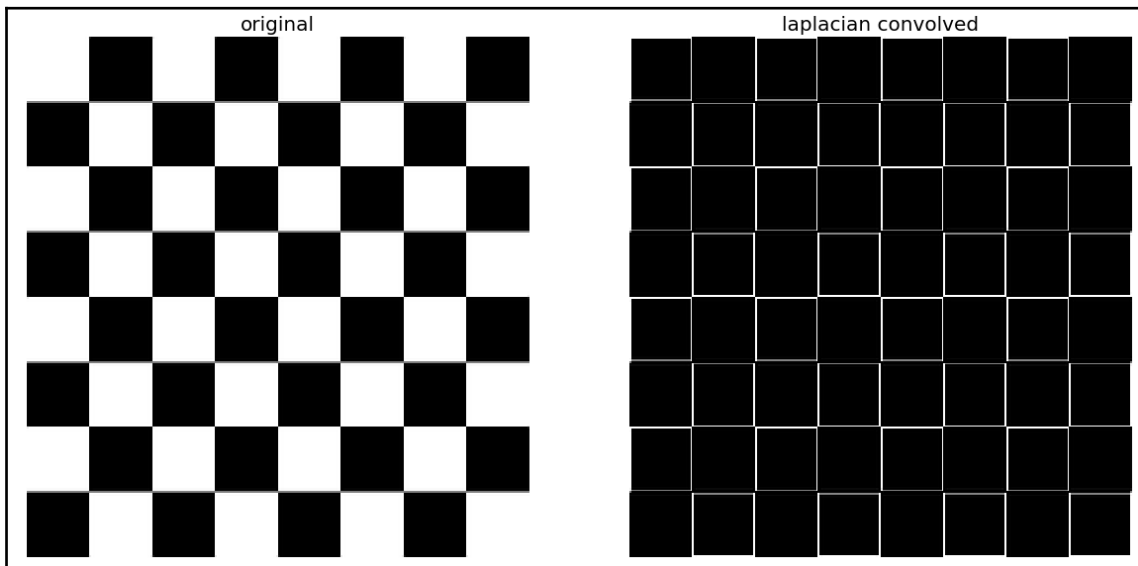
Convolution Kernel

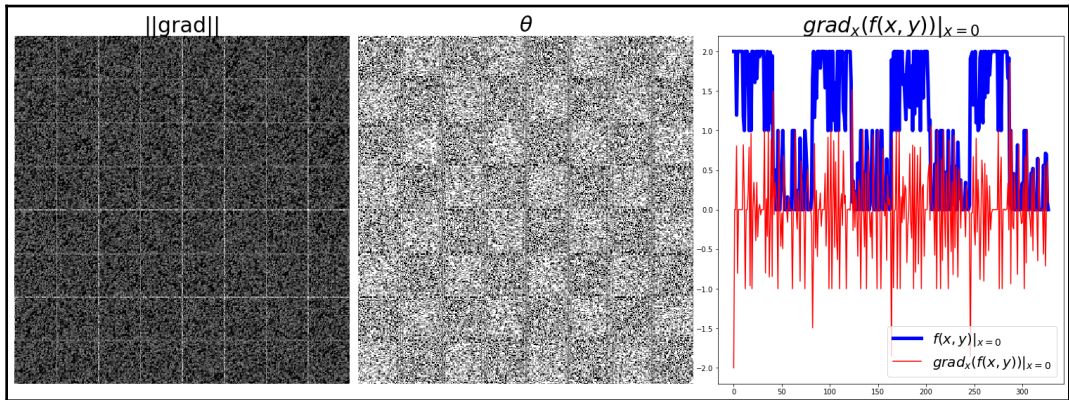
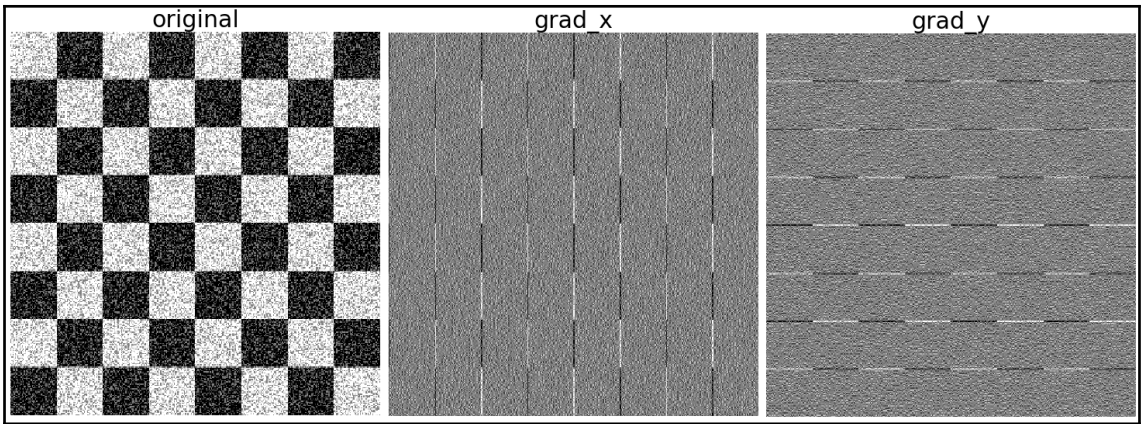


Laplacian

$$\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

$$= f(x+1, y) + f(x-1, y) + f(x, y+1) + f(x, y-1) - 4f(x, y)$$





original image

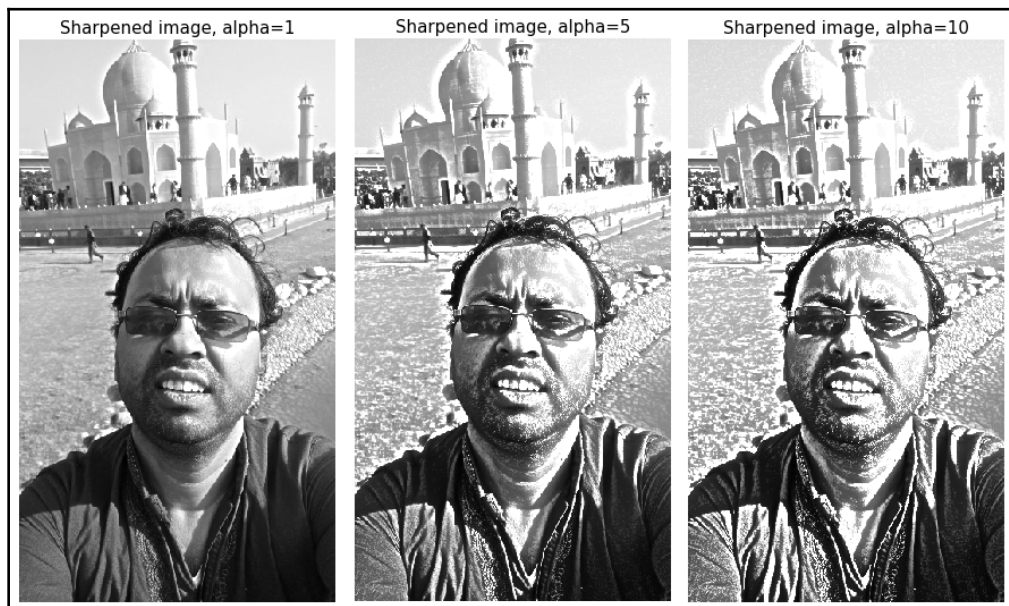


sharpened image



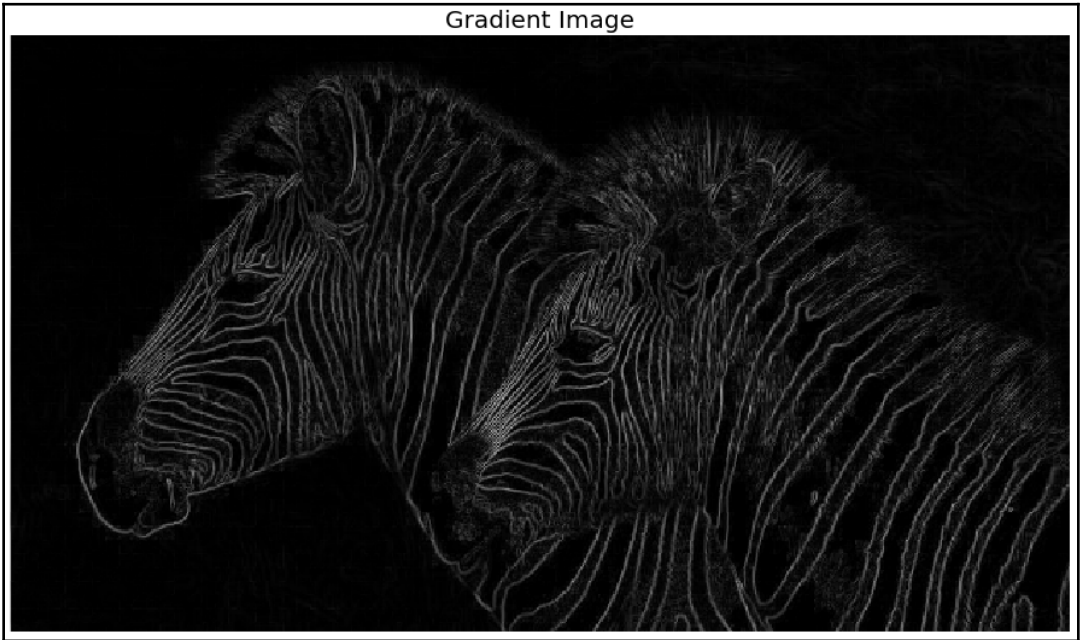
*Original Image - Smoothed Image = Detail Image
(with Gaussian Filter)*

Original Image + α .(Detail Image) = Sharpened Image





Gradient Image



After Non-Maximum suppression



edge direction	pixels to compare
horizontal	top and bottom
vertical	left and right
north west or south east	top right and bottom left
north east or south west	bottom right and top left

$\frac{1}{8}$	-1	0	1	$\frac{1}{8}$	1	2	1
	-2	0	2		0	0	0
	-1	0	1		-1	-2	-1

S_x S_y

1	0	-1	=	1	x	1	0	-1
2	0	-2		2		x-derivative		
1	0	-1		1				

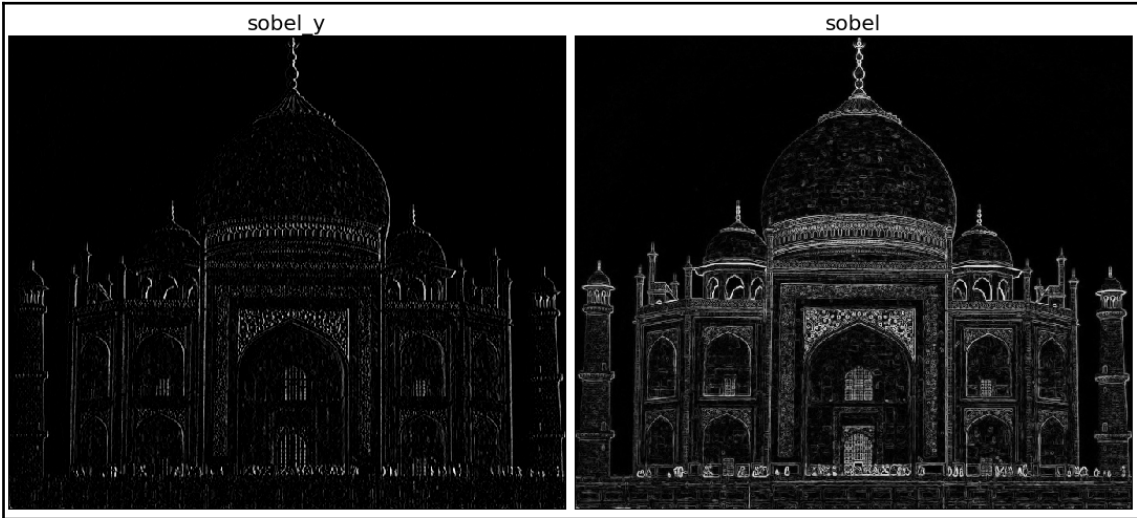
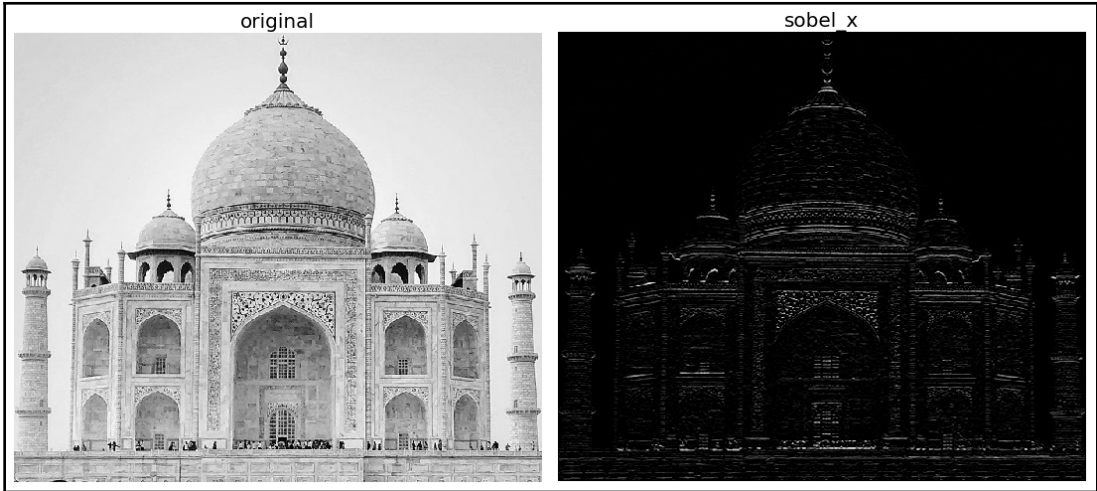
Sobel weighted average and scaling

Run filter over image

$$\frac{\partial f}{\partial x} = S_x \otimes f \qquad \frac{\partial f}{\partial y} = S_y \otimes f$$

Image gradient

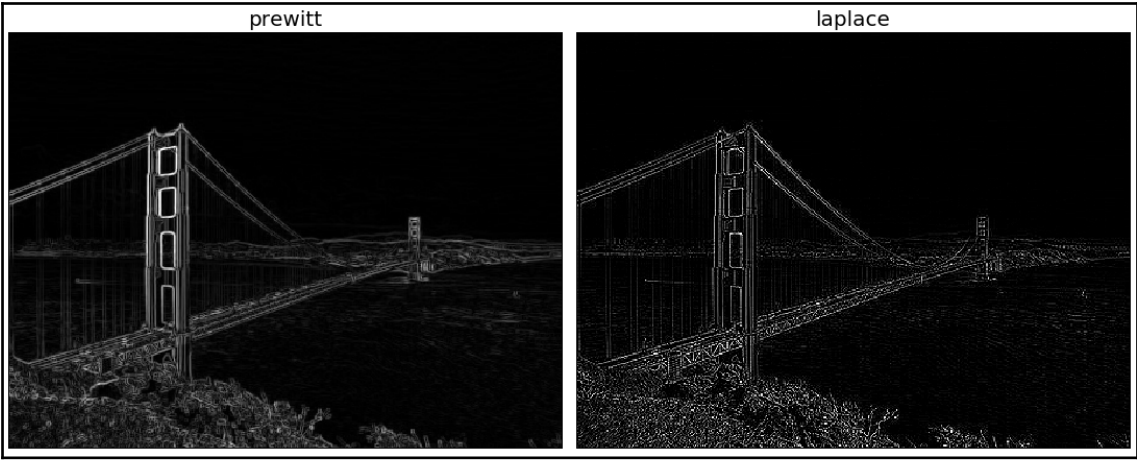
$$\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$$

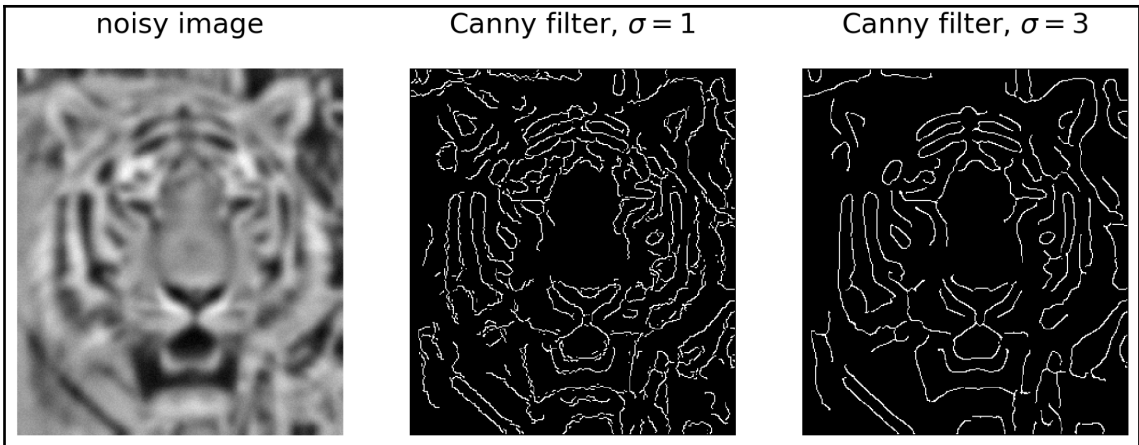


Derivative Filters

1st Order	Sobel	x	y	Scharr	x	y									
		1 0 -1	1 2 1		3 0 -3	3 10 3									
		2 0 -2	0 0 0		10 0 -10	0 0 0									
		1 0 -1	-1 -2 -1		3 0 -3	-3 -10 -3									
2nd Order	Prewitt	1 0 -1	1 1 1	Roberts	0 1	1 0									
		1 0 -1	0 0 0		-1 0	0 -1									
		1 0 -1	-1 -1 -1												
	Laplace	<table style="margin: auto; border-collapse: collapse;"> <tr><td style="padding: 2px 10px;">0</td><td style="padding: 2px 10px;">-1</td><td style="padding: 2px 10px;">0</td></tr> <tr><td style="padding: 2px 10px;">-1</td><td style="padding: 2px 10px;">4</td><td style="padding: 2px 10px;">-1</td></tr> <tr><td style="padding: 2px 10px;">0</td><td style="padding: 2px 10px;">-1</td><td style="padding: 2px 10px;">0</td></tr> </table>			0	-1	0	-1	4	-1	0	-1	0		
0	-1	0													
-1	4	-1													
0	-1	0													







LoG

$$G_{\sigma}(x, y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$



$$\frac{\partial^2 G_{\sigma}(x, y)}{\partial x^2} = \frac{1}{2\pi\sigma^4} e^{-\frac{x^2+y^2}{2\sigma^2}} \left(\frac{x^2}{\sigma^2} - 1 \right)$$

$$\frac{\partial^2 G_{\sigma}(x, y)}{\partial y^2} = \frac{1}{2\pi\sigma^4} e^{-\frac{x^2+y^2}{2\sigma^2}} \left(\frac{y^2}{\sigma^2} - 1 \right)$$



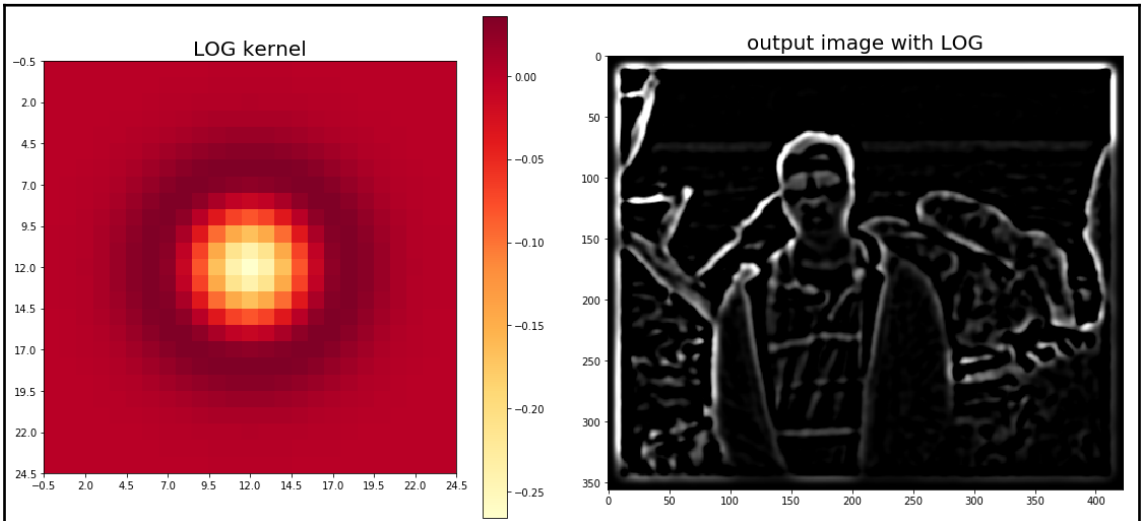
$$\begin{aligned} \text{LoG}(x, y) = \nabla^2 G_{\sigma}(x, y) &= \frac{\partial^2 G_{\sigma}(x, y)}{\partial x^2} + \frac{\partial^2 G_{\sigma}(x, y)}{\partial y^2} \\ &= -\frac{1}{\pi\sigma^4} e^{-\frac{x^2+y^2}{2\sigma^2}} \left(1 - \frac{x^2 + y^2}{2\sigma^2} \right) \end{aligned}$$

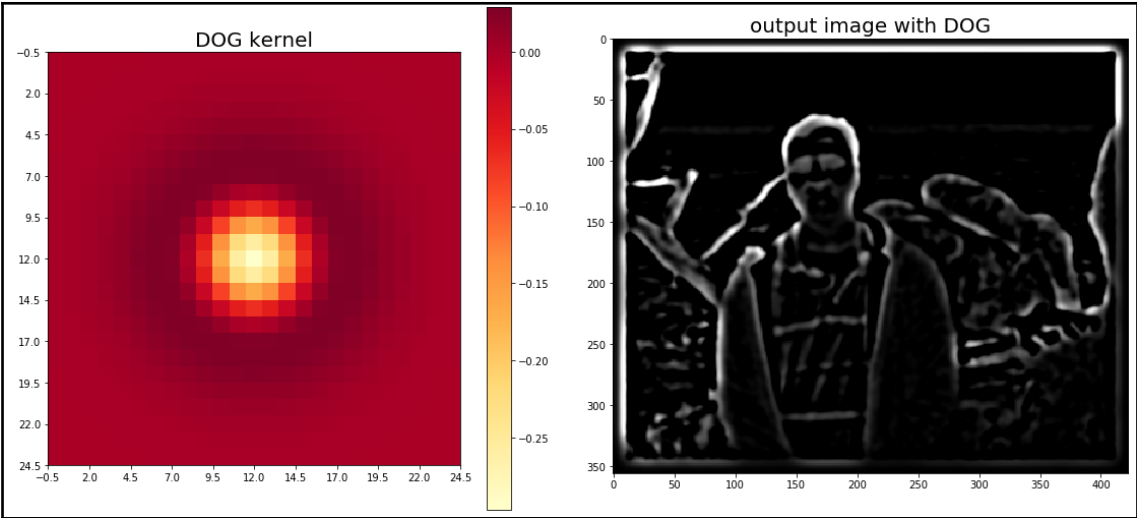
Approximation with DoG

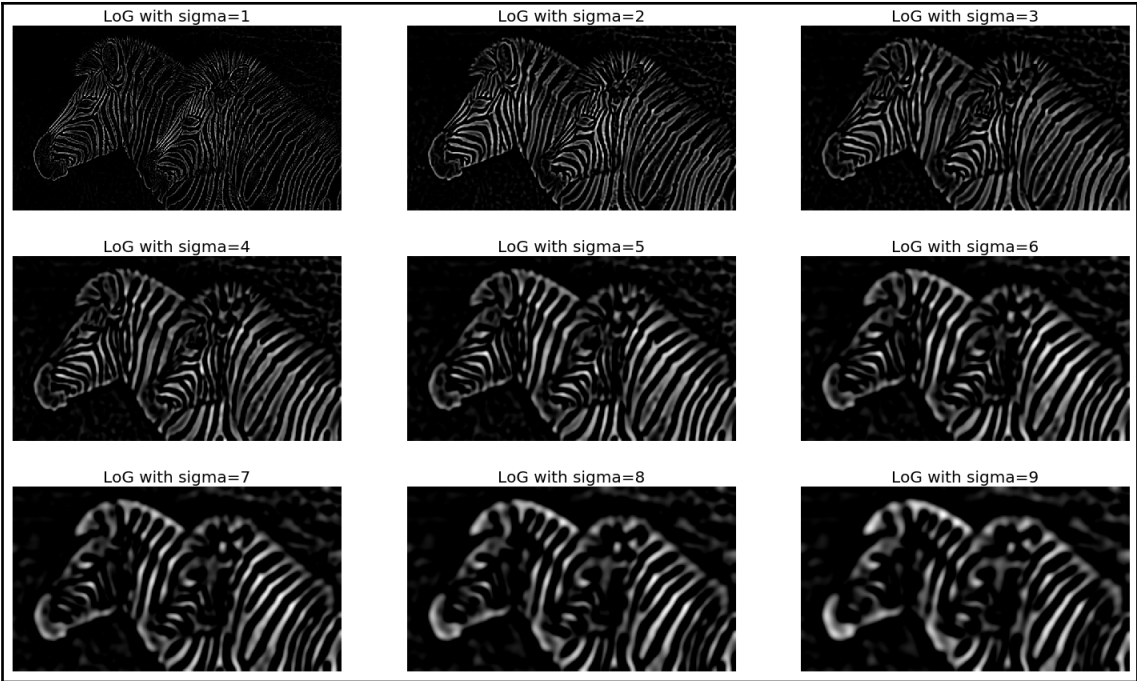
$$\nabla^2 G_{\sigma} \approx G_{\sigma_1} - G_{\sigma_2}$$

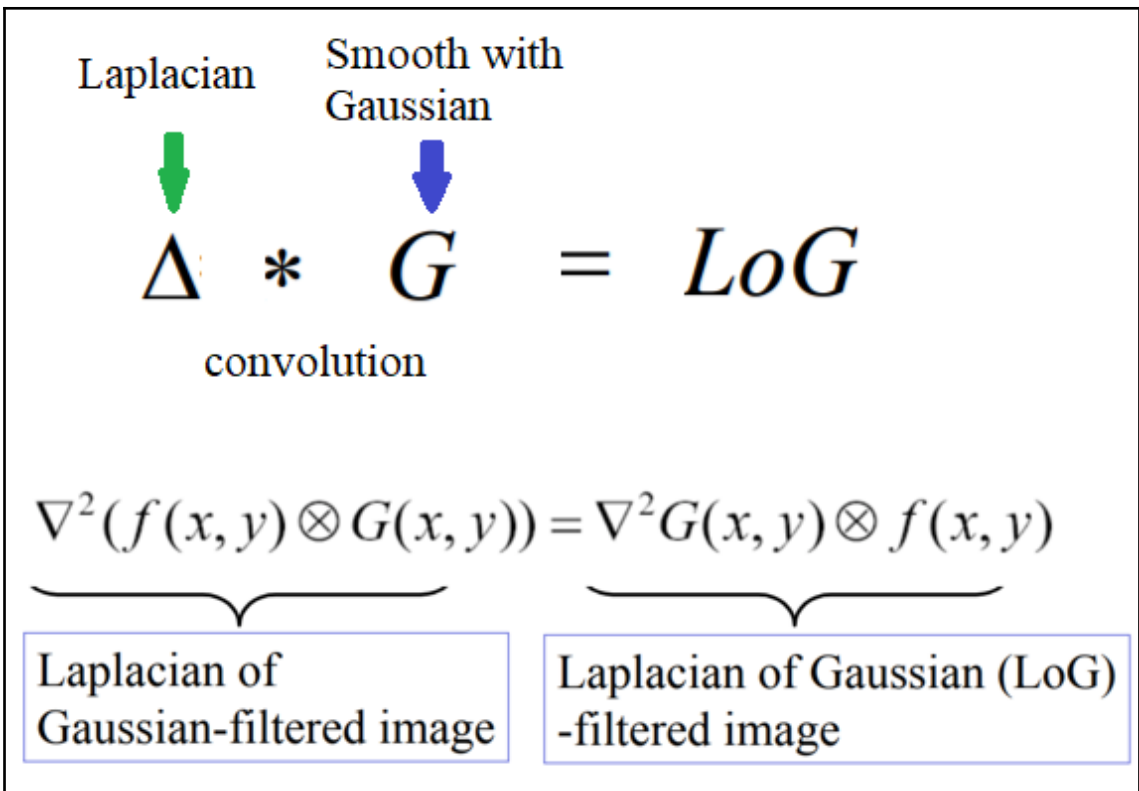
Best approximation with

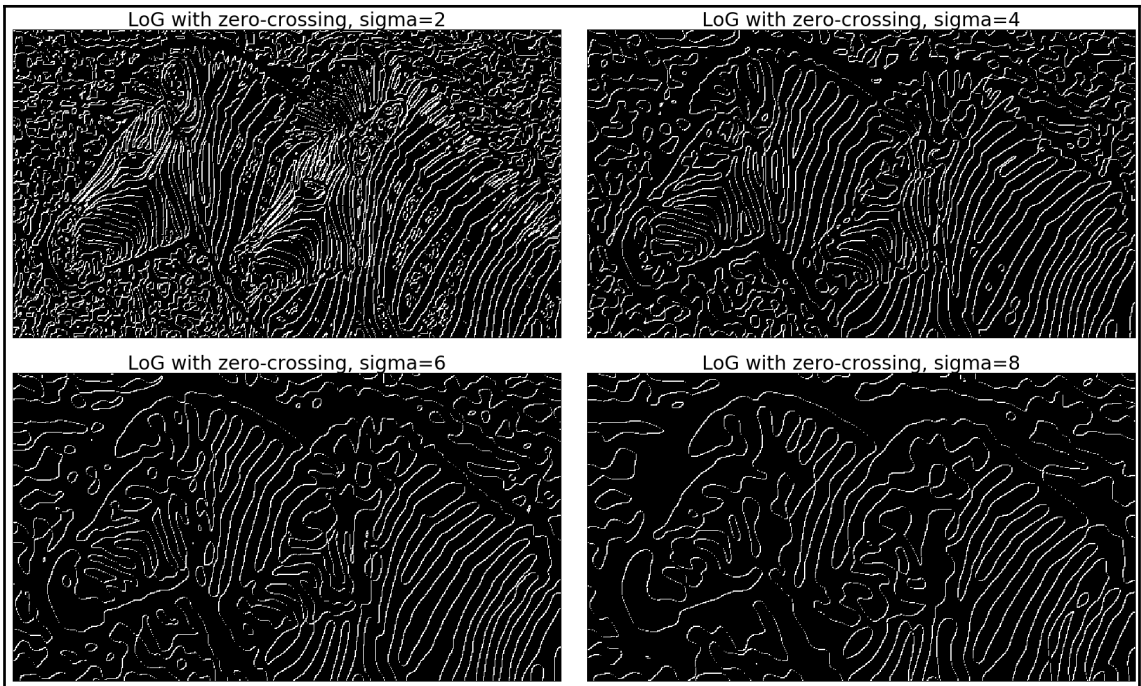
$$\sigma_1 = \sqrt{2}\sigma, \sigma_2 = \frac{\sigma}{\sqrt{2}}$$

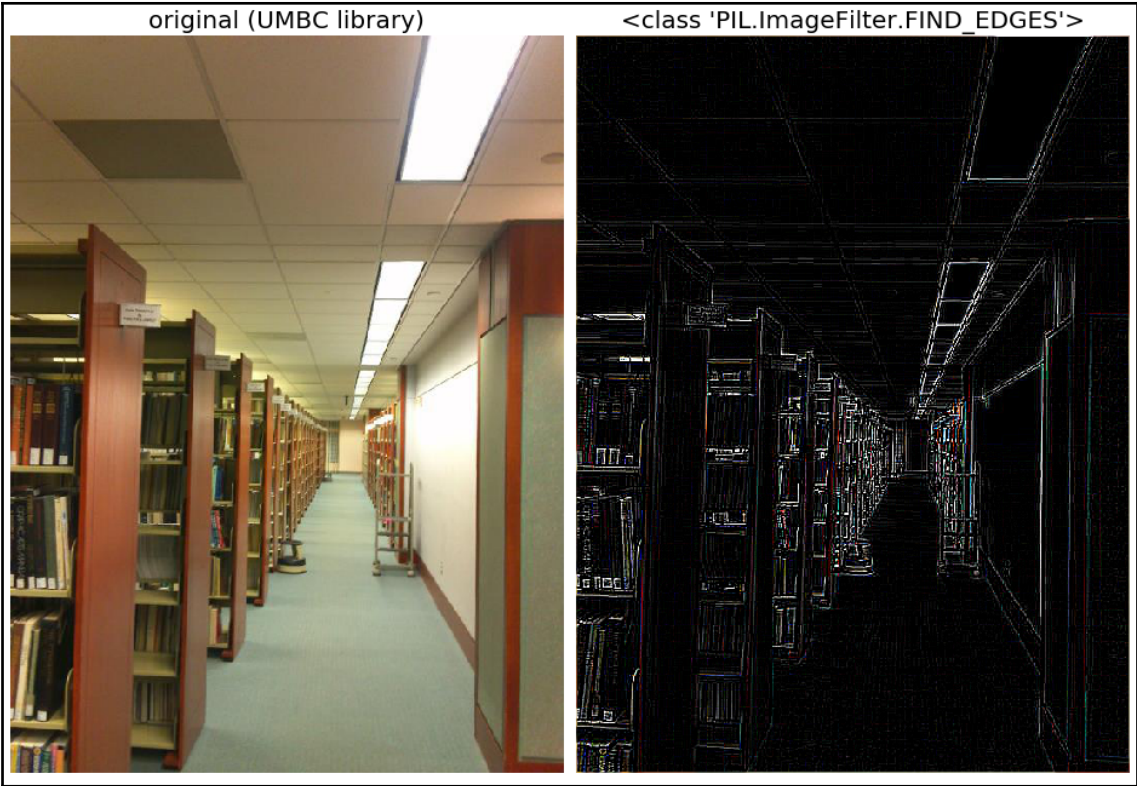


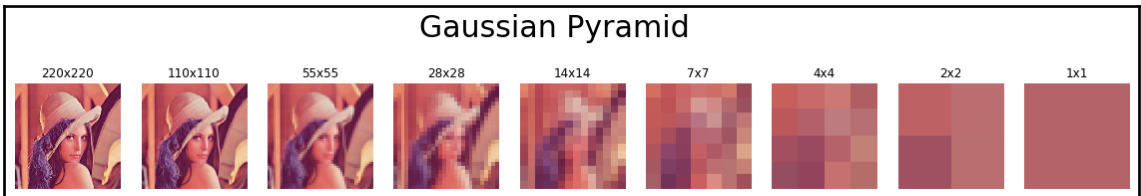








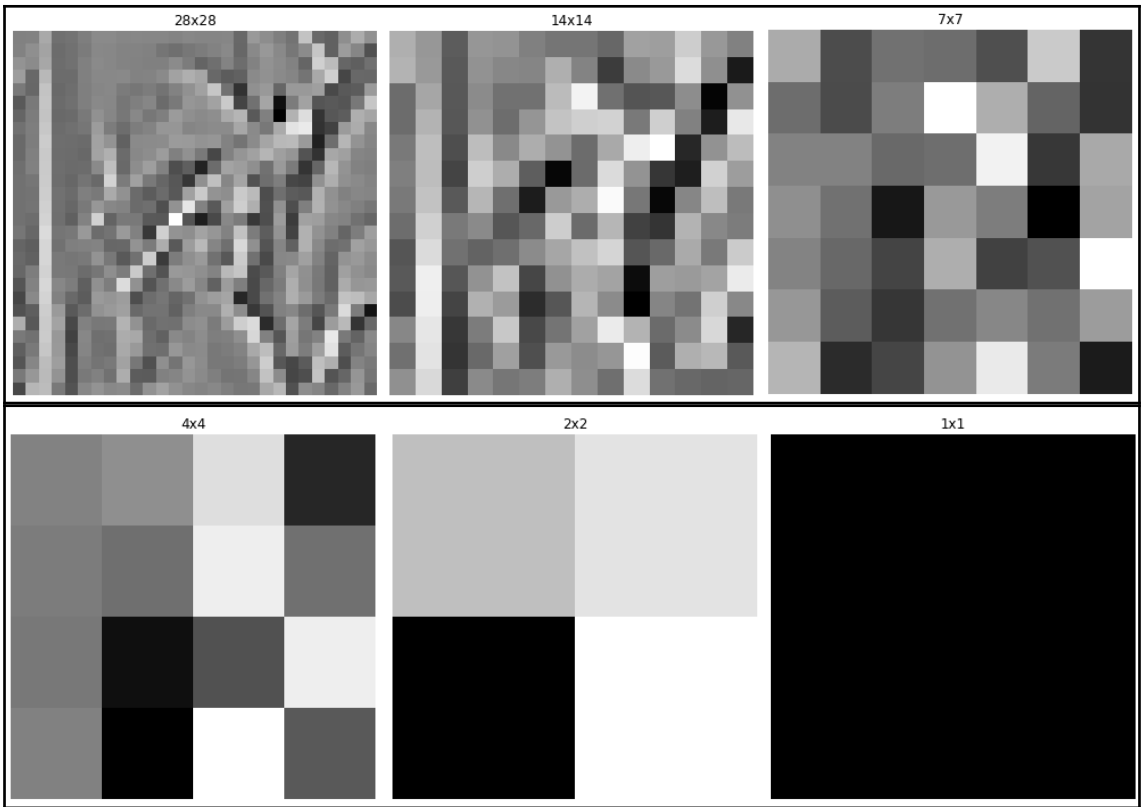






Laplacian Pyramid







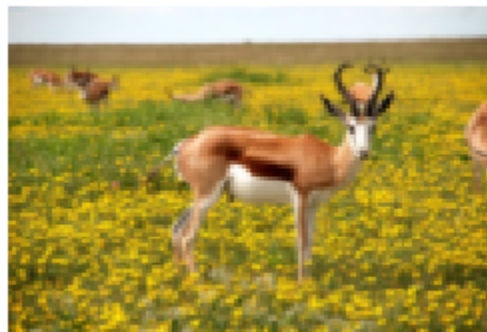
350x523



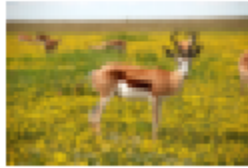
175x262



88x131



44x66



175x262



88x131



44x66

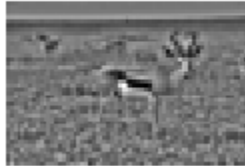
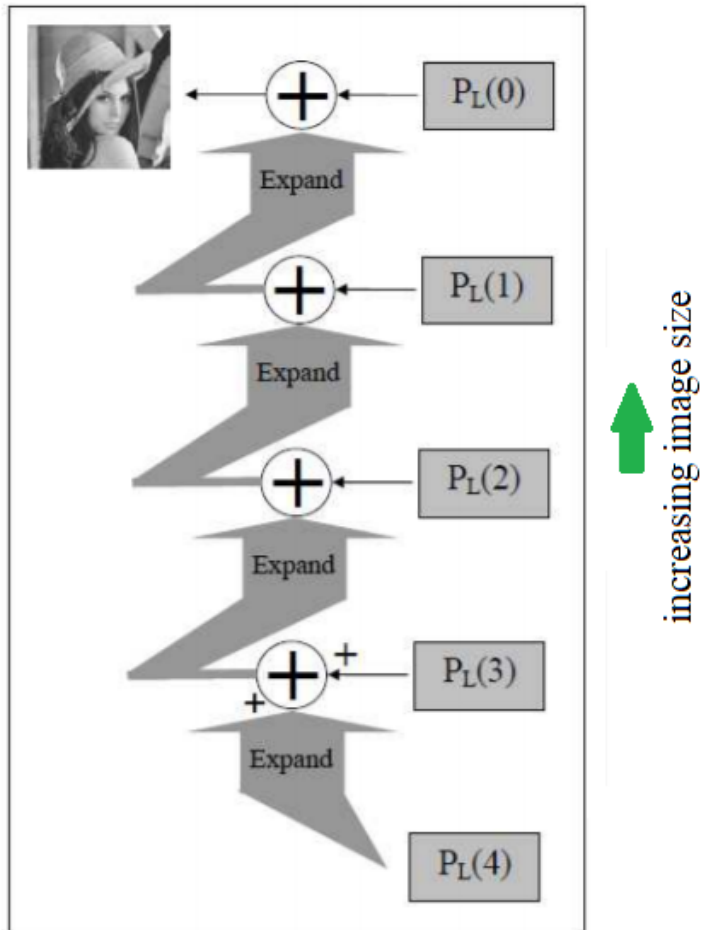
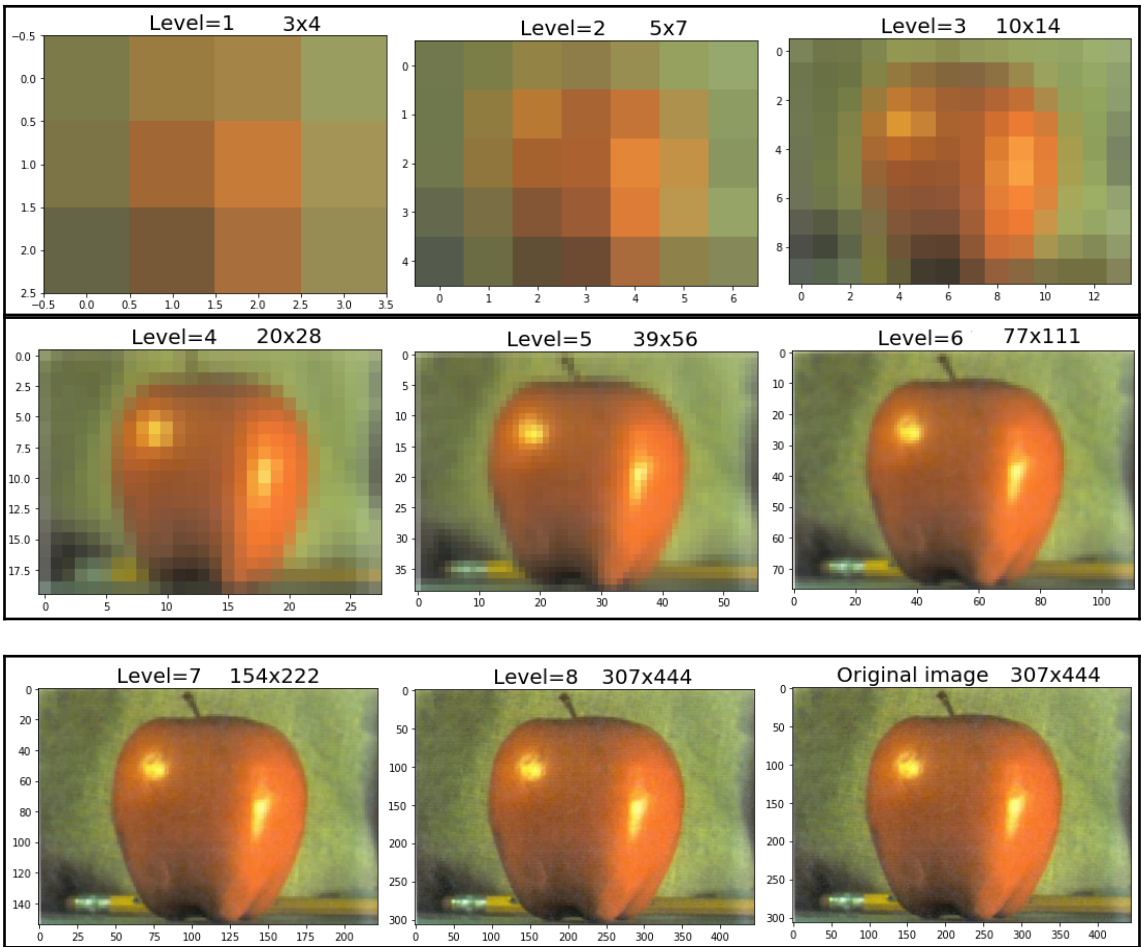
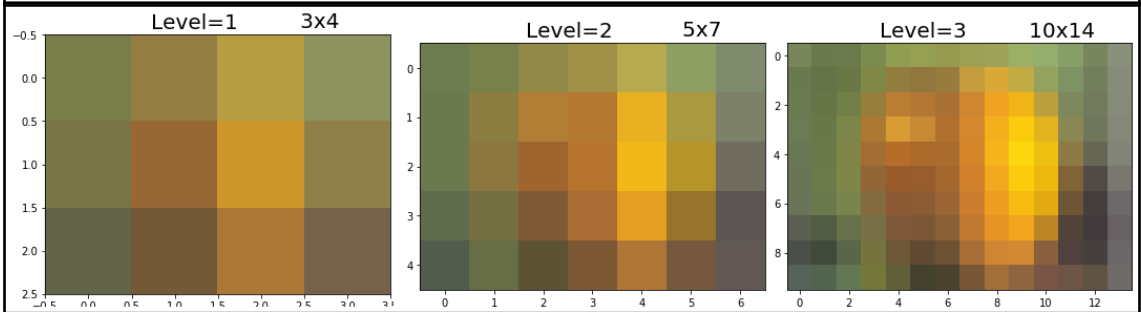
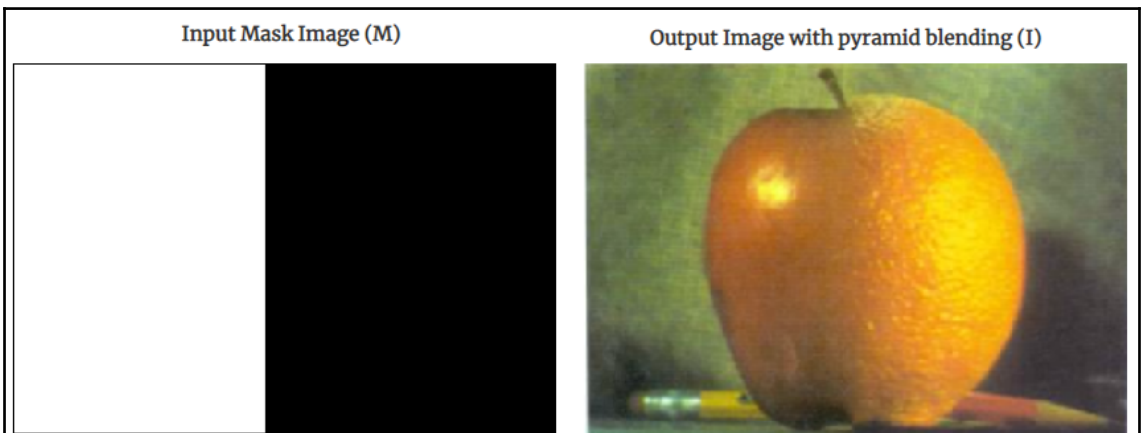
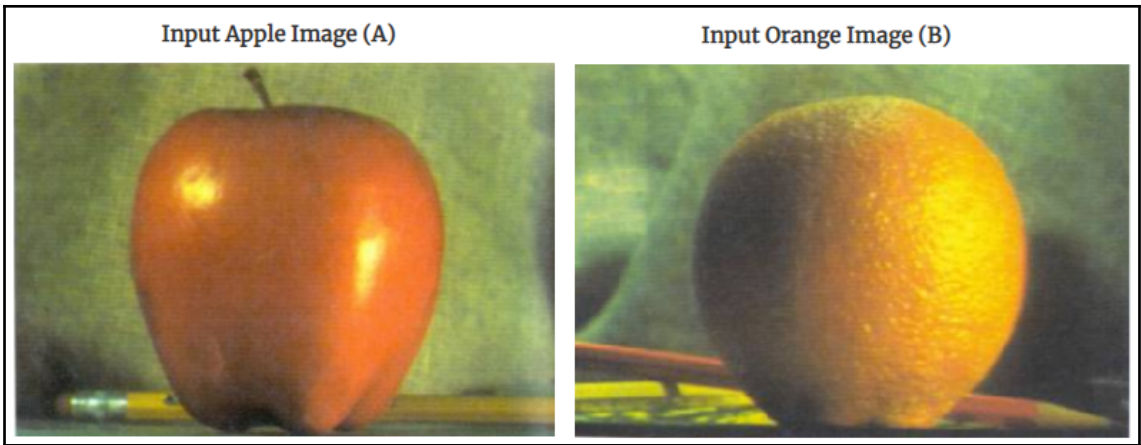


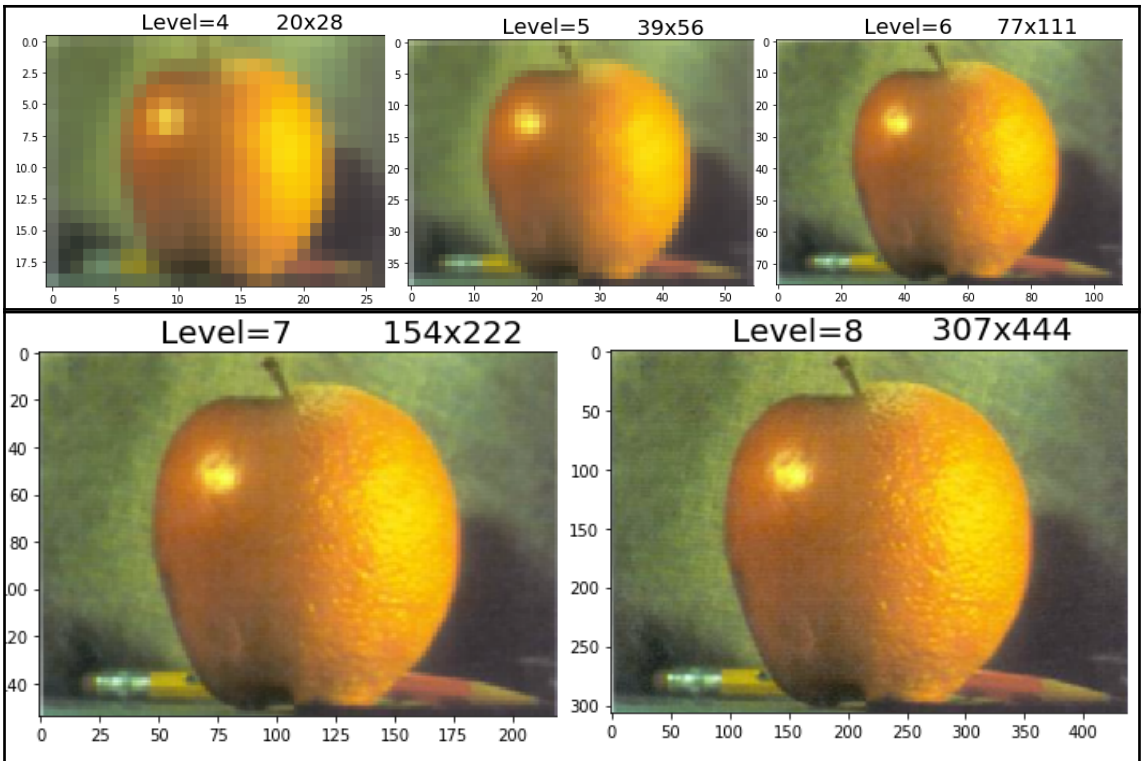
Image Reconstruction from Laplacian pyramid



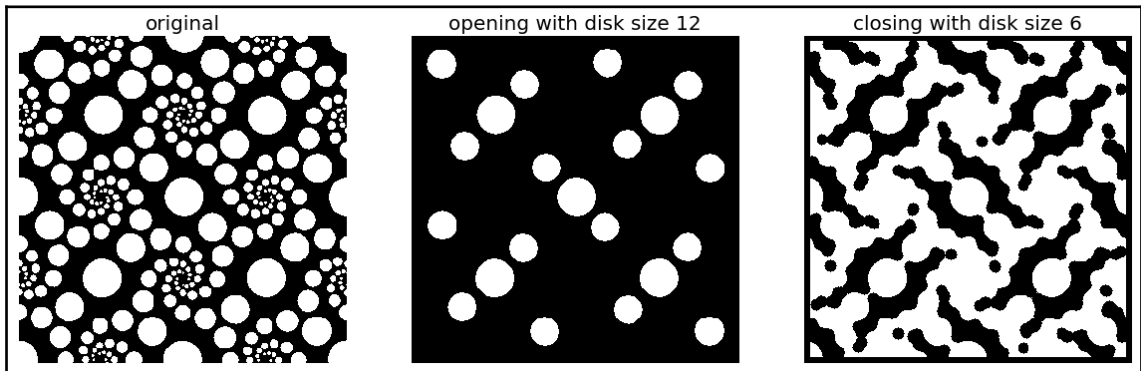
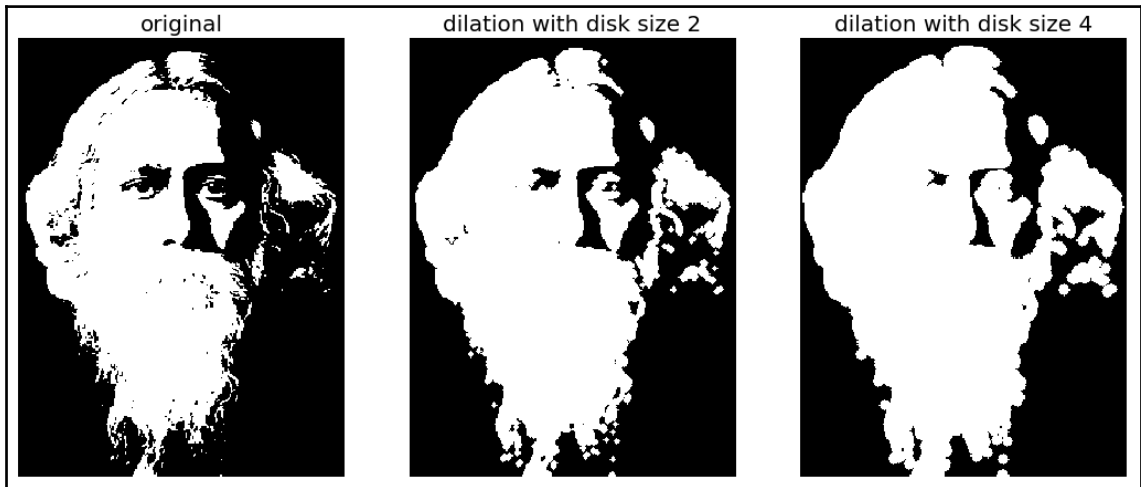
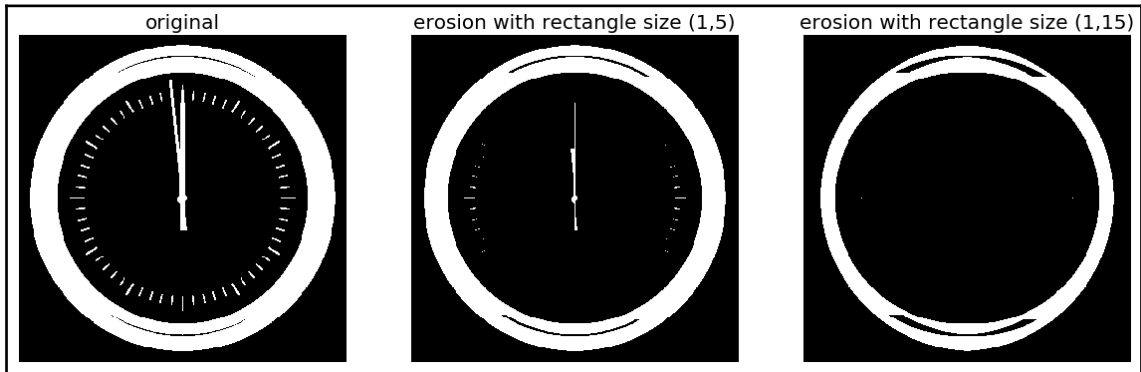
expand = upsample + smooth

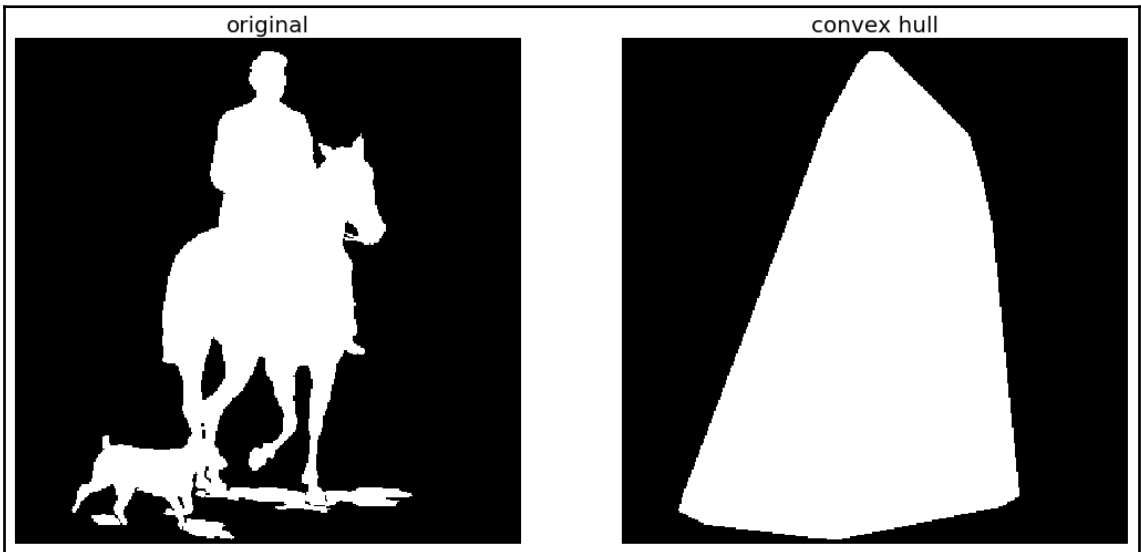
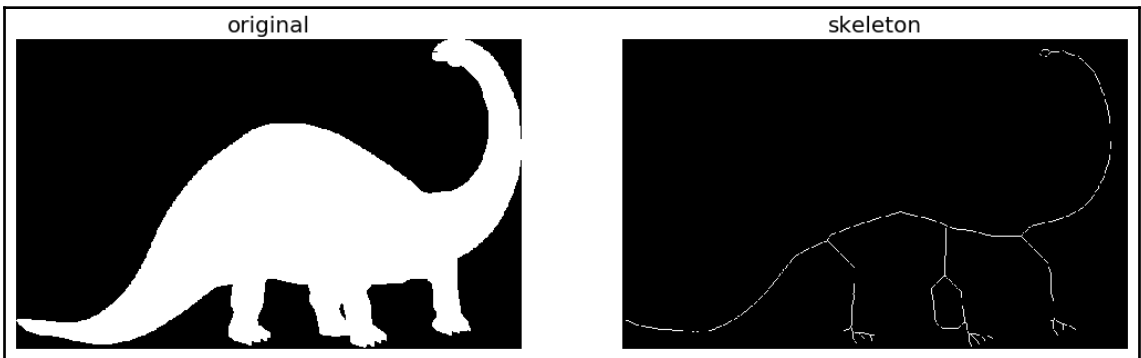
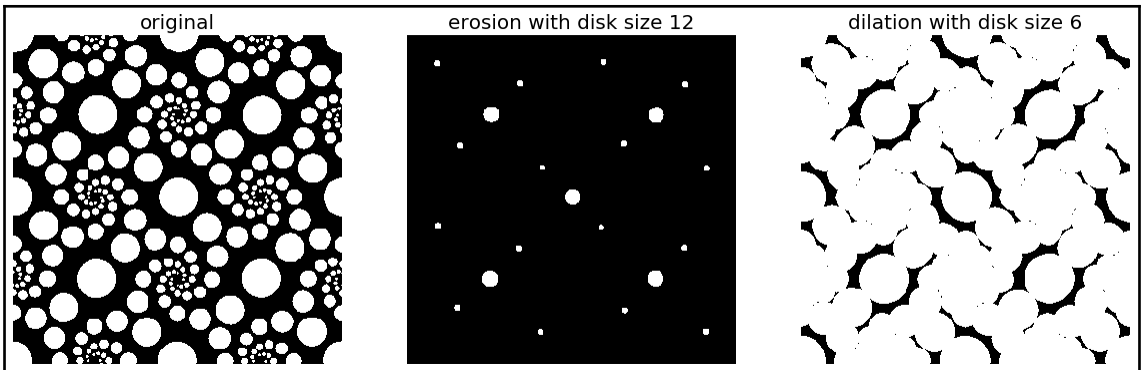


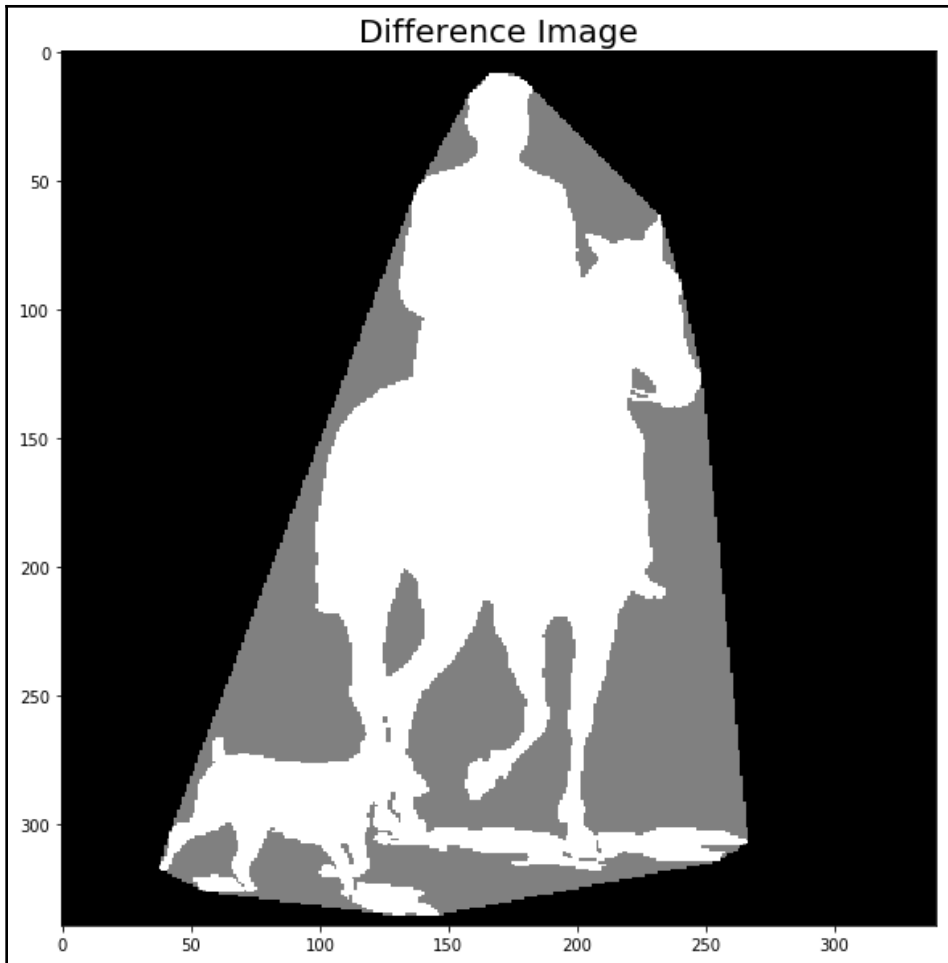


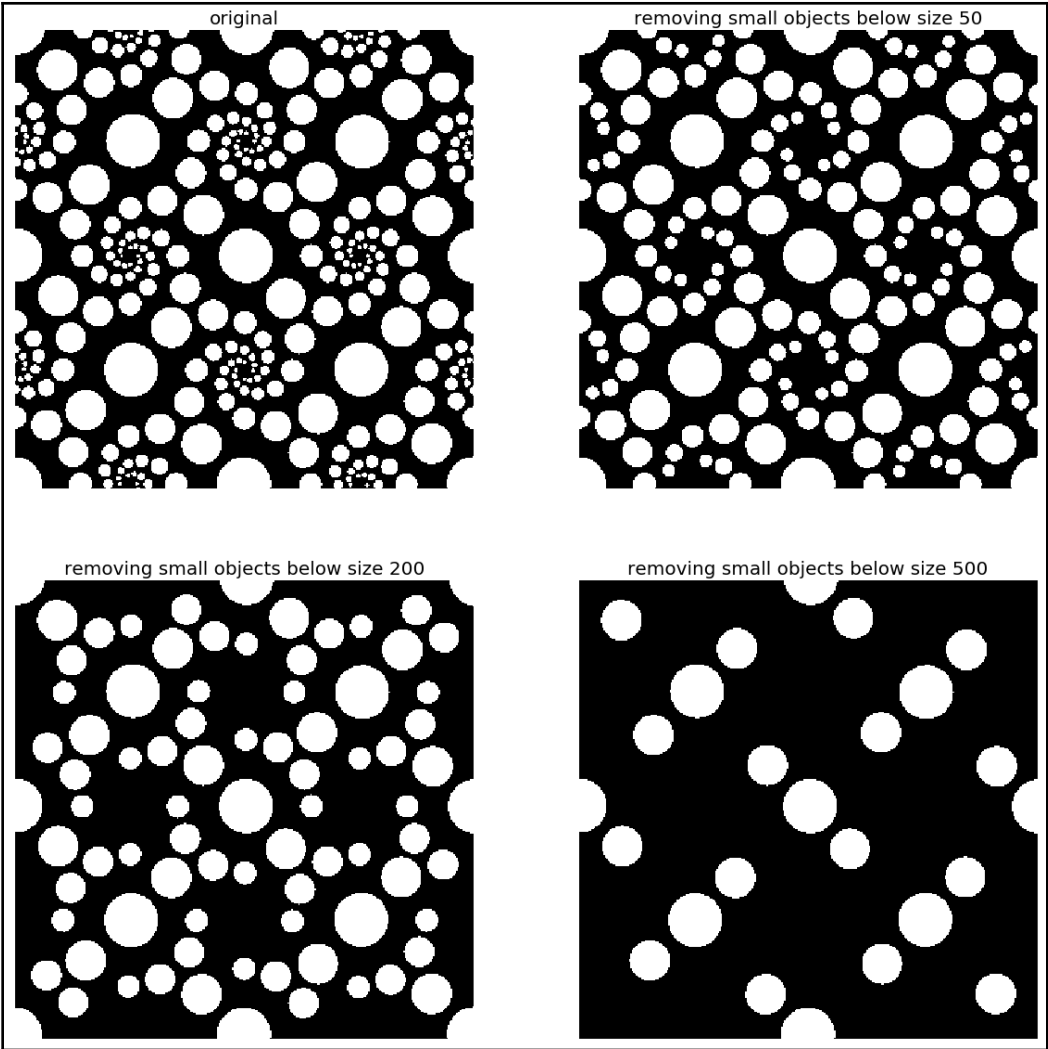


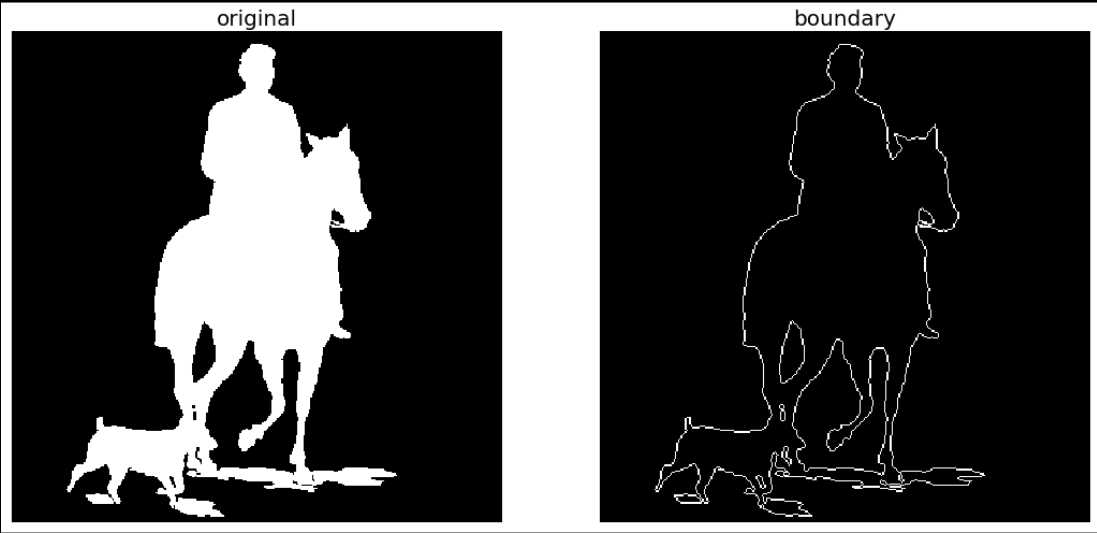
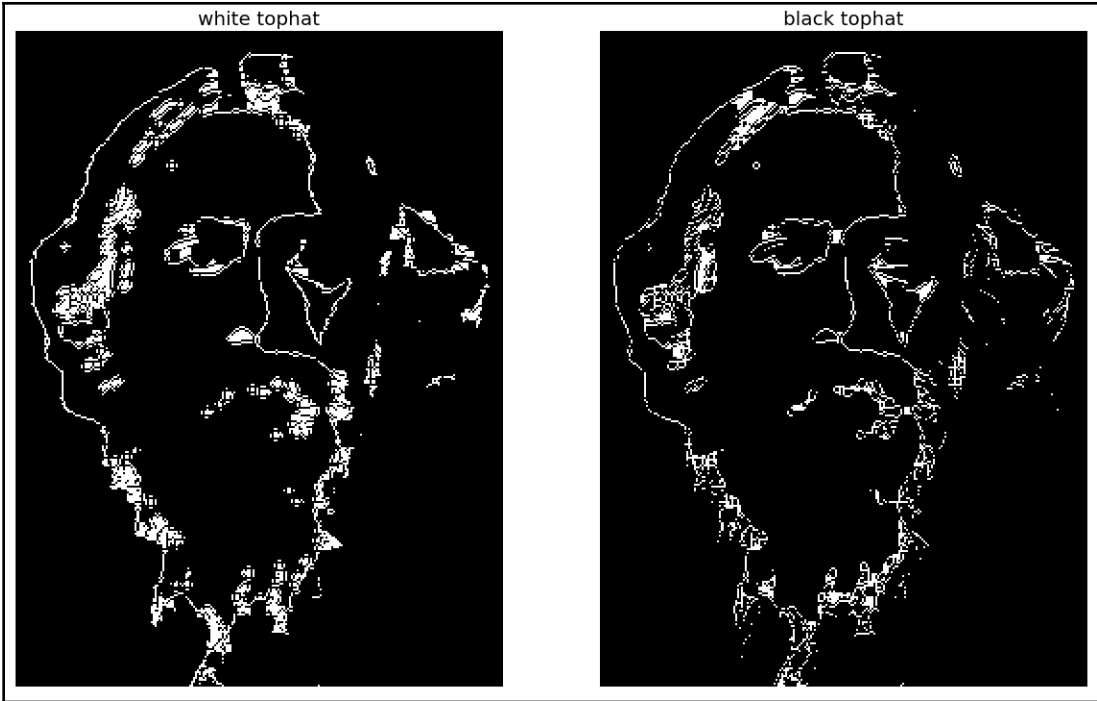
Chapter 6: Morphological Image Processing

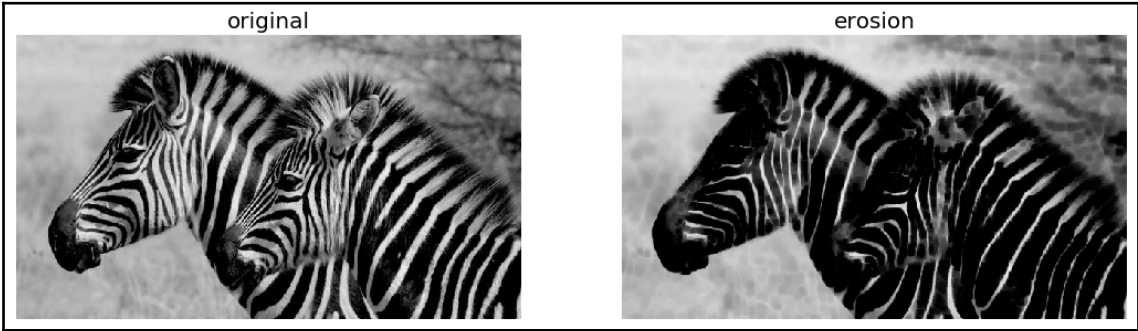
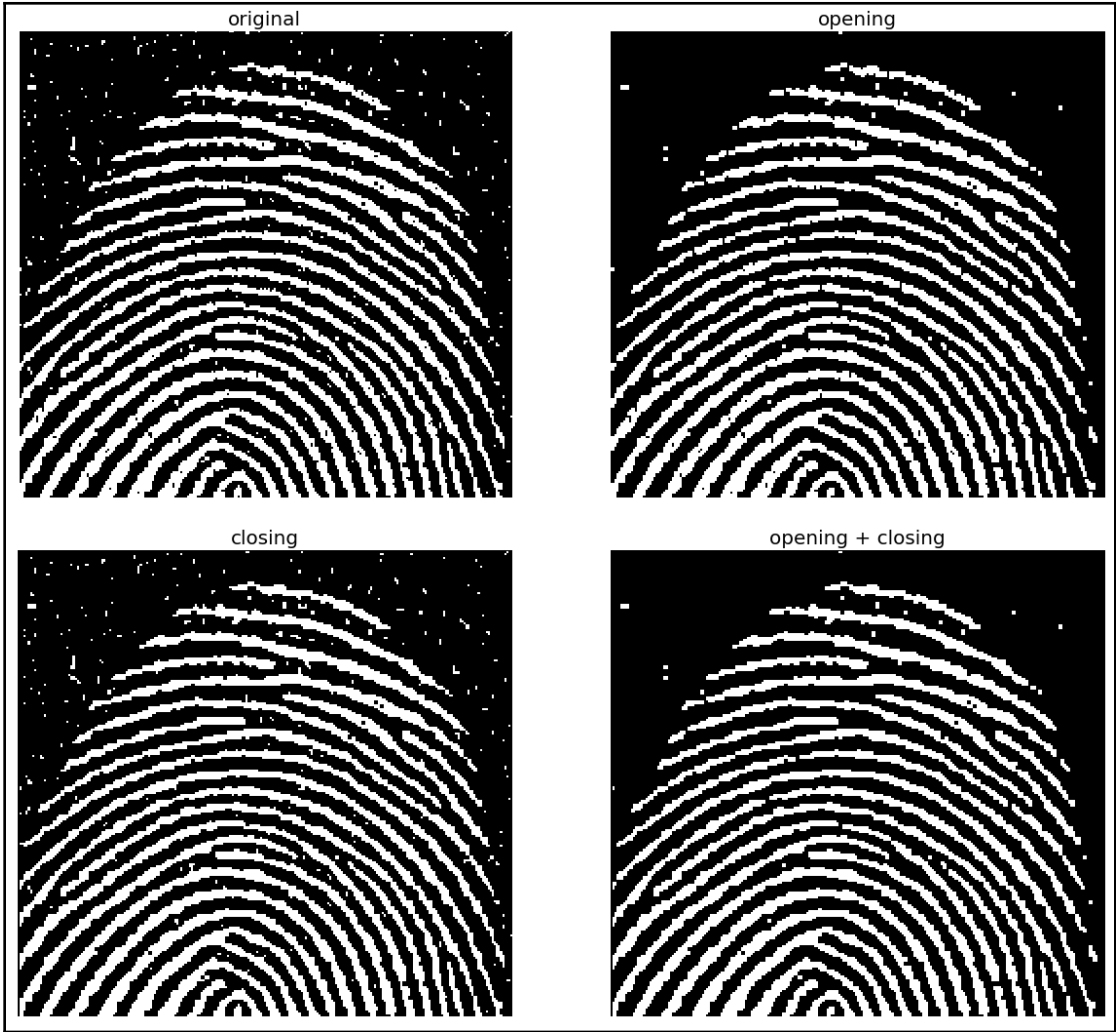


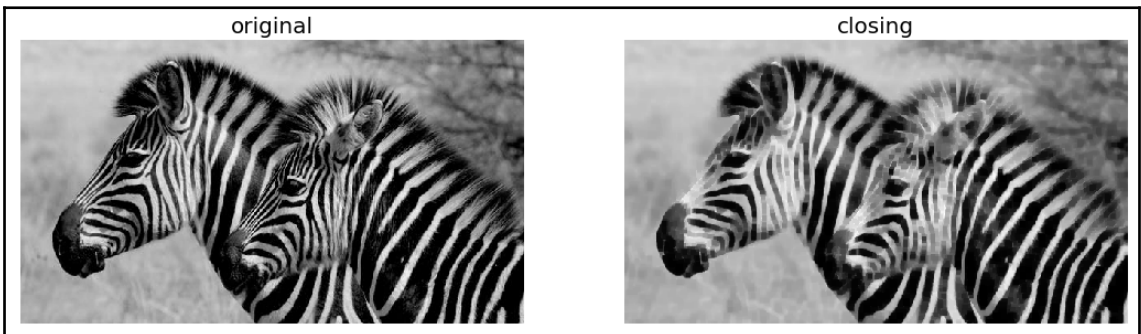
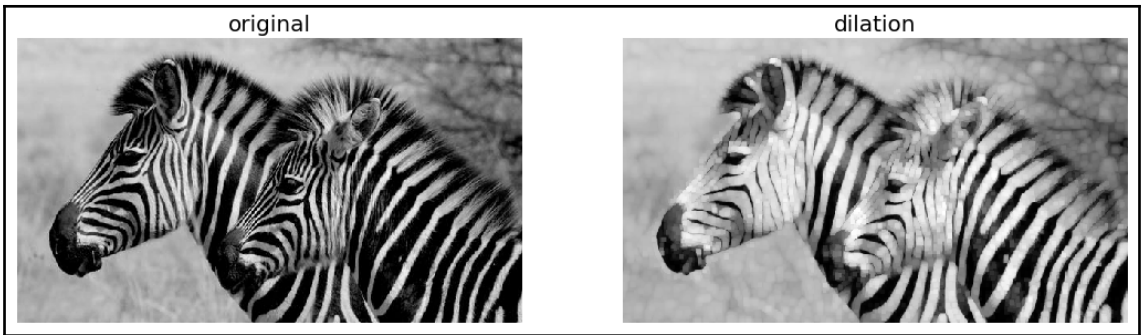


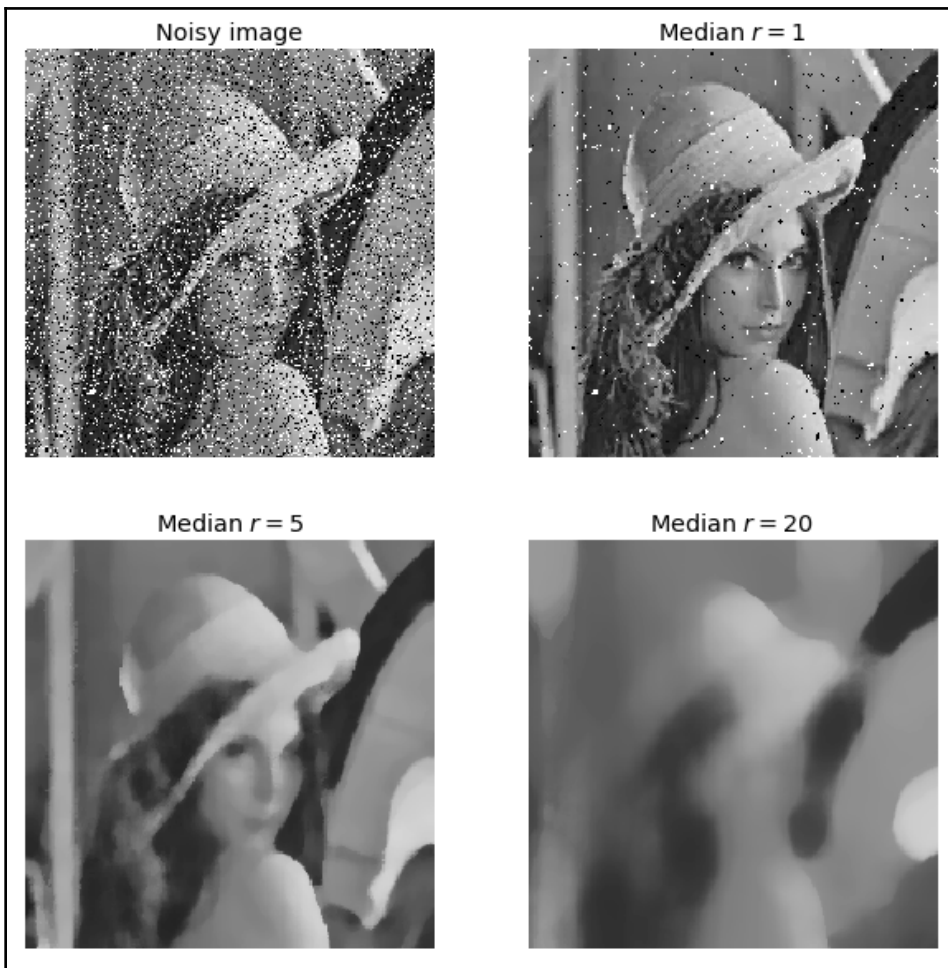


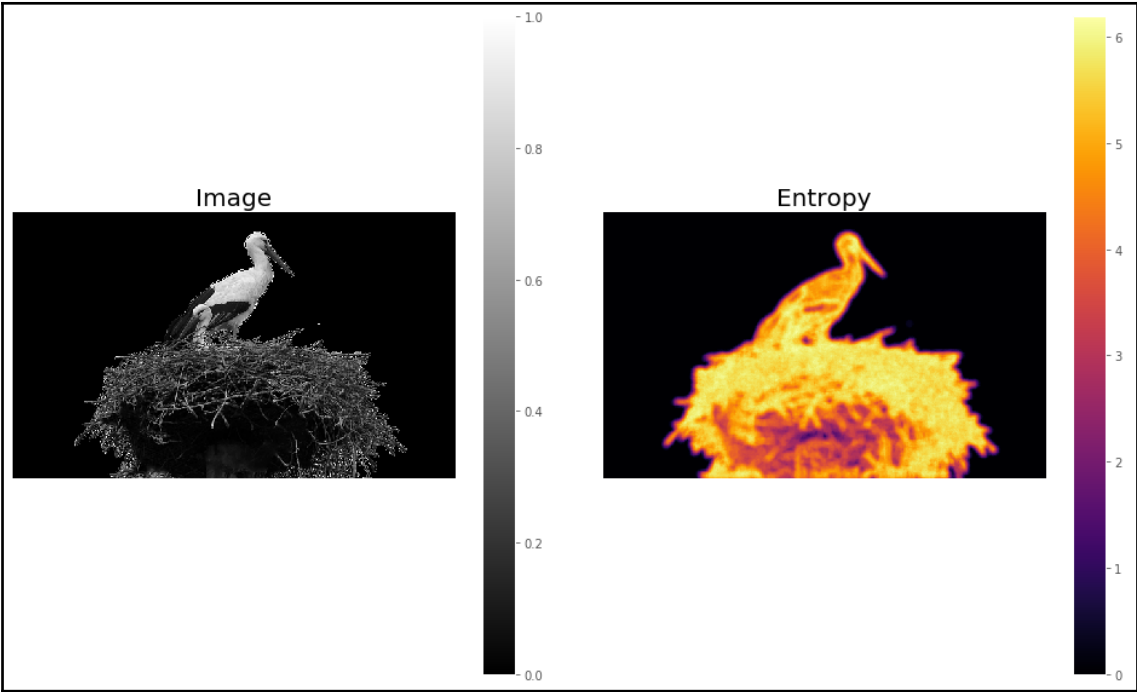


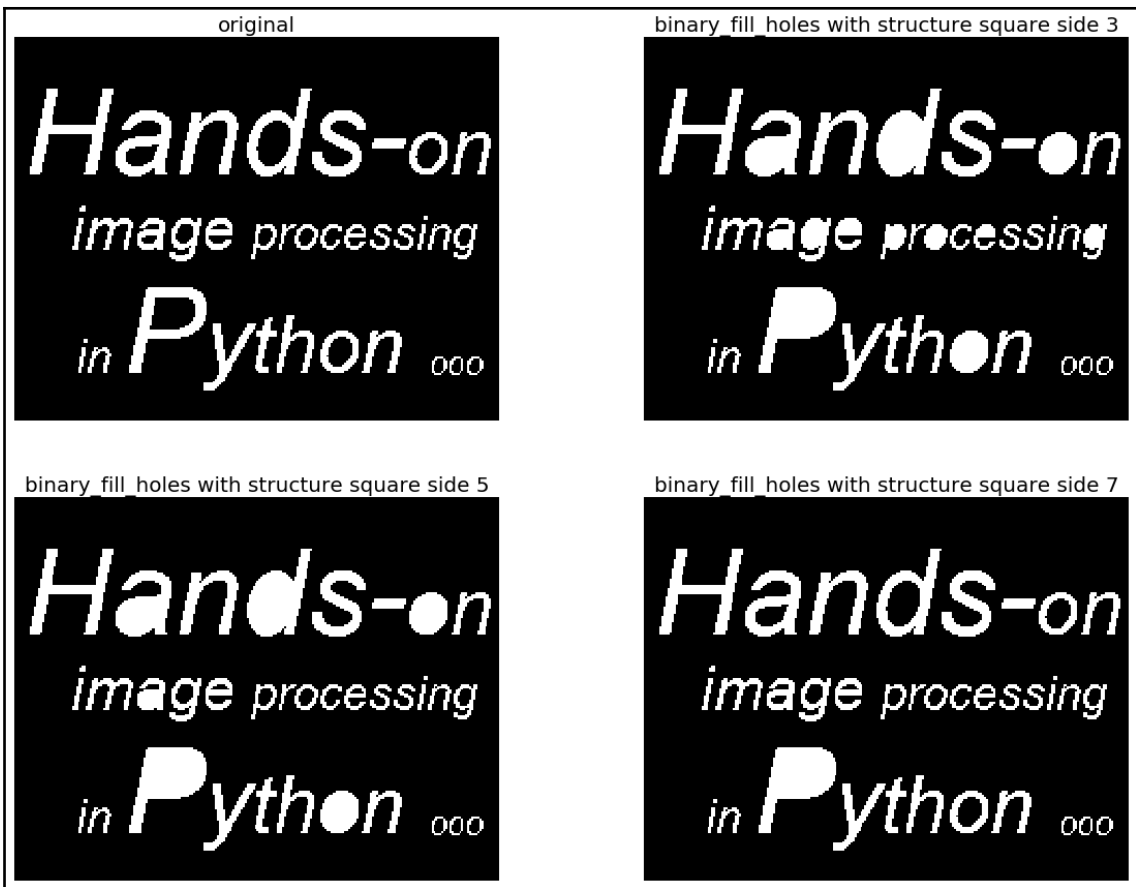


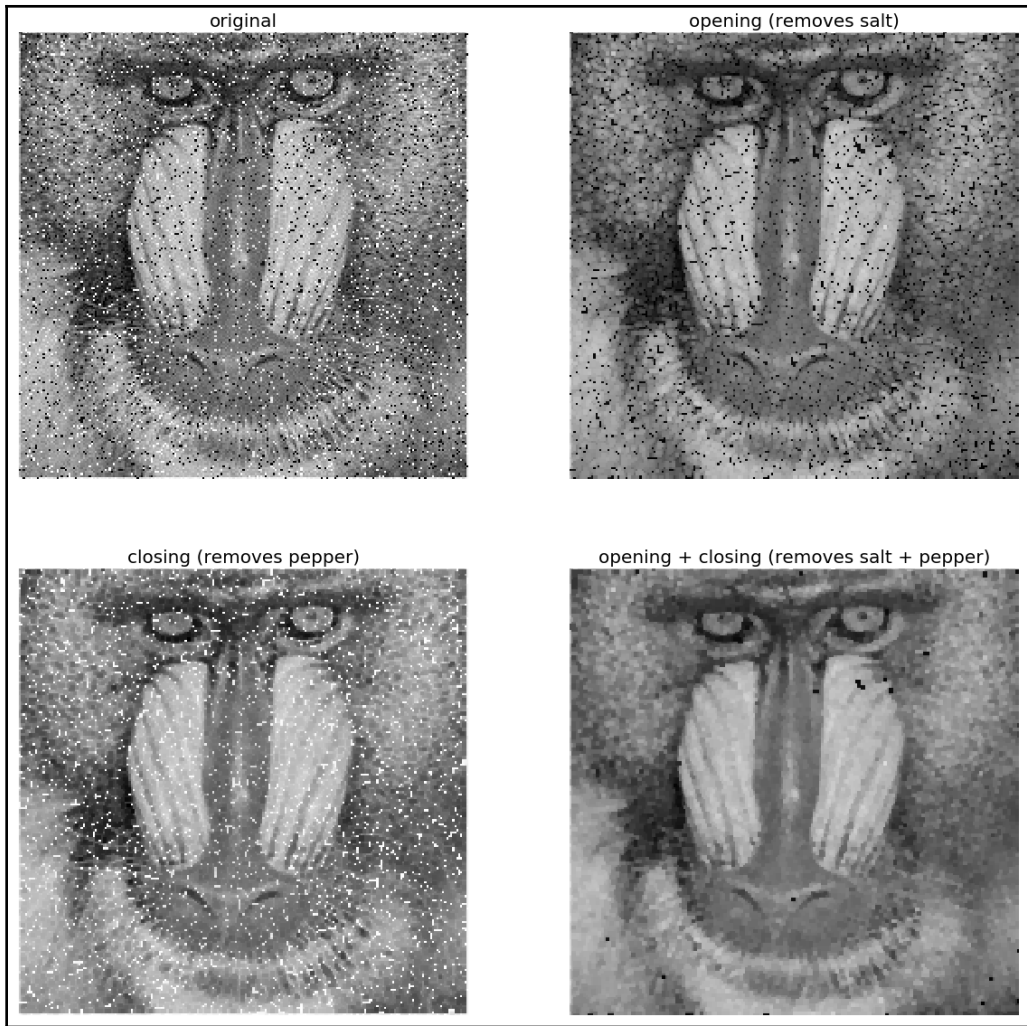


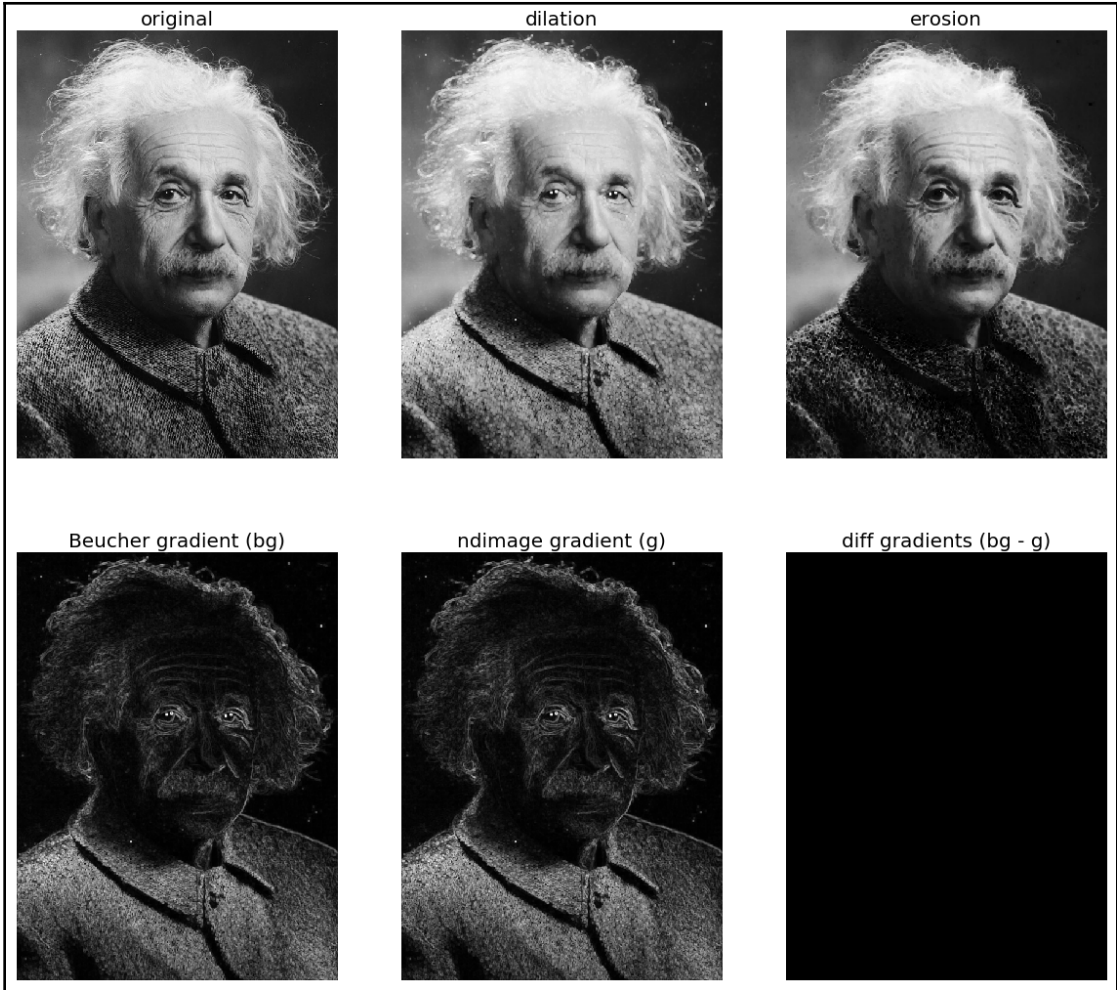


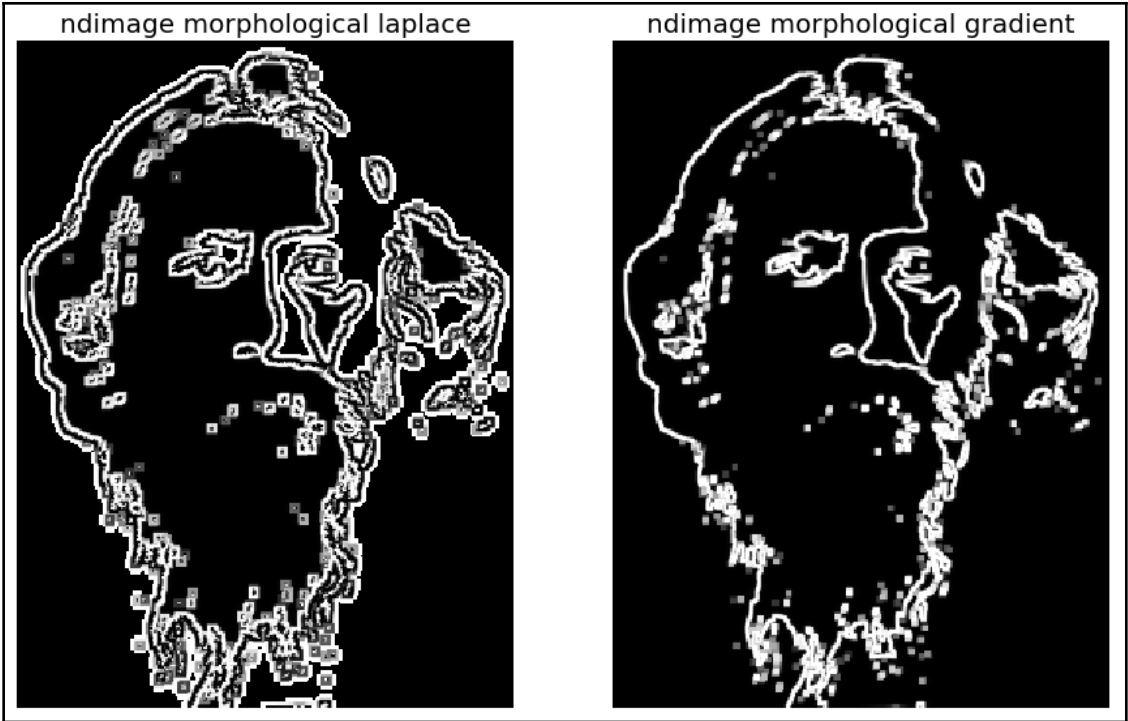


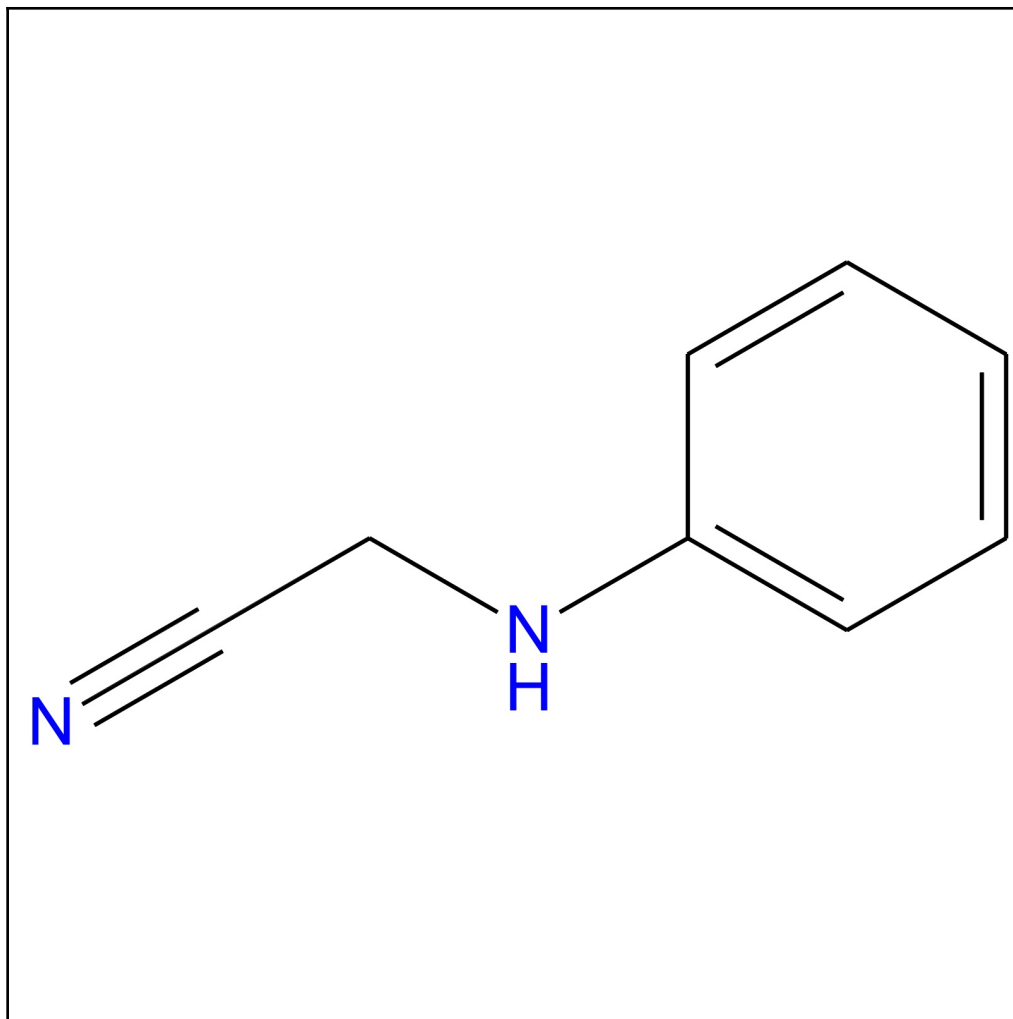


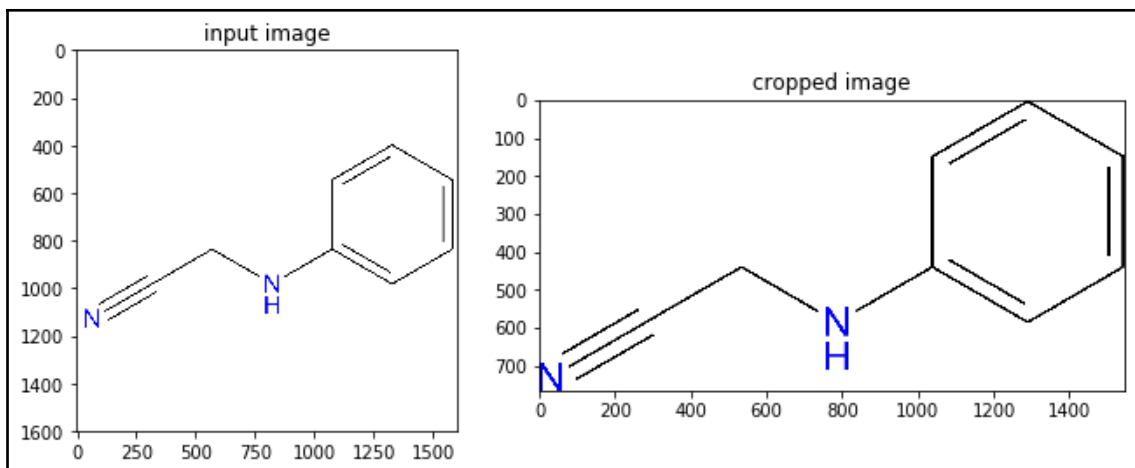




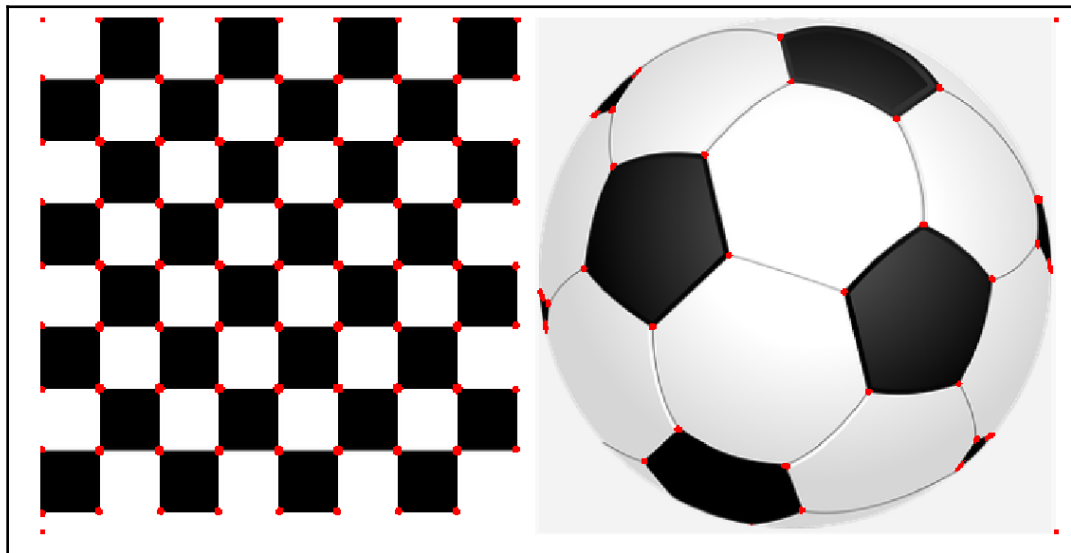
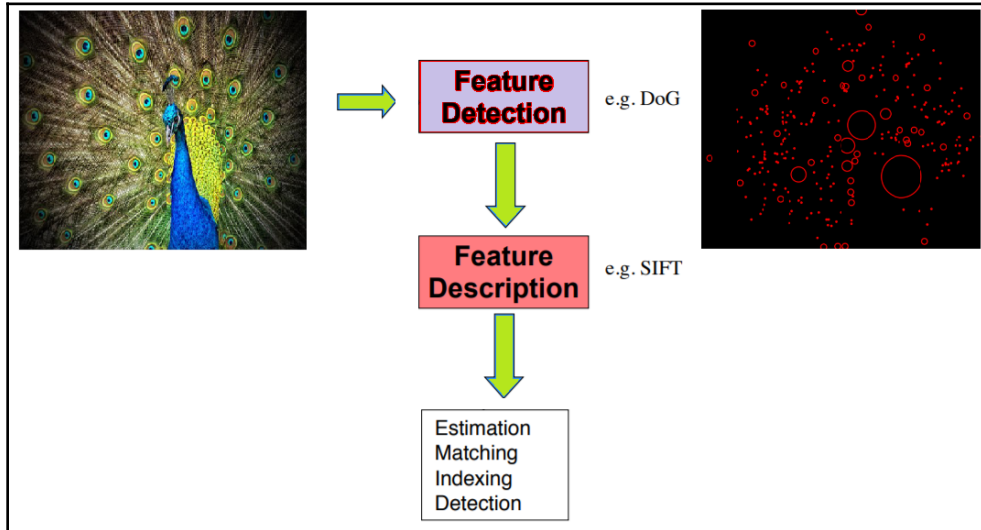


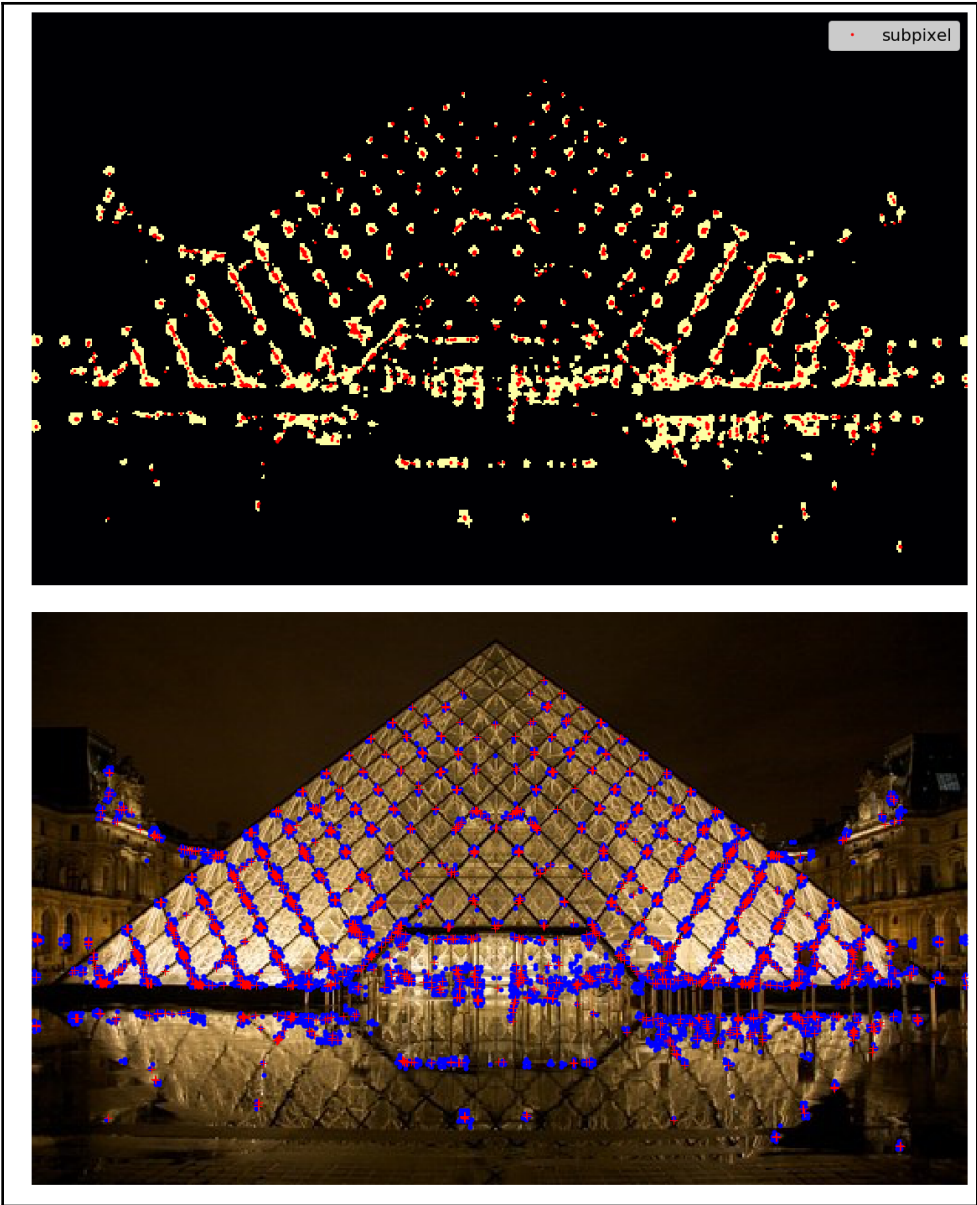


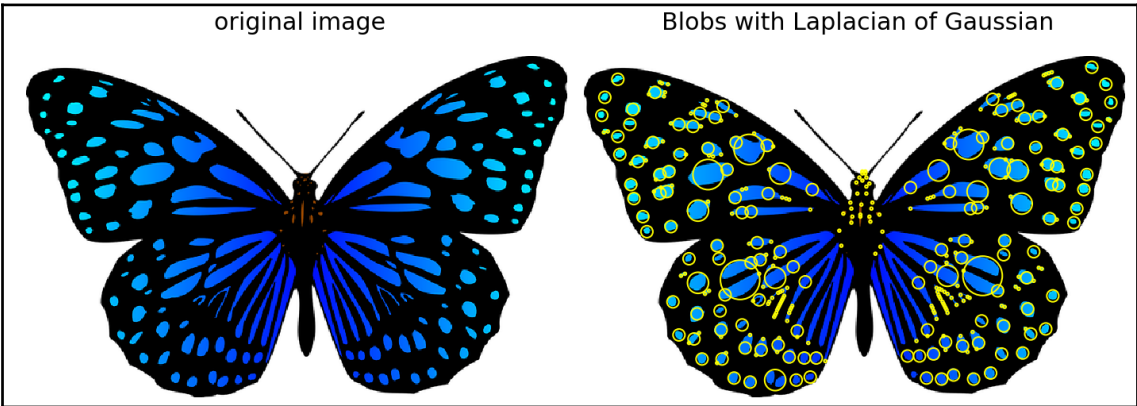
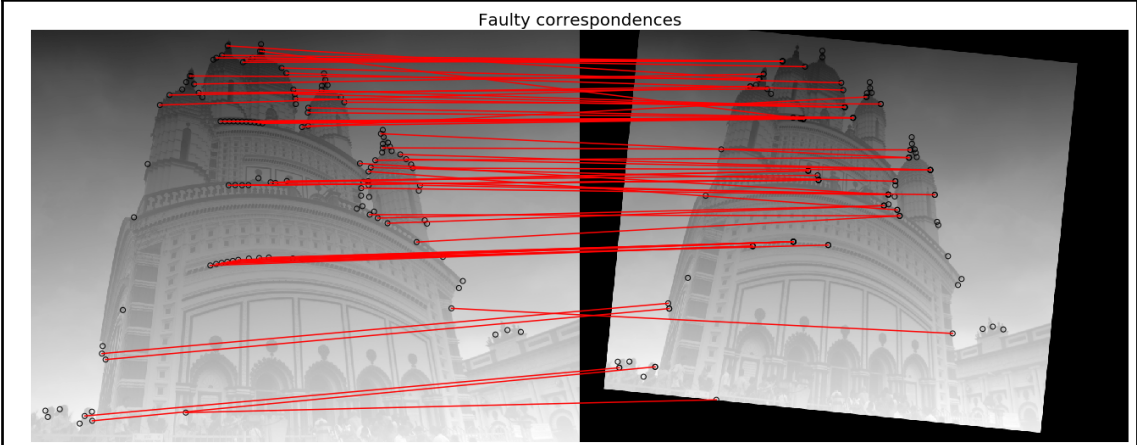
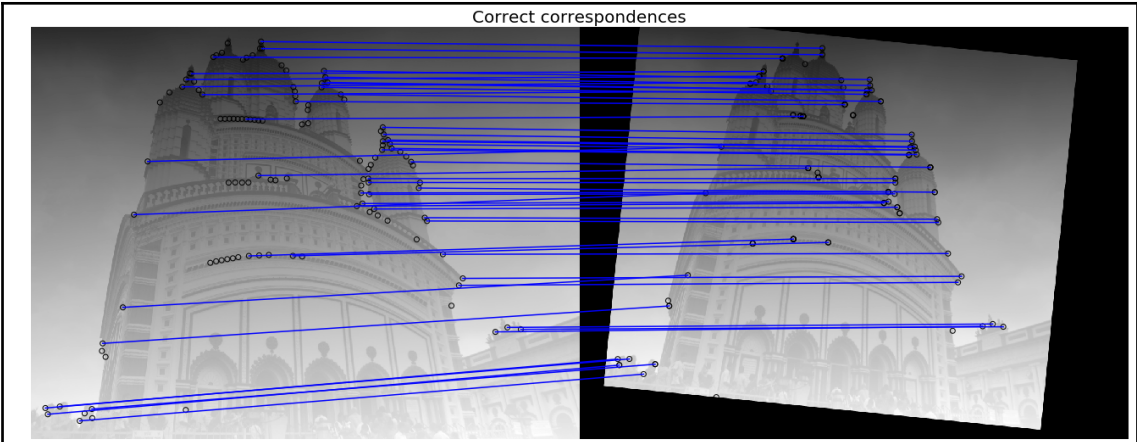


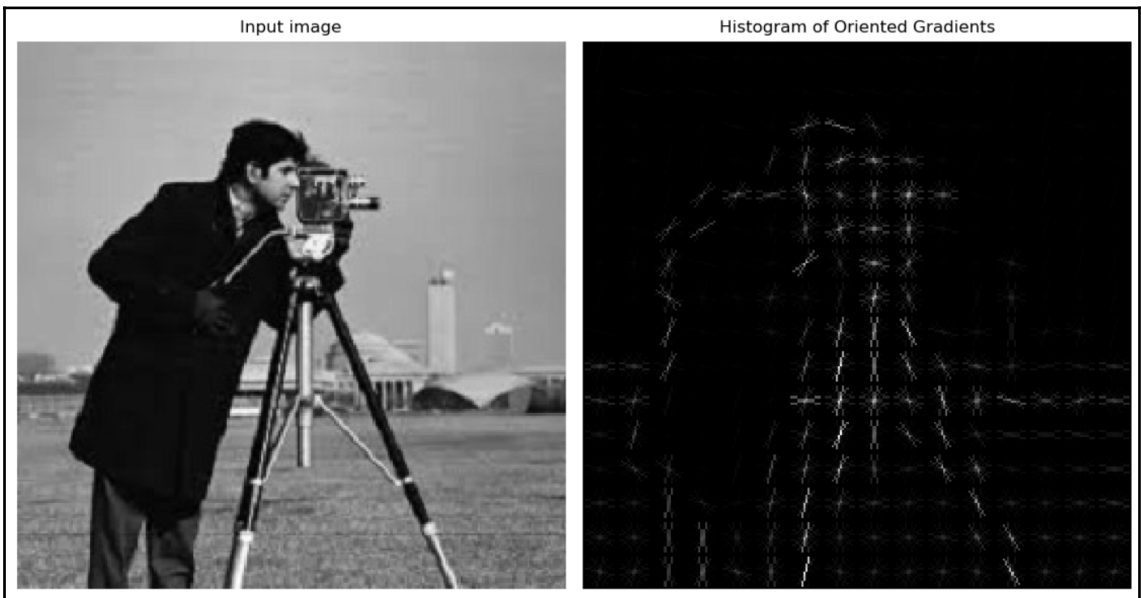
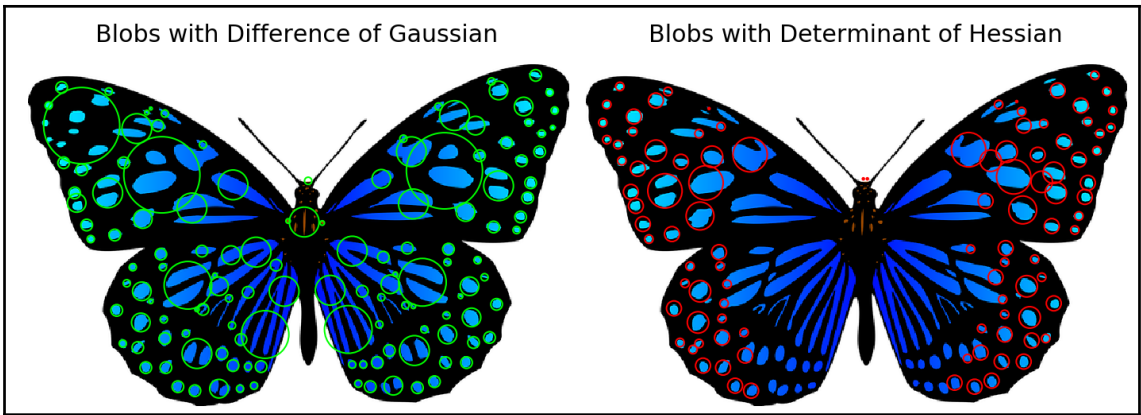


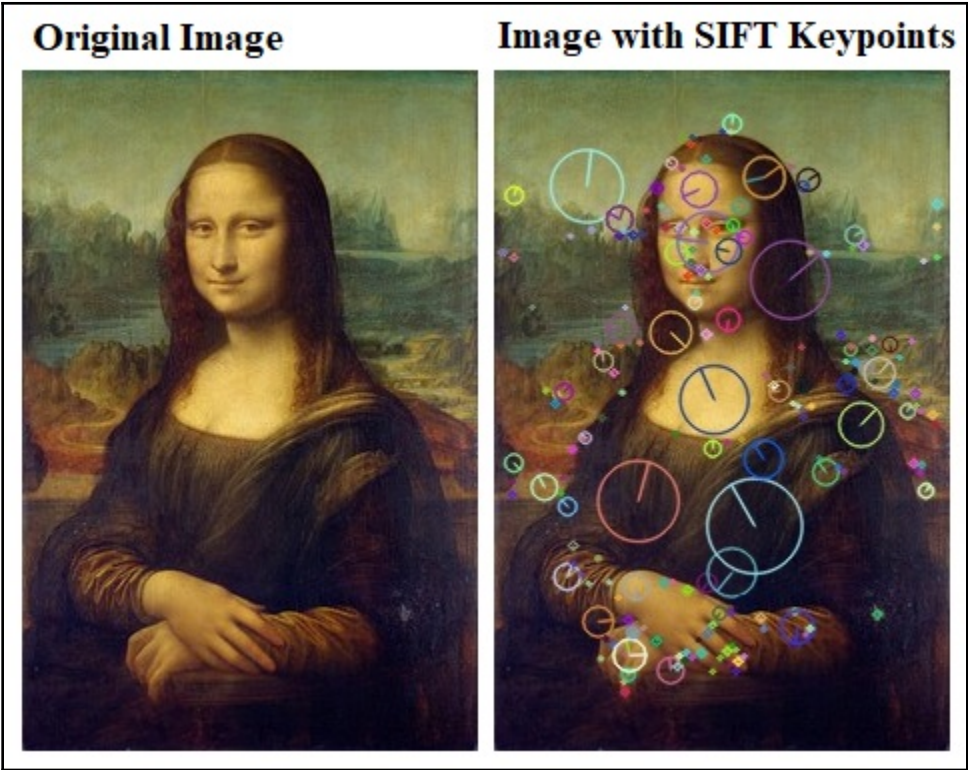
Chapter 7: Extracting Image Features and Descriptors

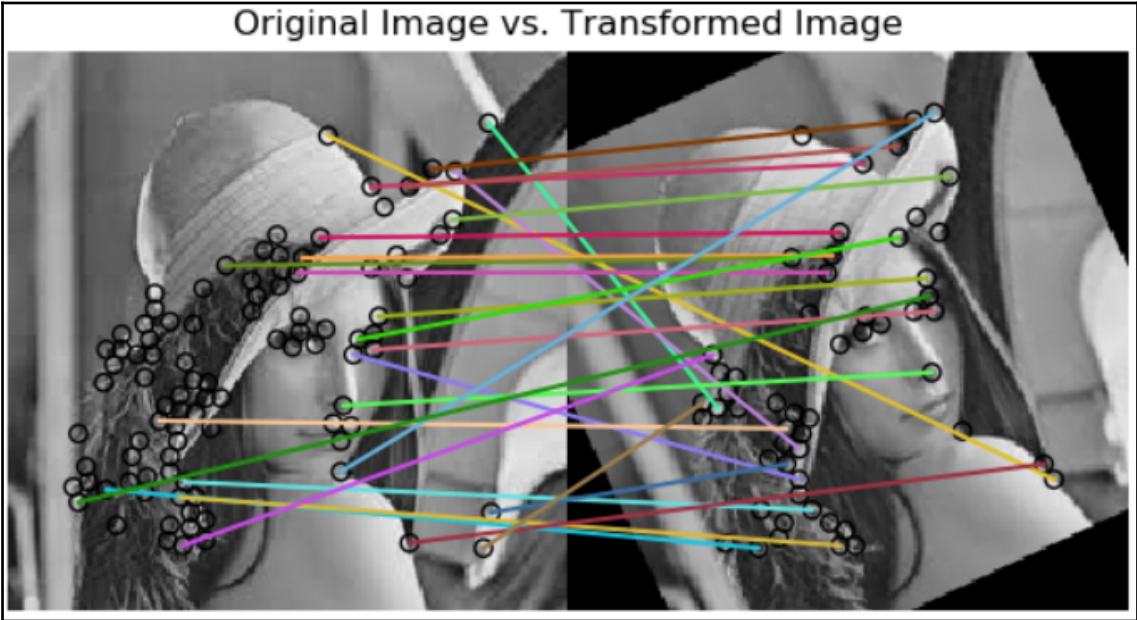
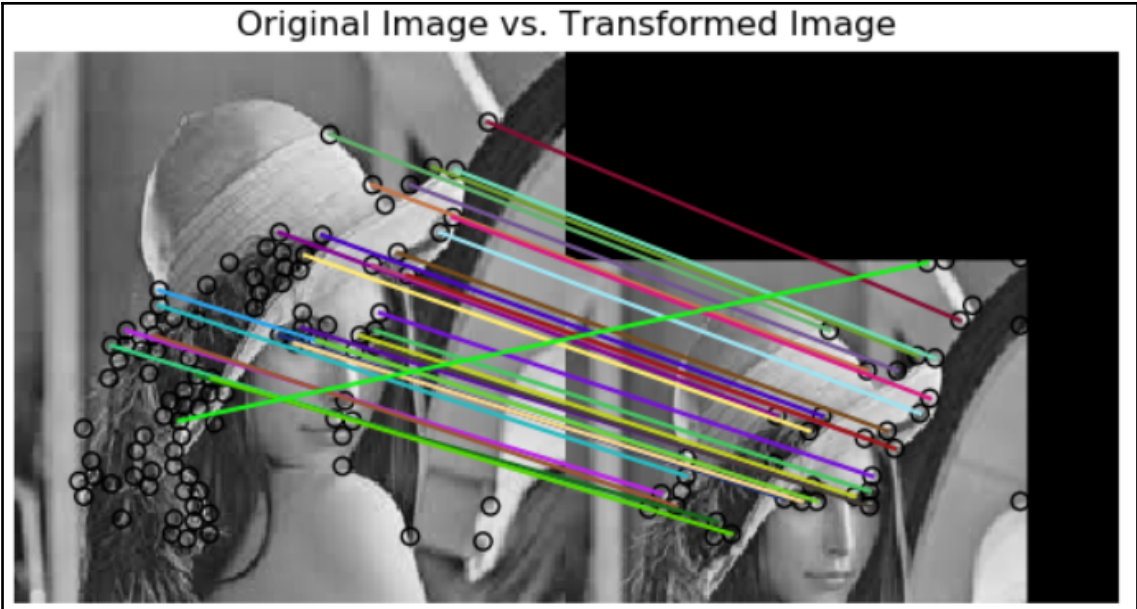


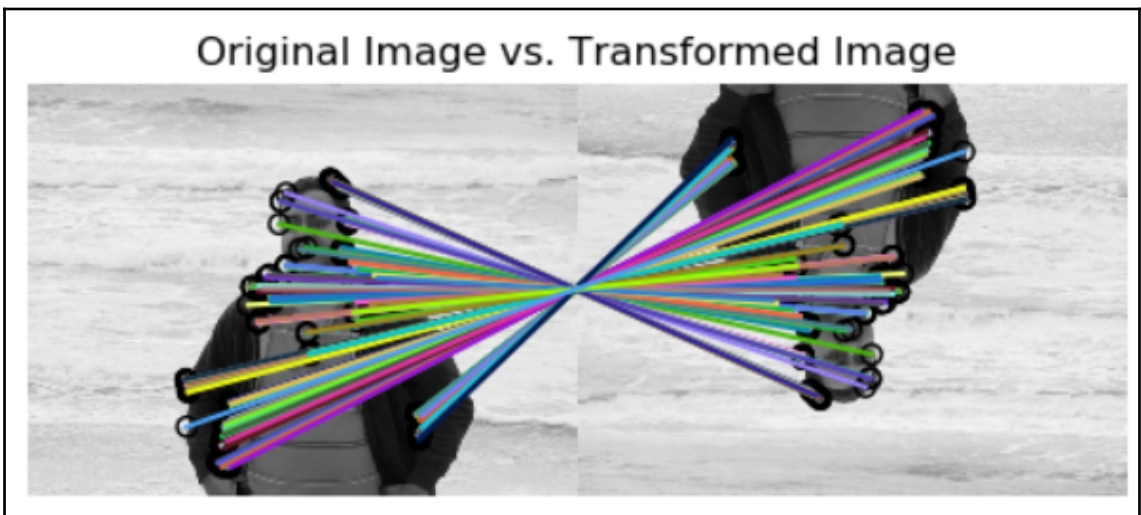












Original Image vs. Transformed Image

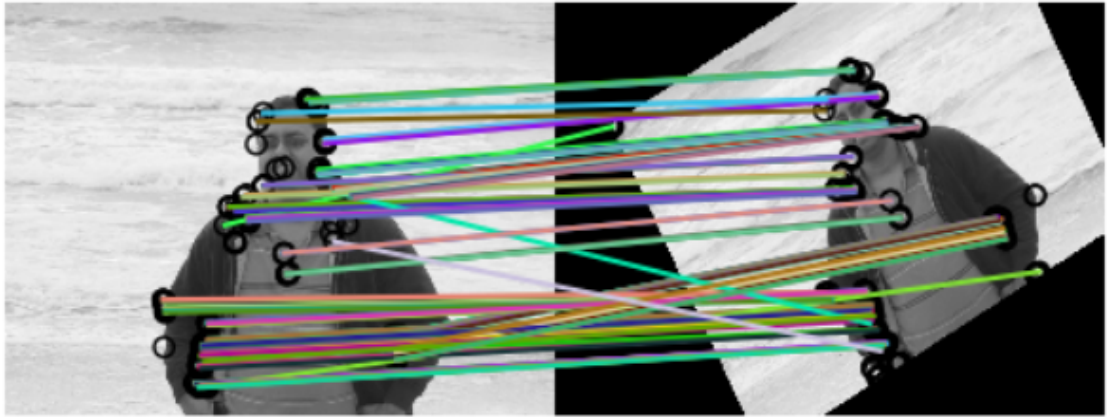
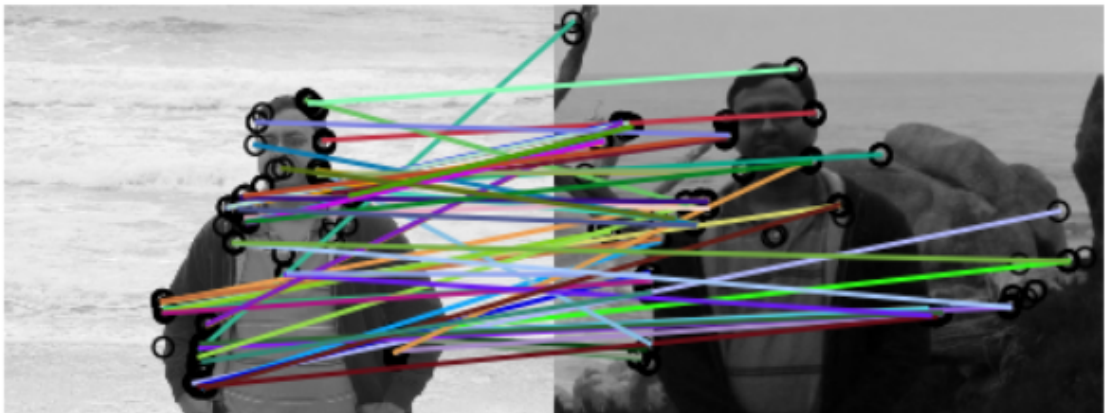
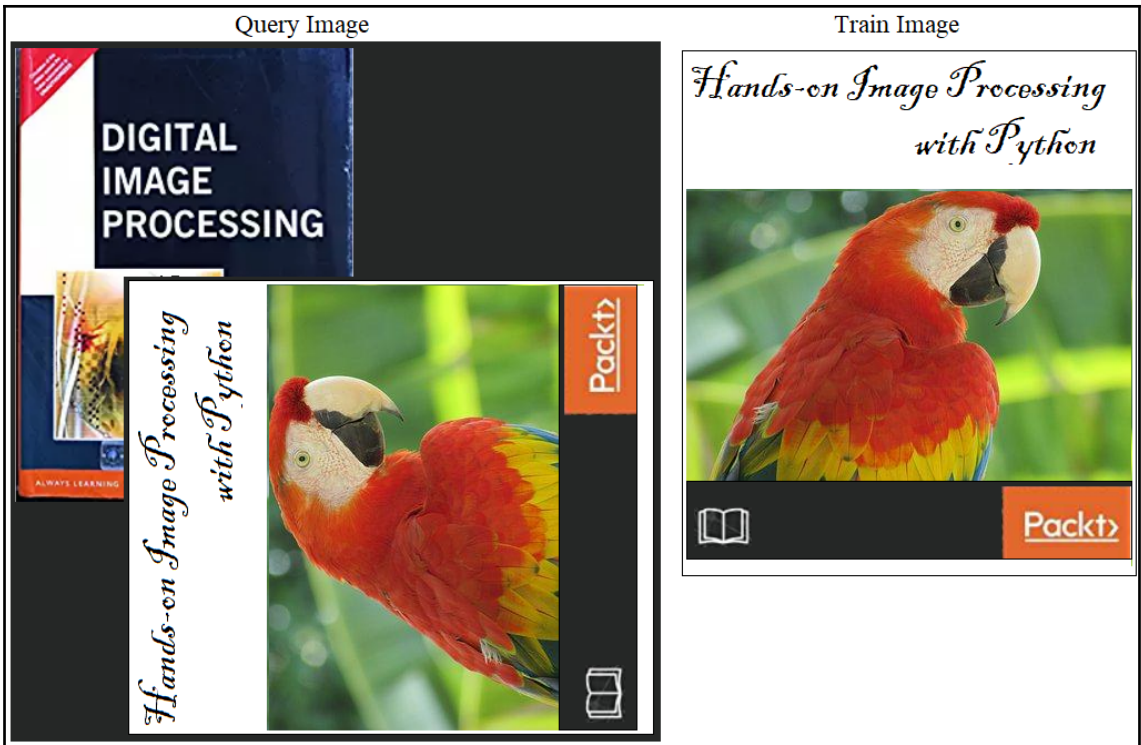
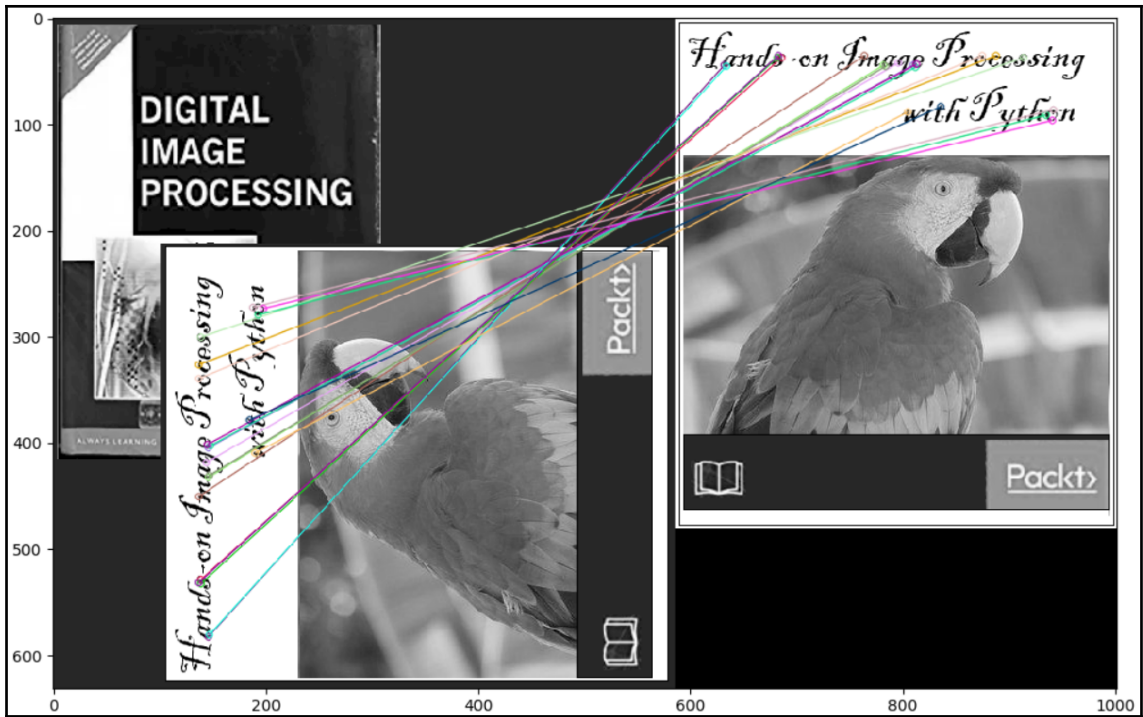
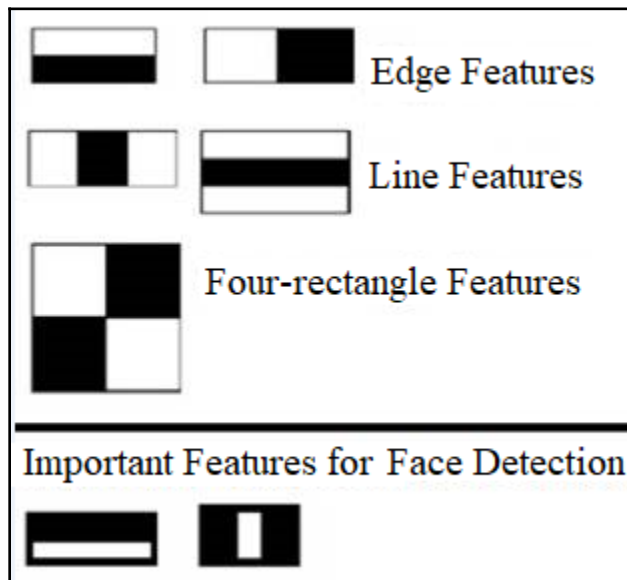
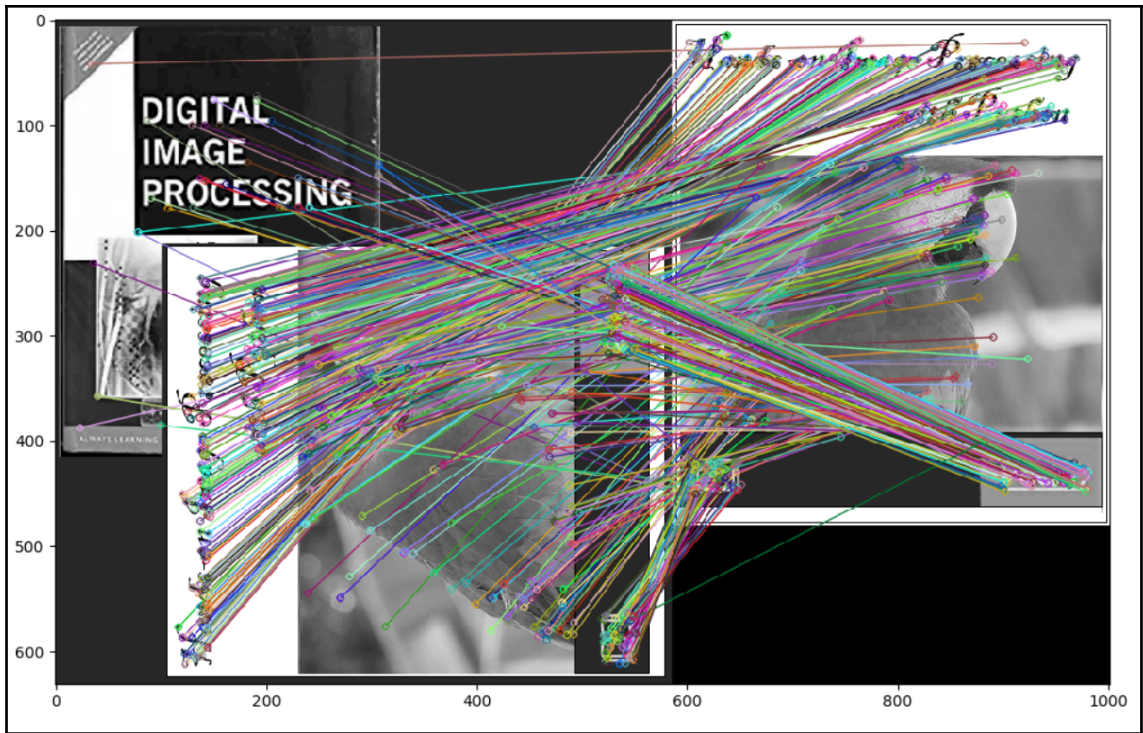


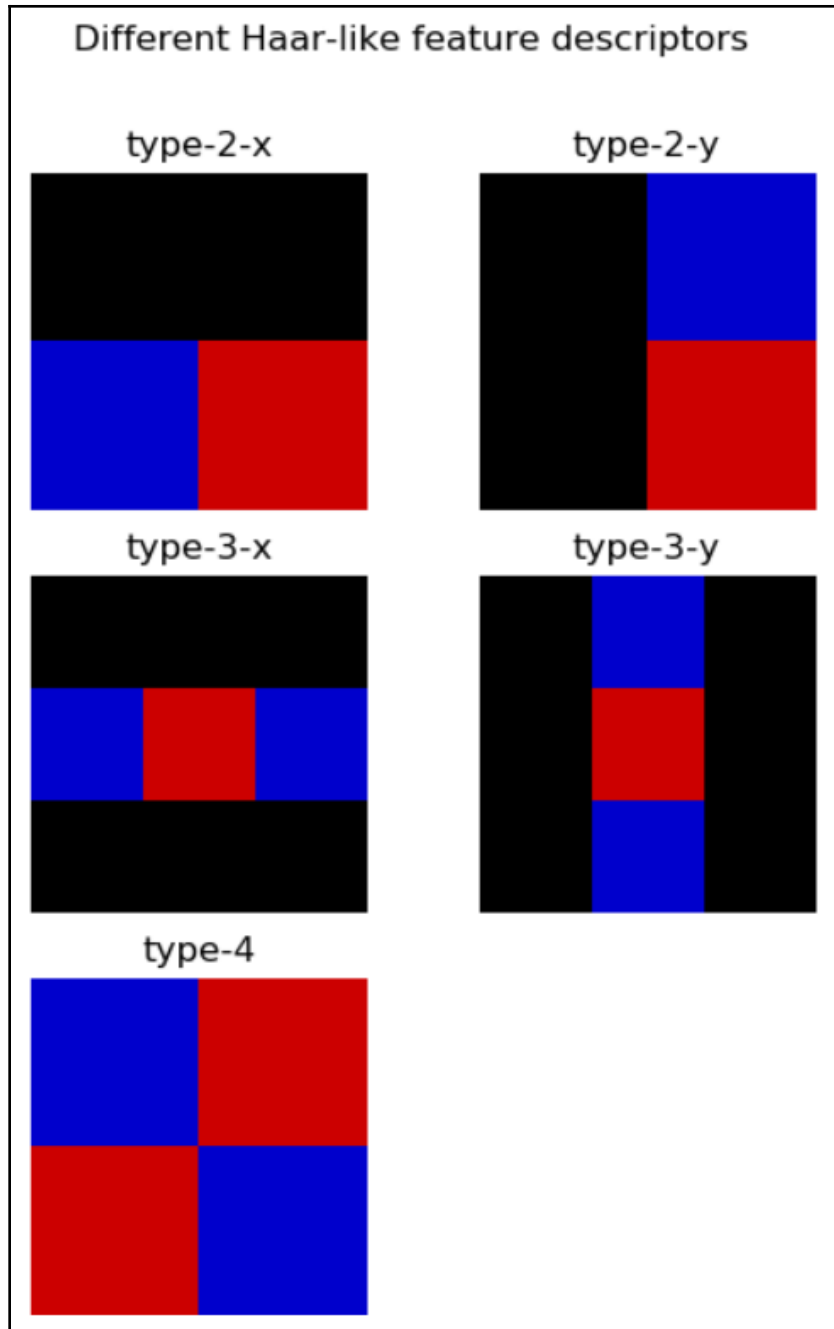
Image1 vs. Image2

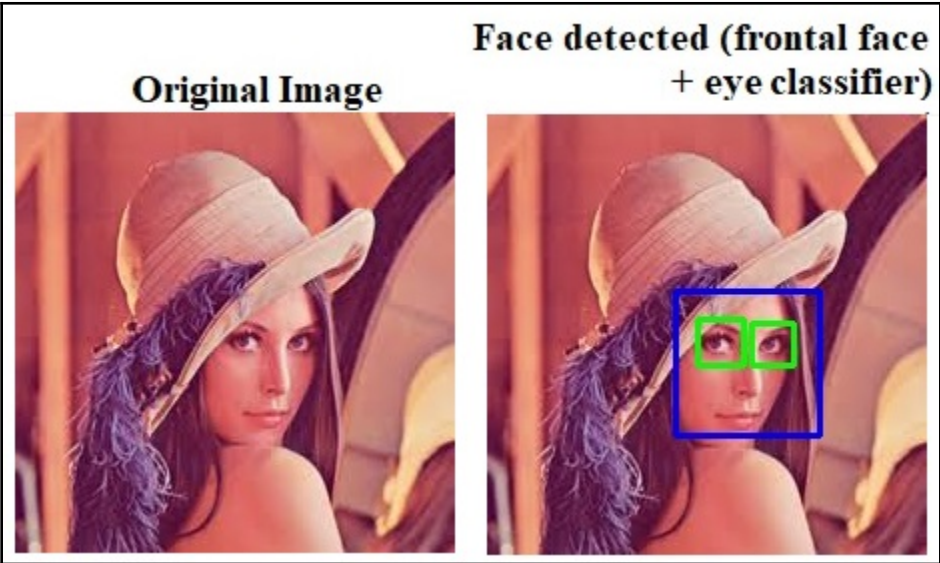


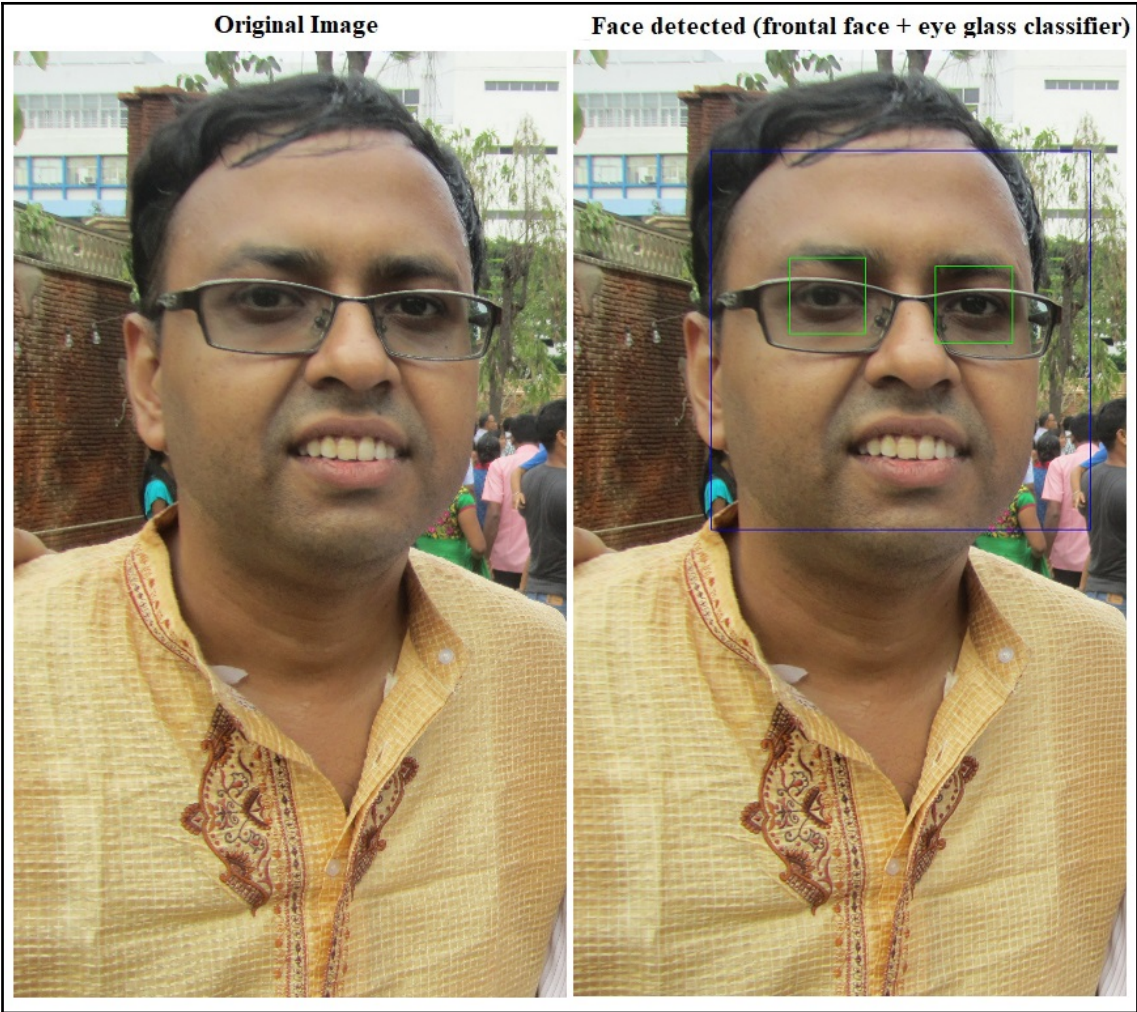




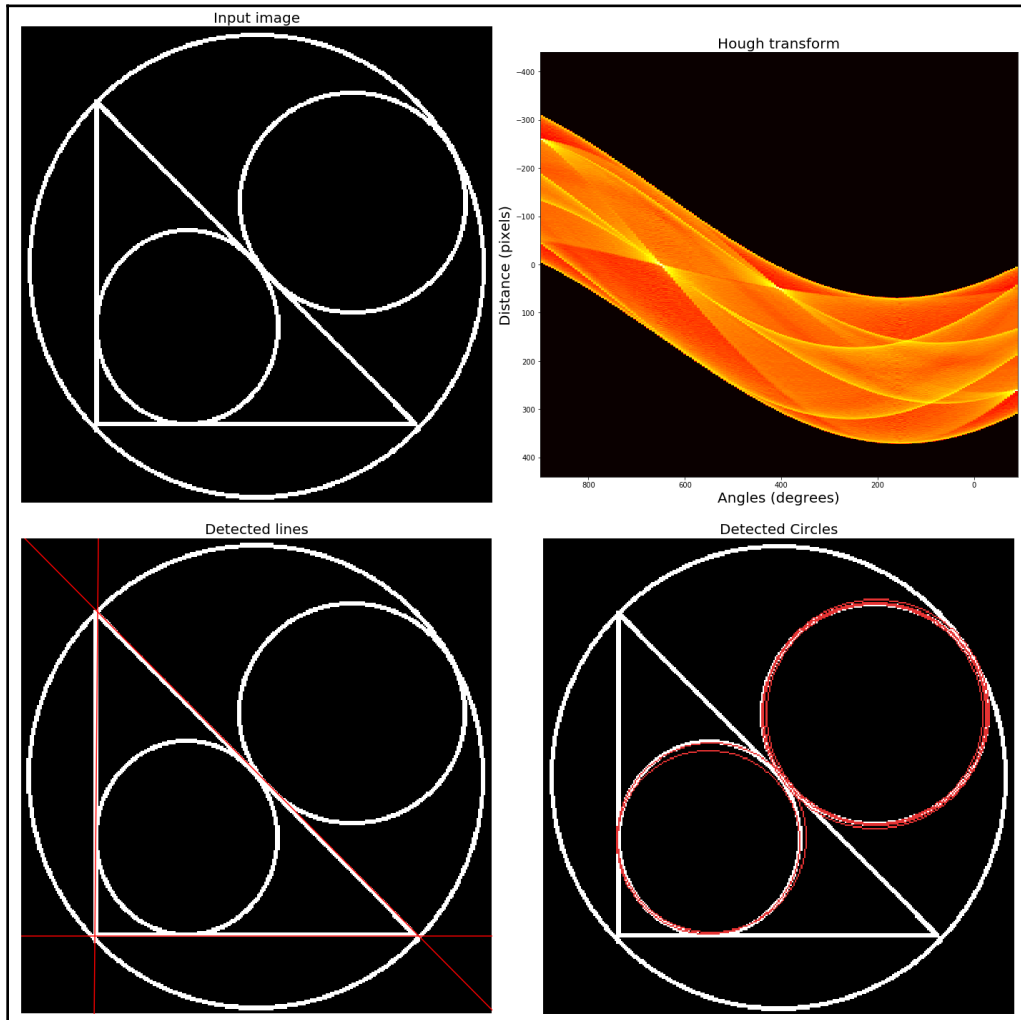


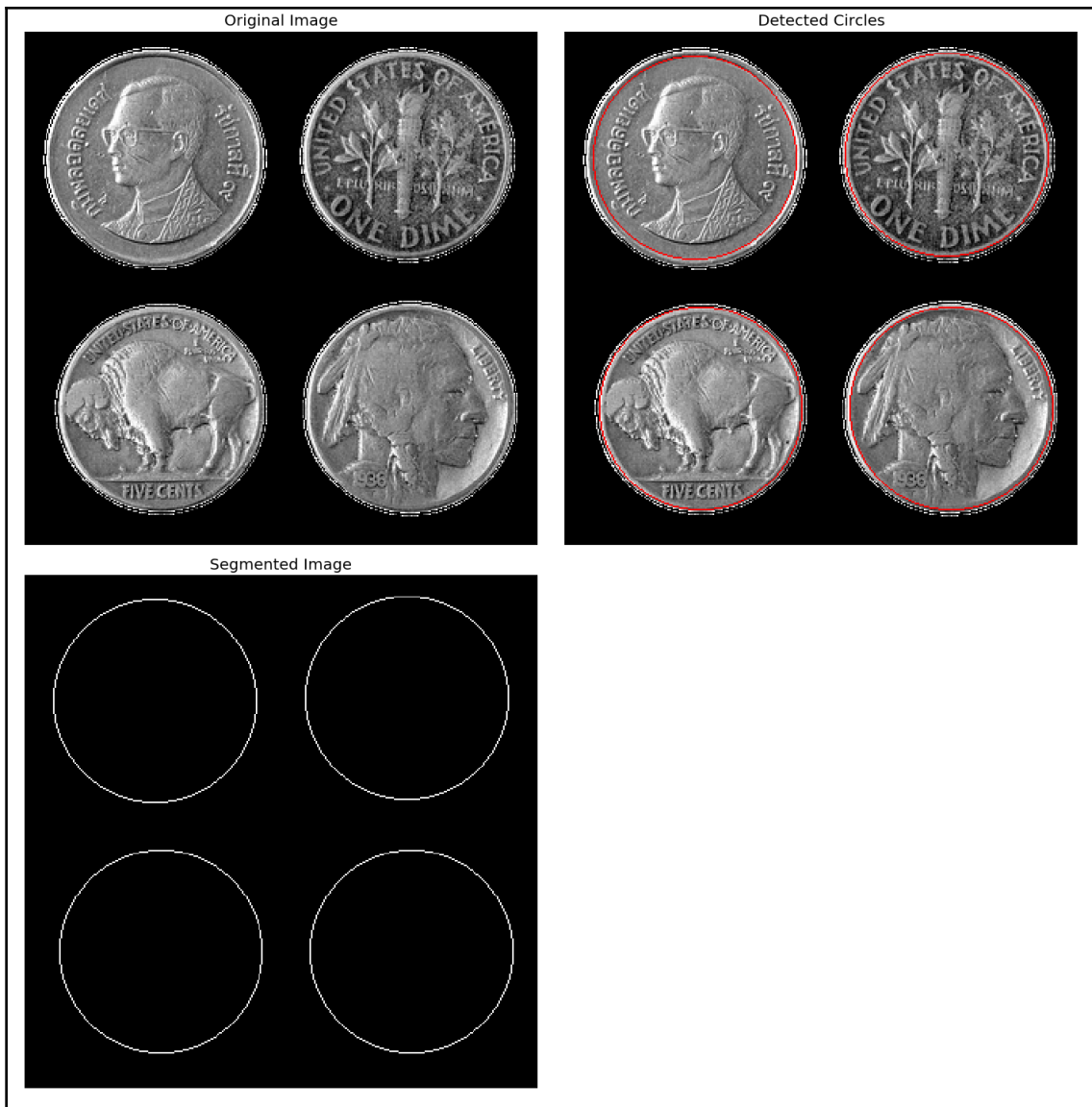


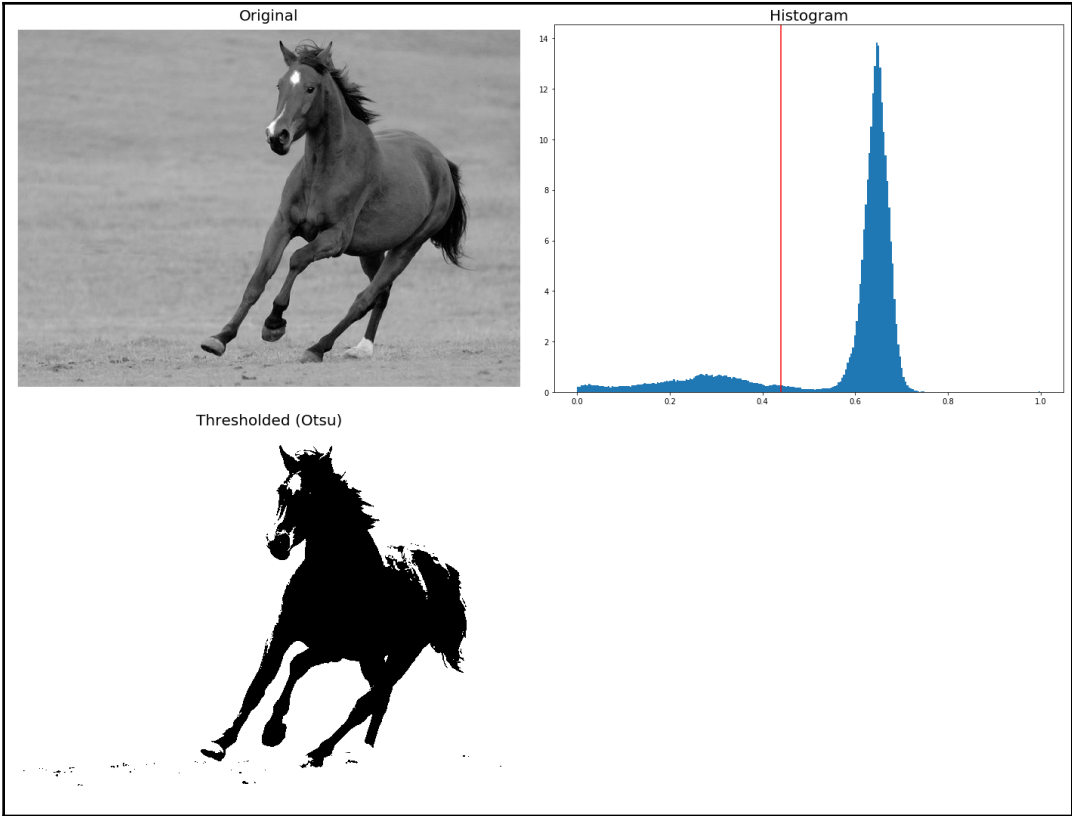


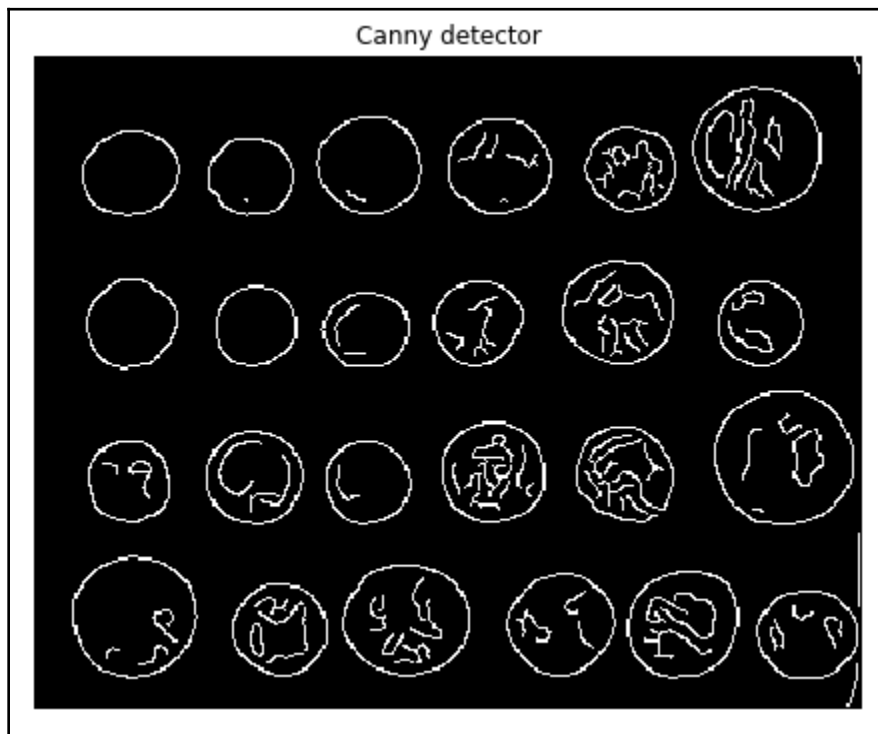
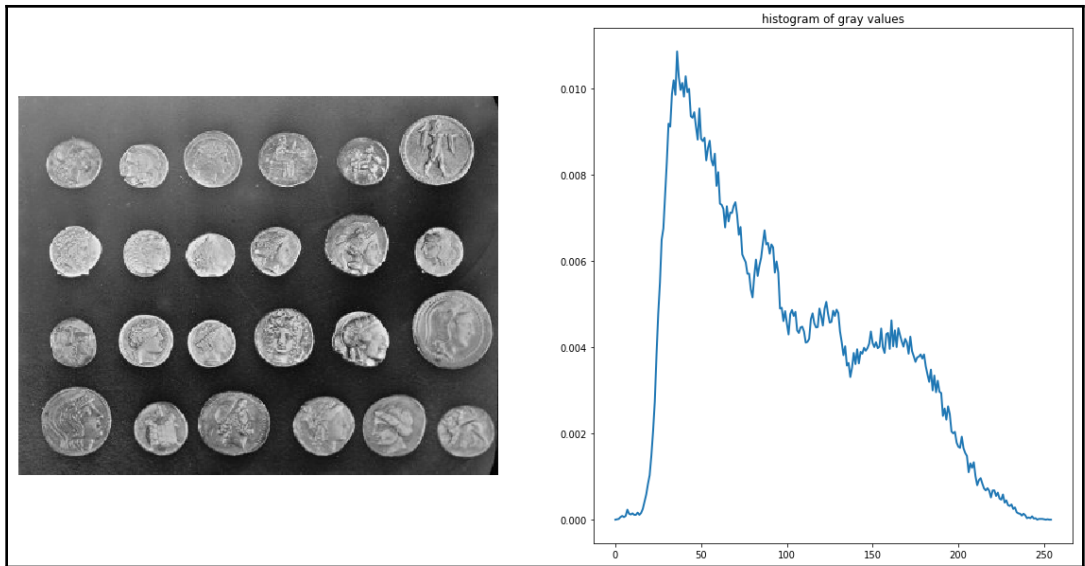


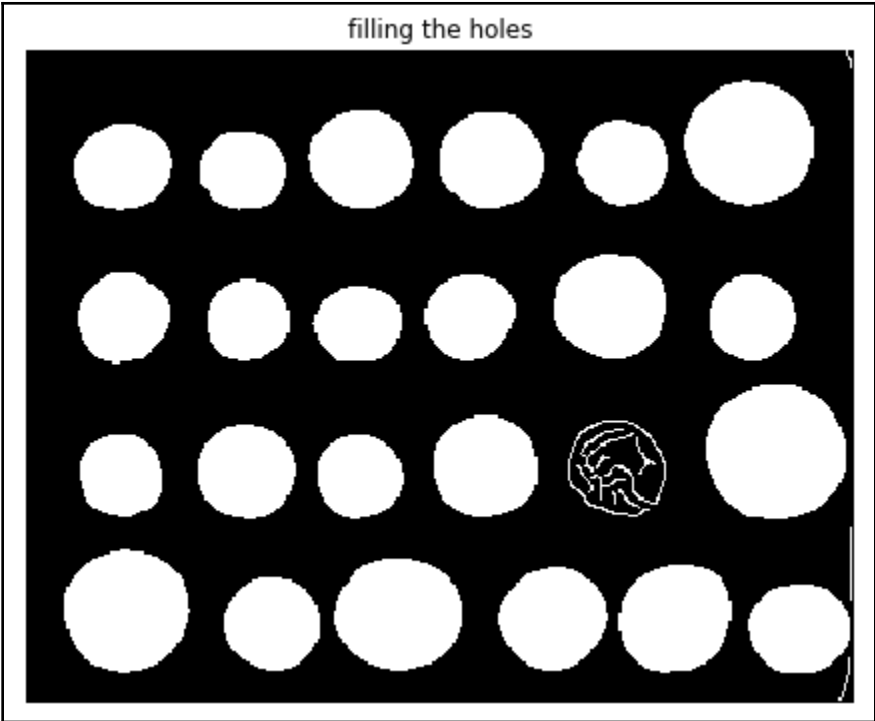
Chapter 8: Image Segmentation

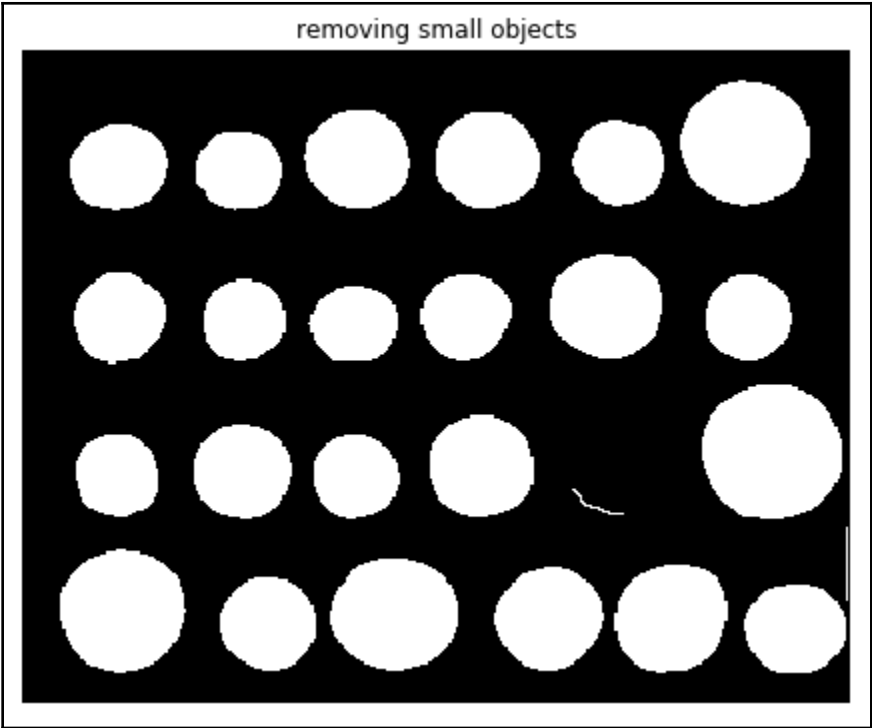


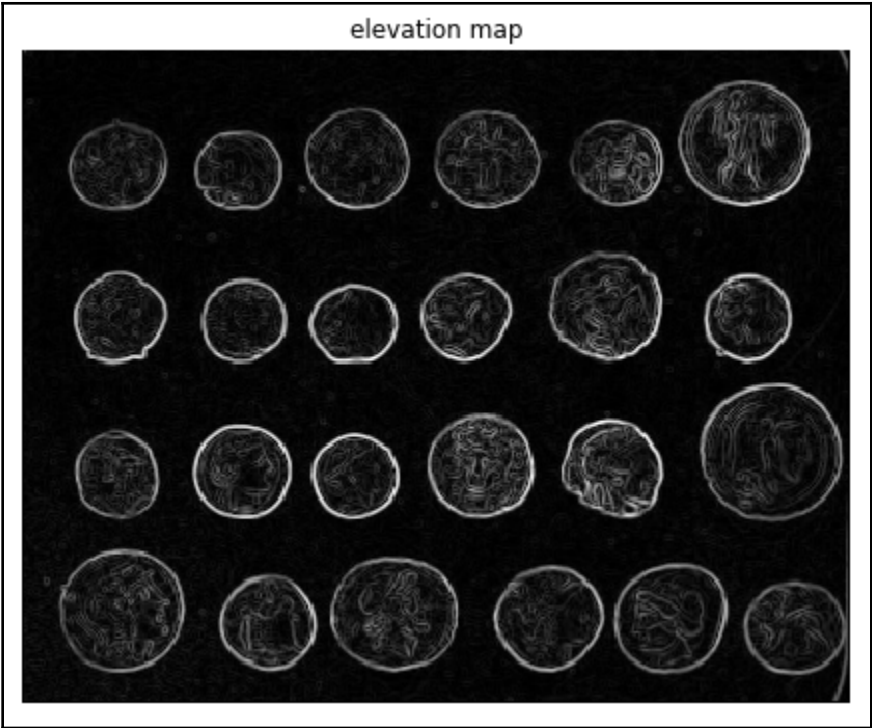


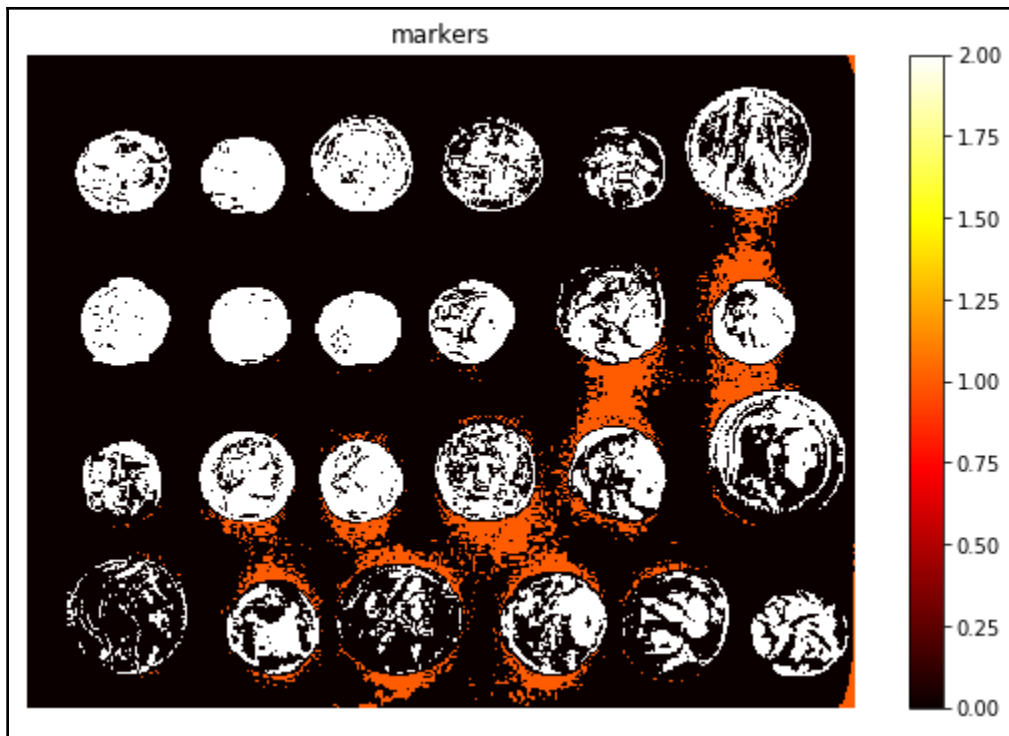


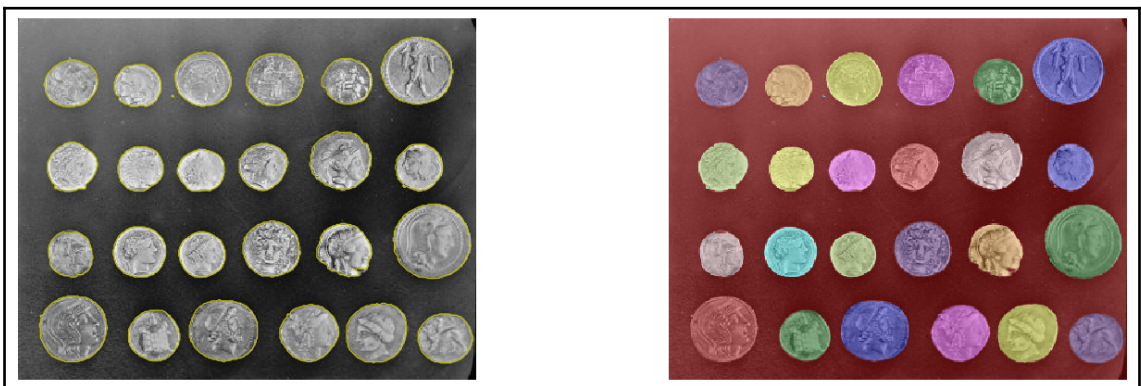
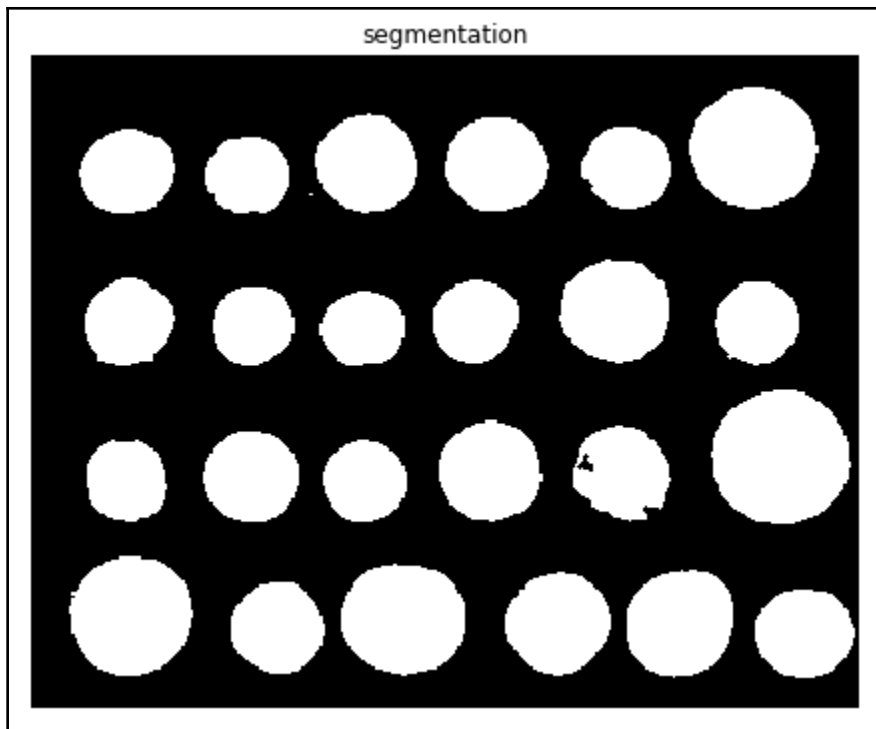


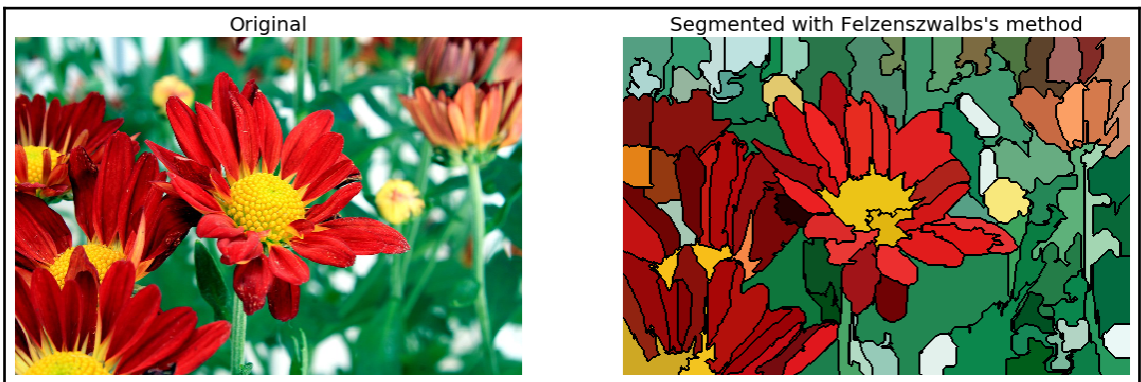
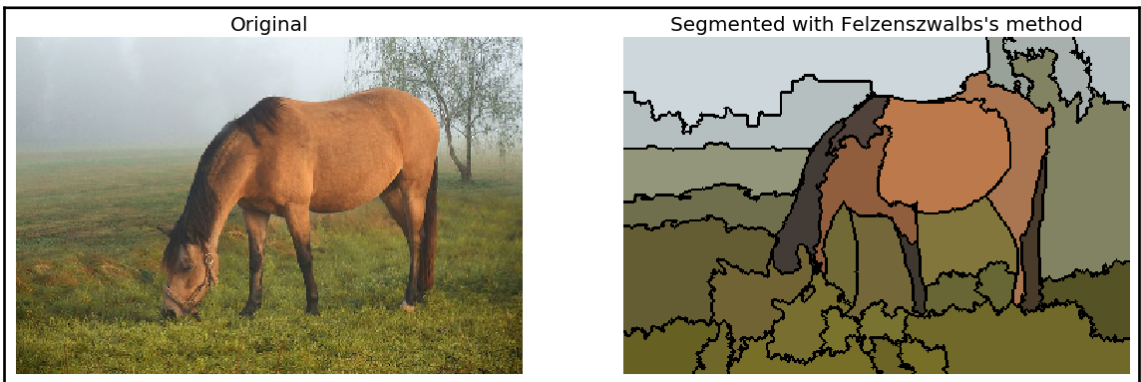
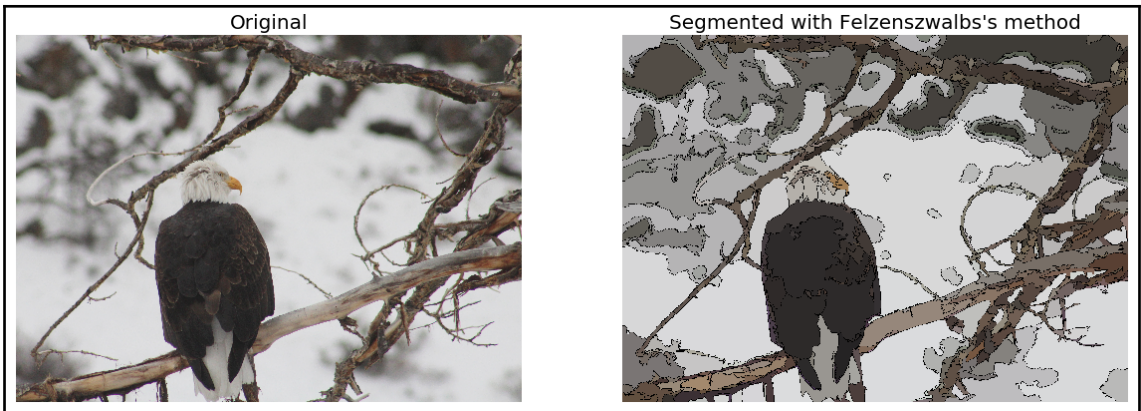


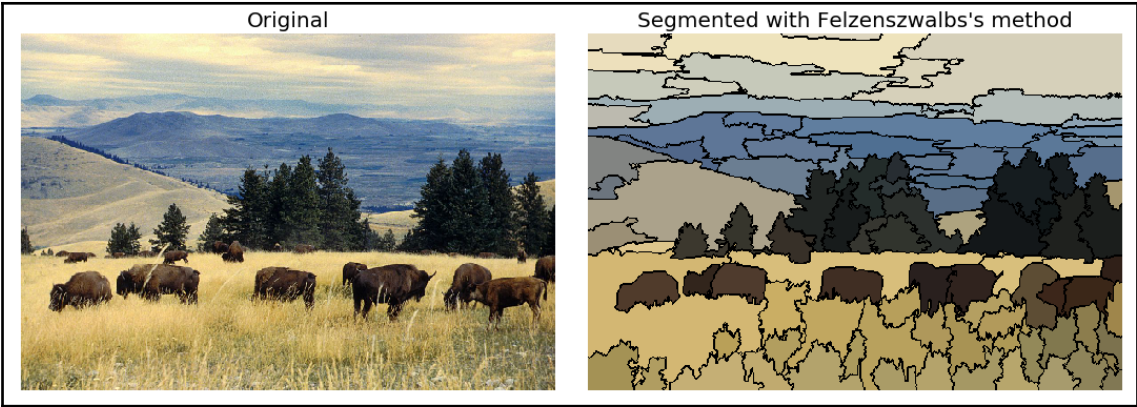


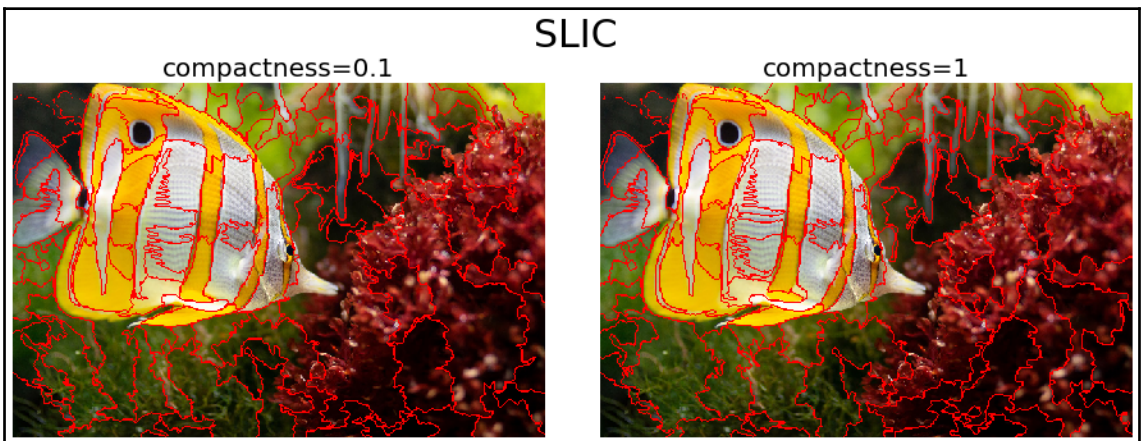
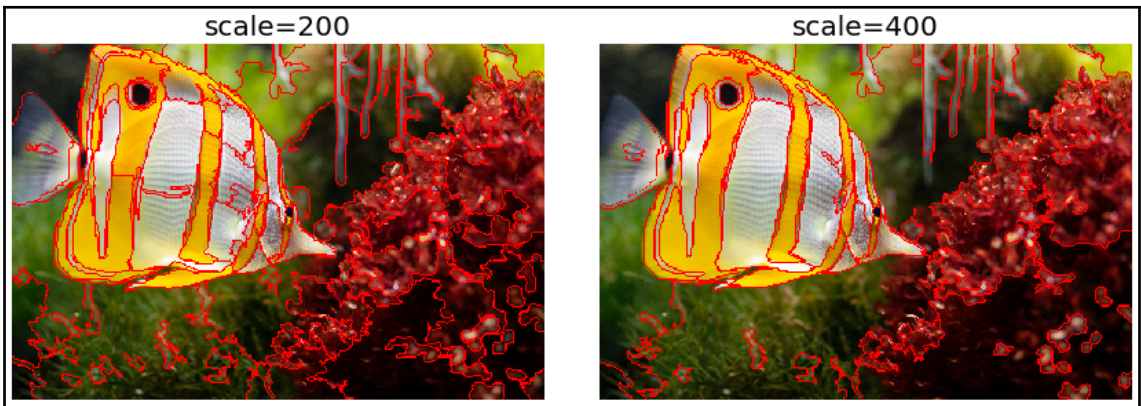


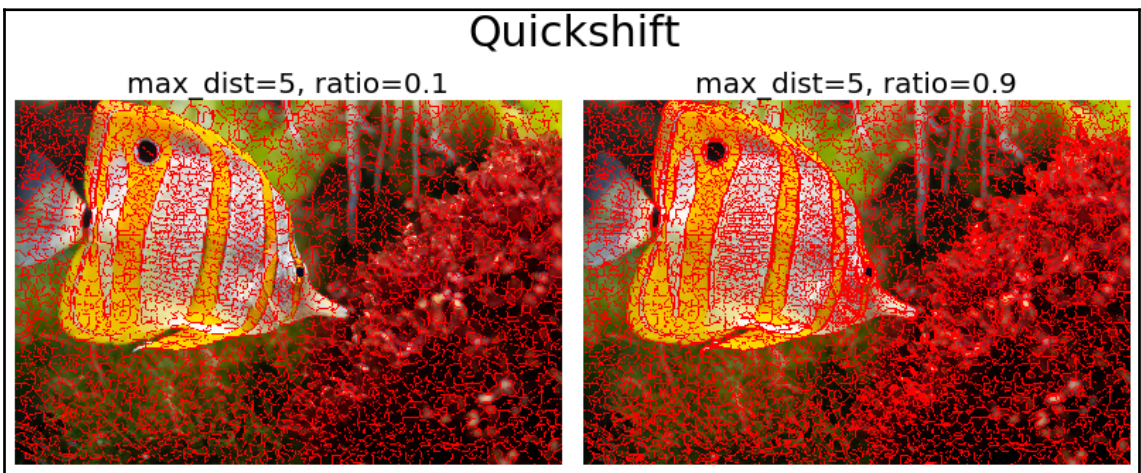
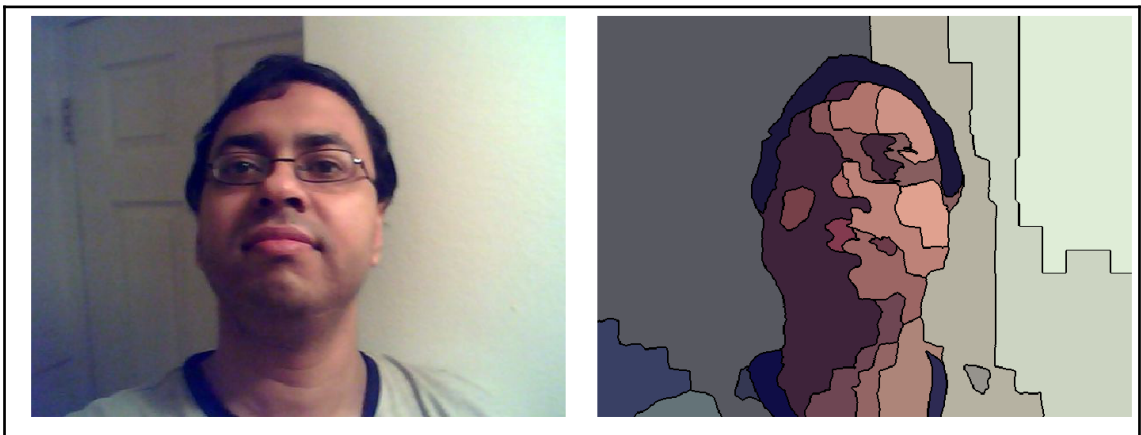
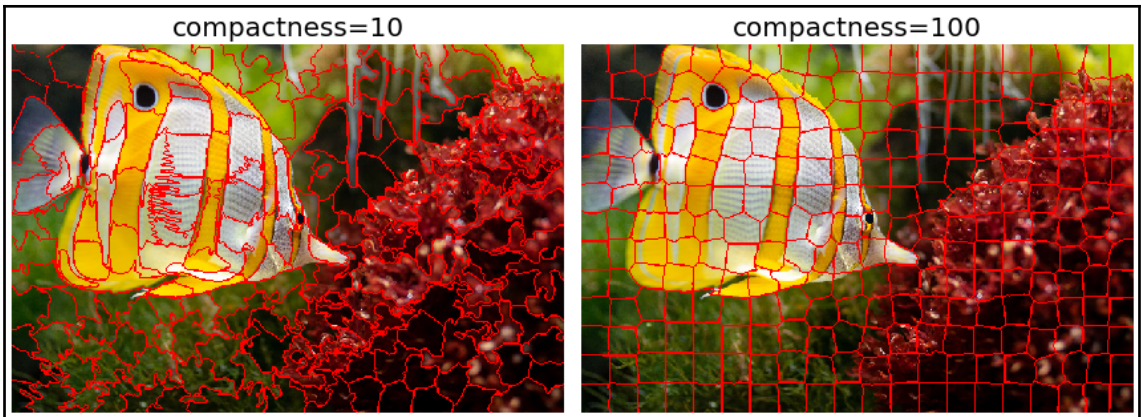


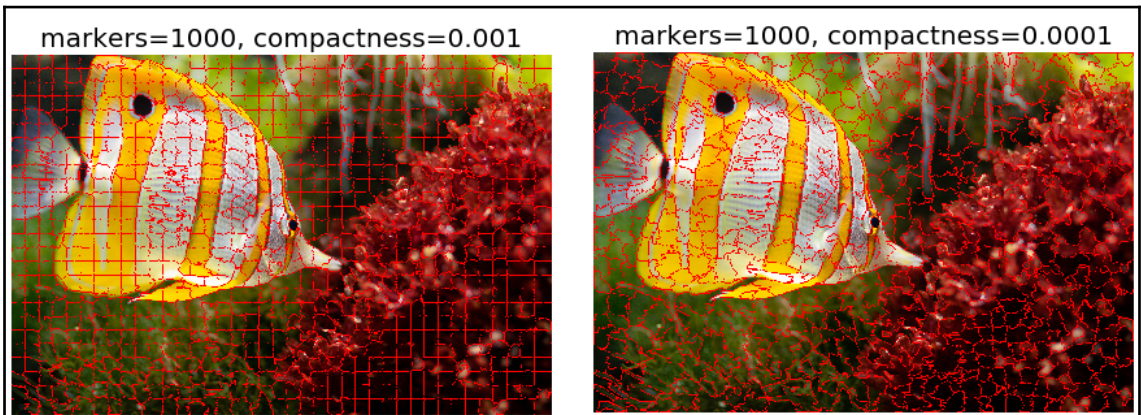
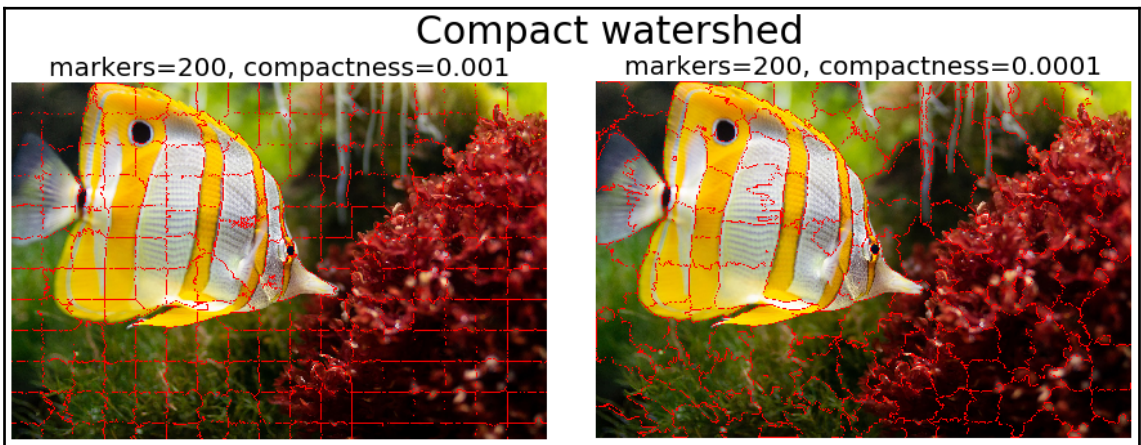
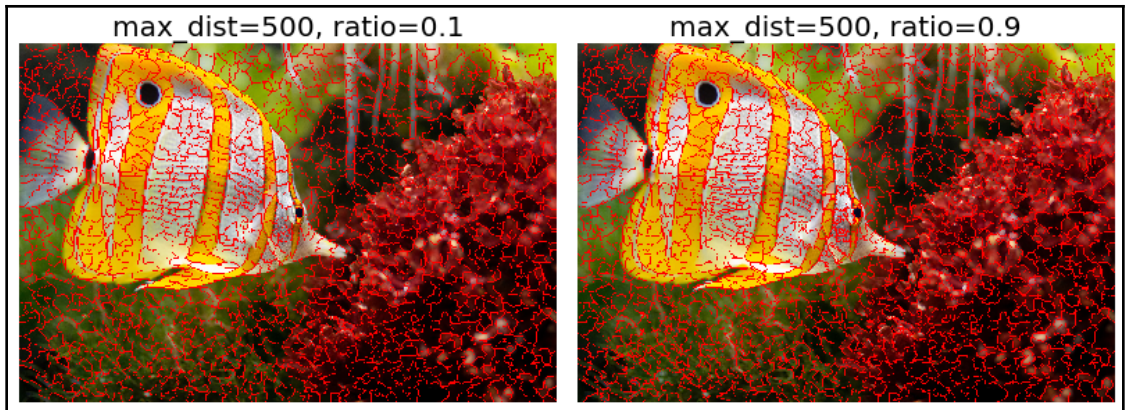


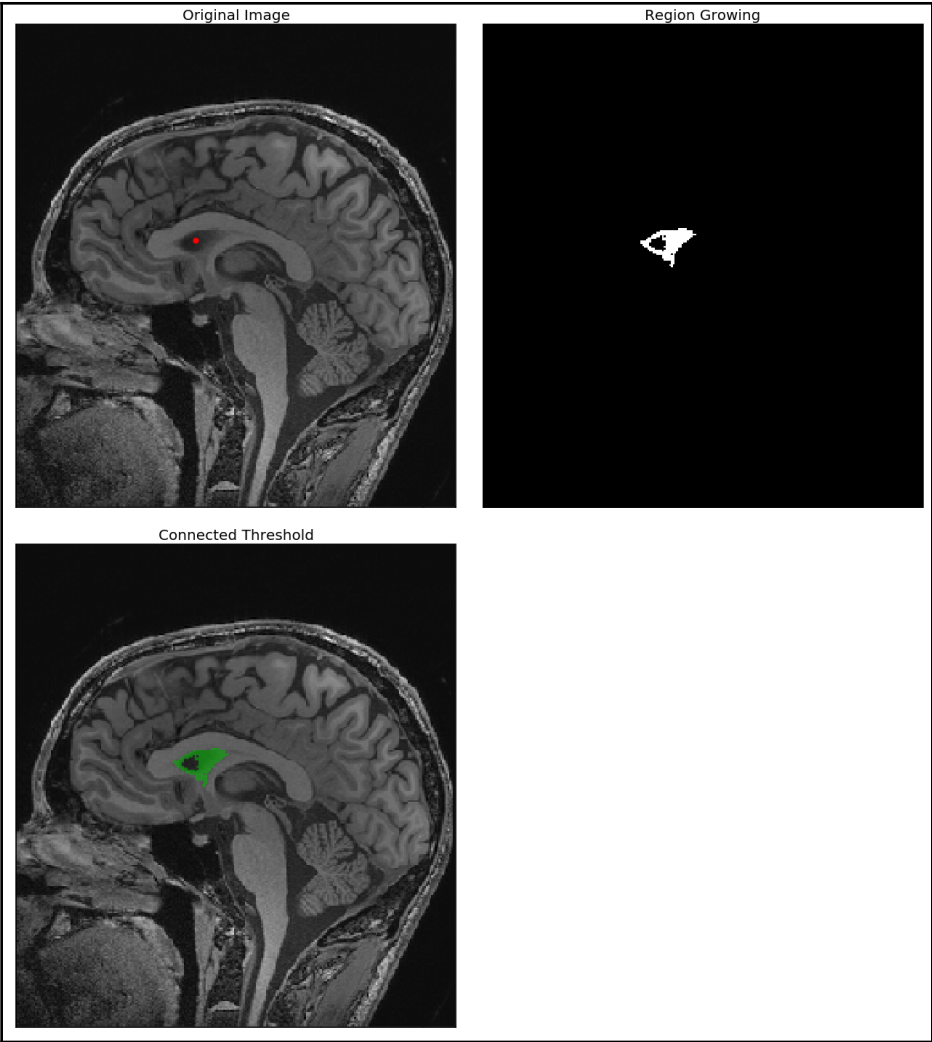


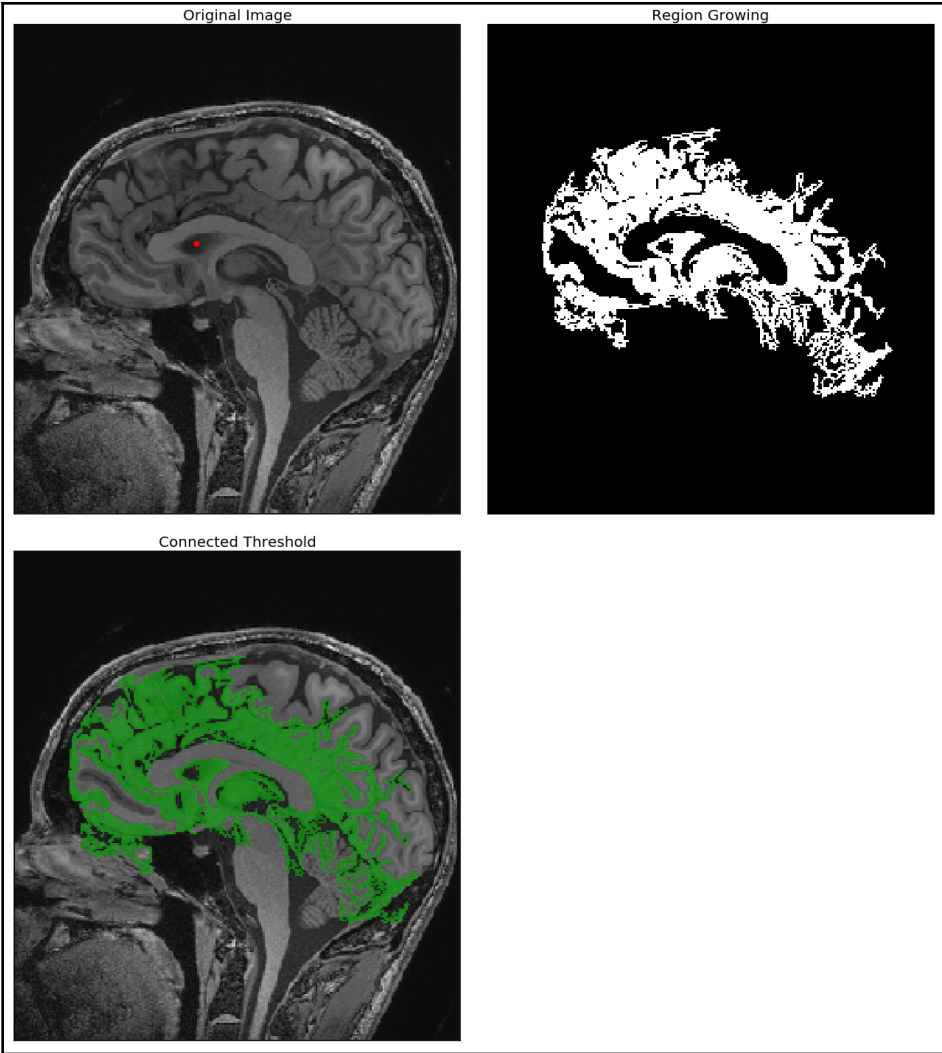


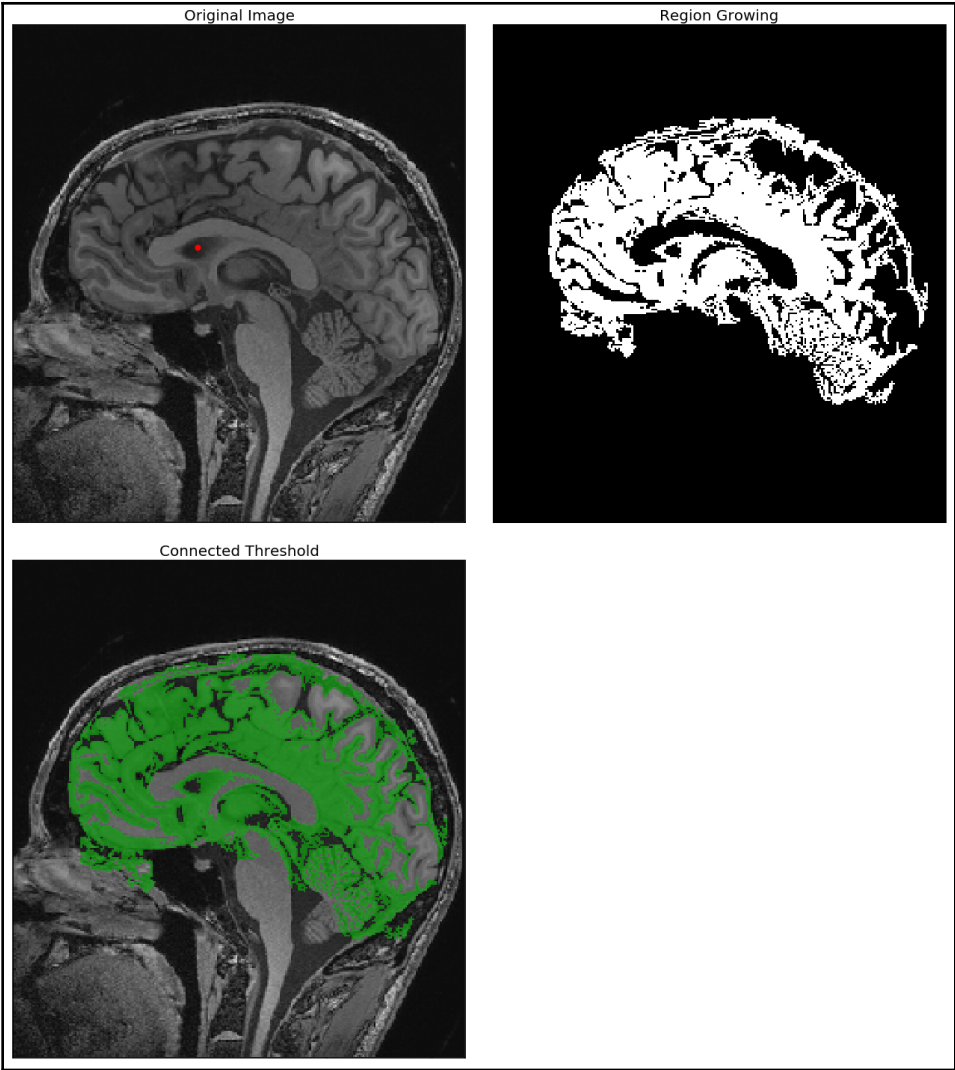


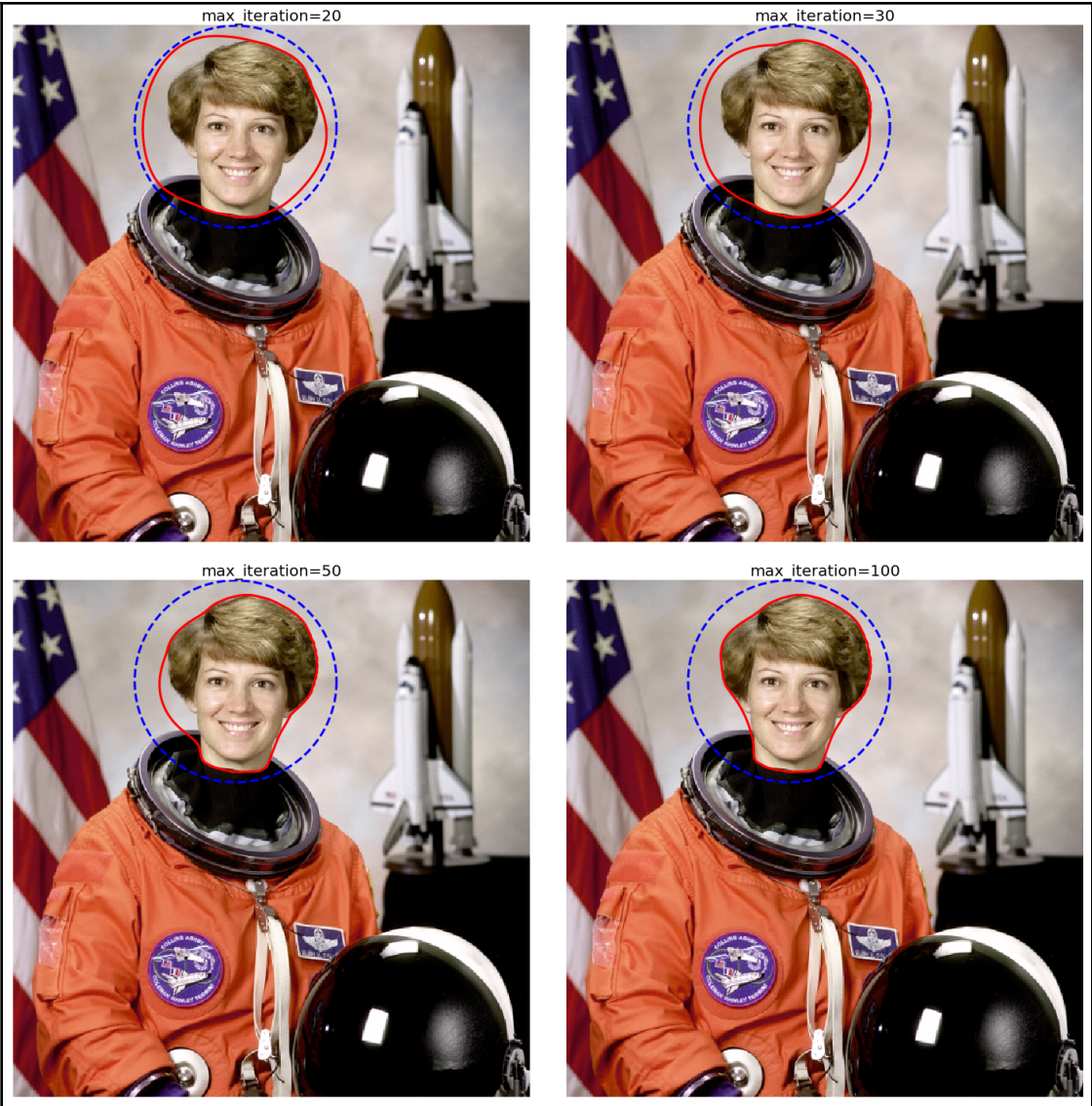








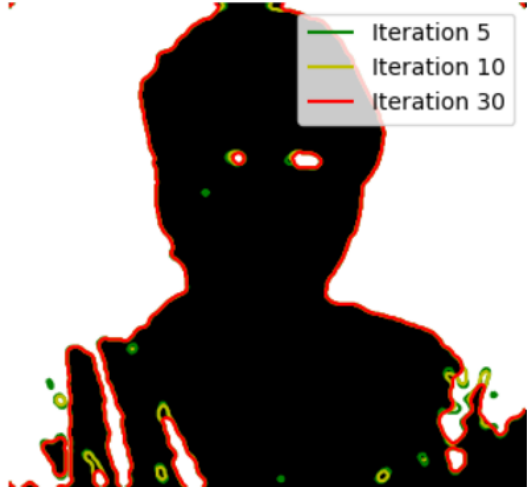




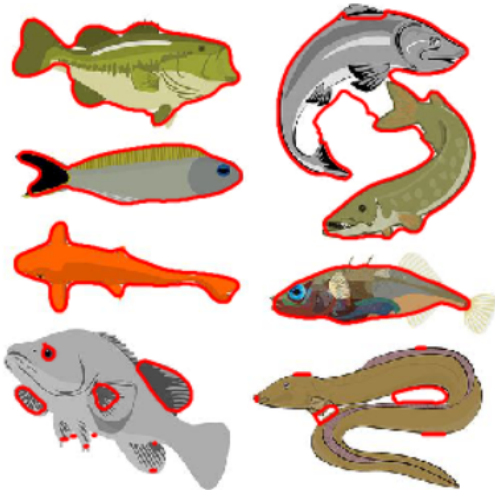
Morphological ACWE segmentation



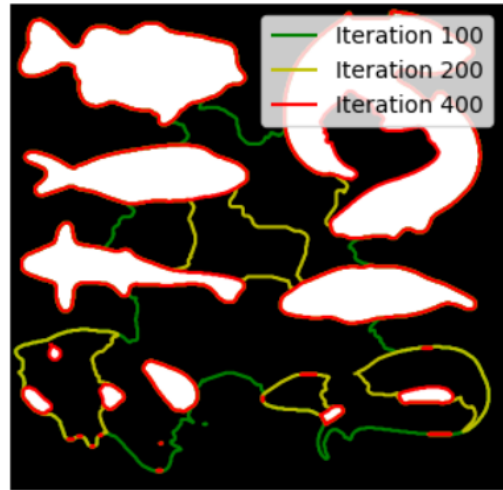
Morphological ACWE evolution



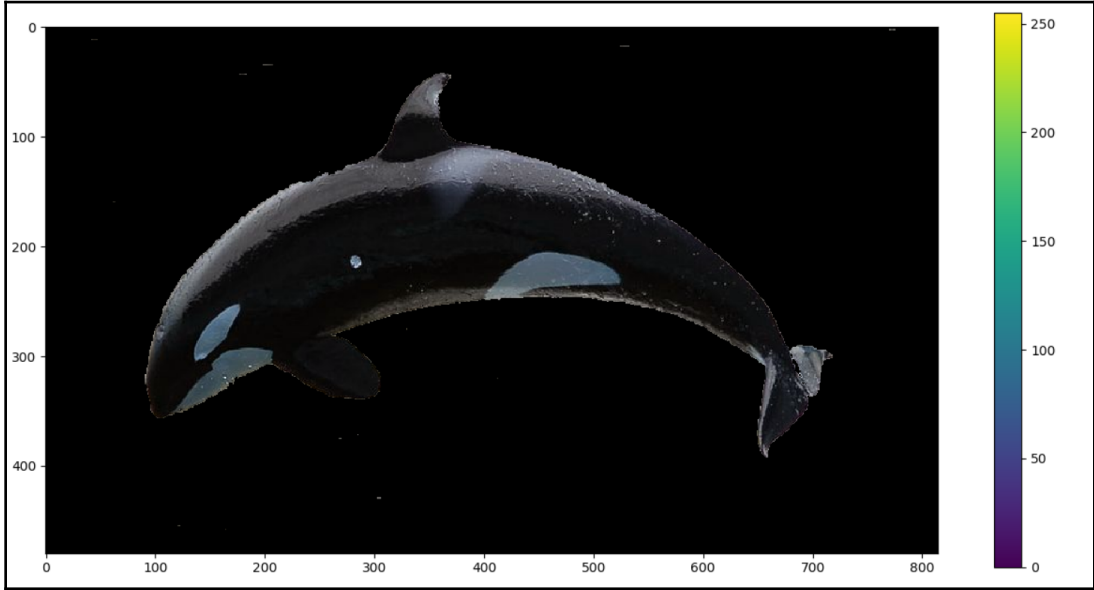
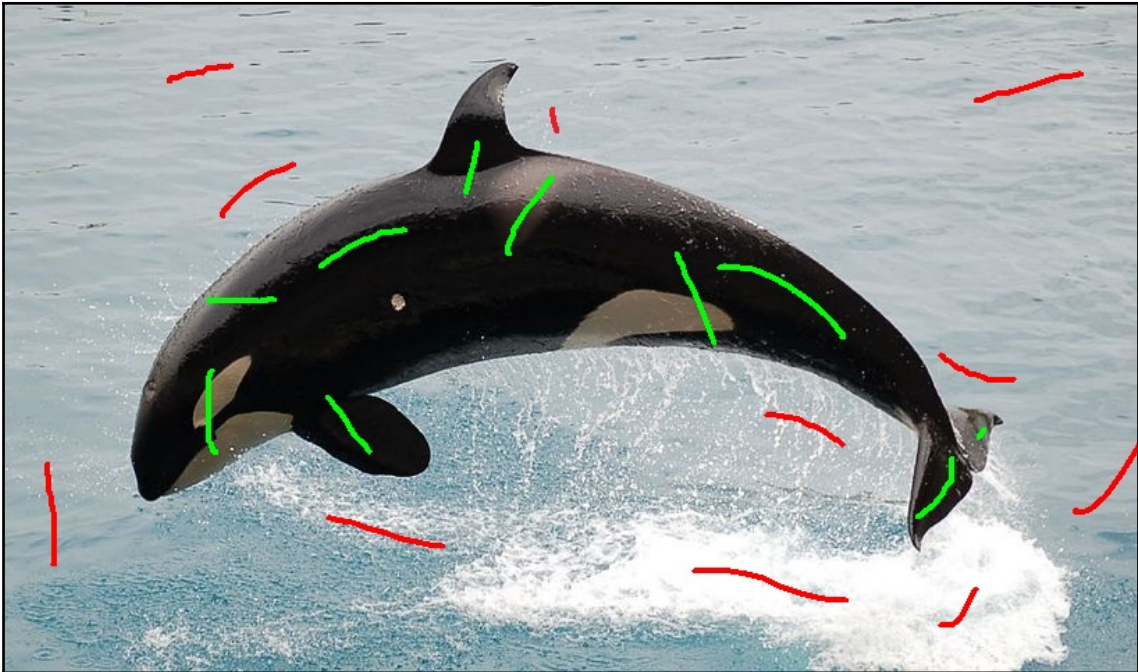
Morphological GAC segmentation



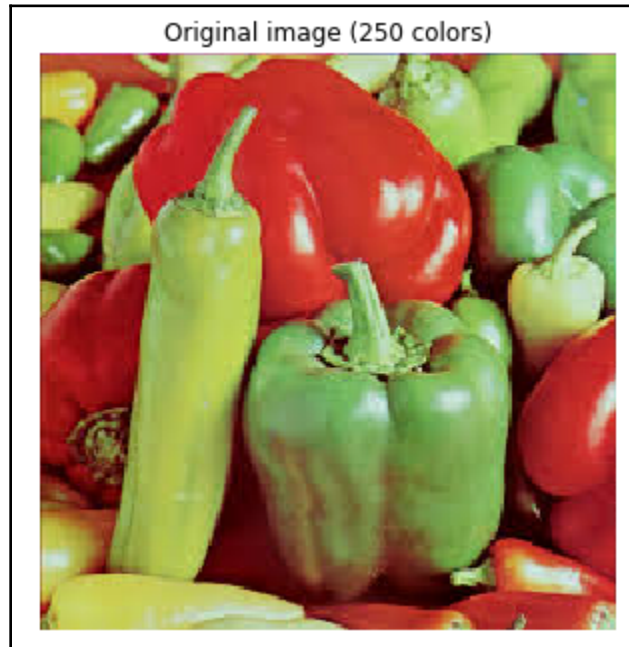
Morphological GAC evolution







Chapter 9: Classical Machine Learning Methods in Image Processing



Quantized image (64 colors, K-Means)



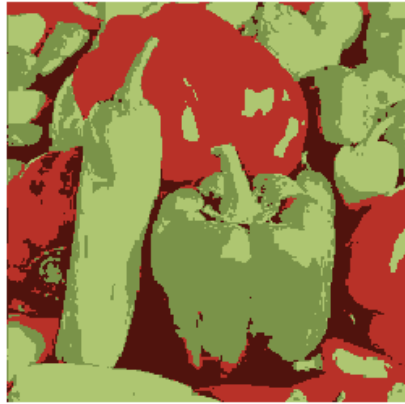
Quantized image (32 colors, K-Means)



Quantized image (16 colors, K-Means)



Quantized image (4 colors, K-Means)



Quantized image (64 colors, Random)



Quantized image (32 colors, Random)

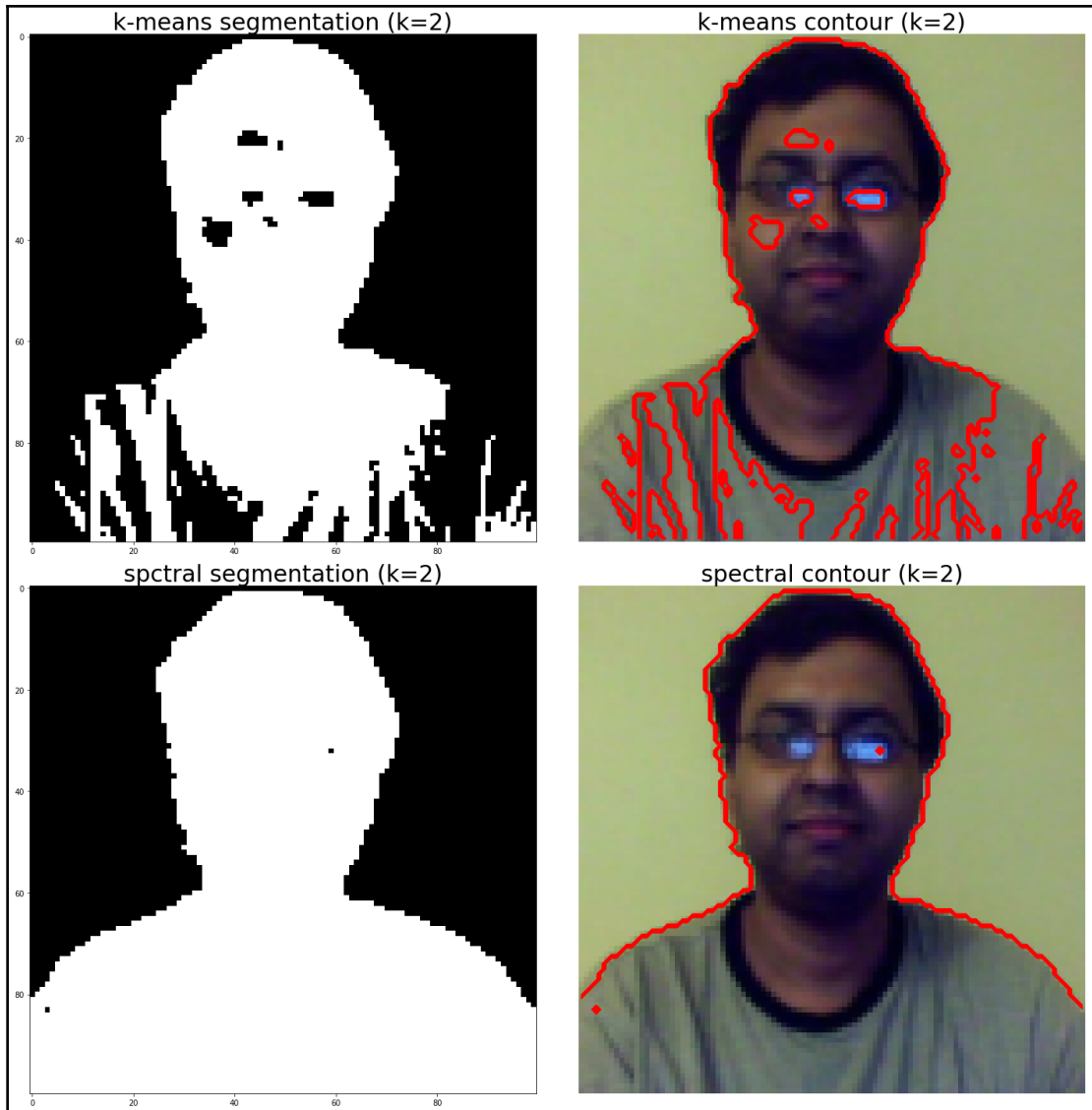


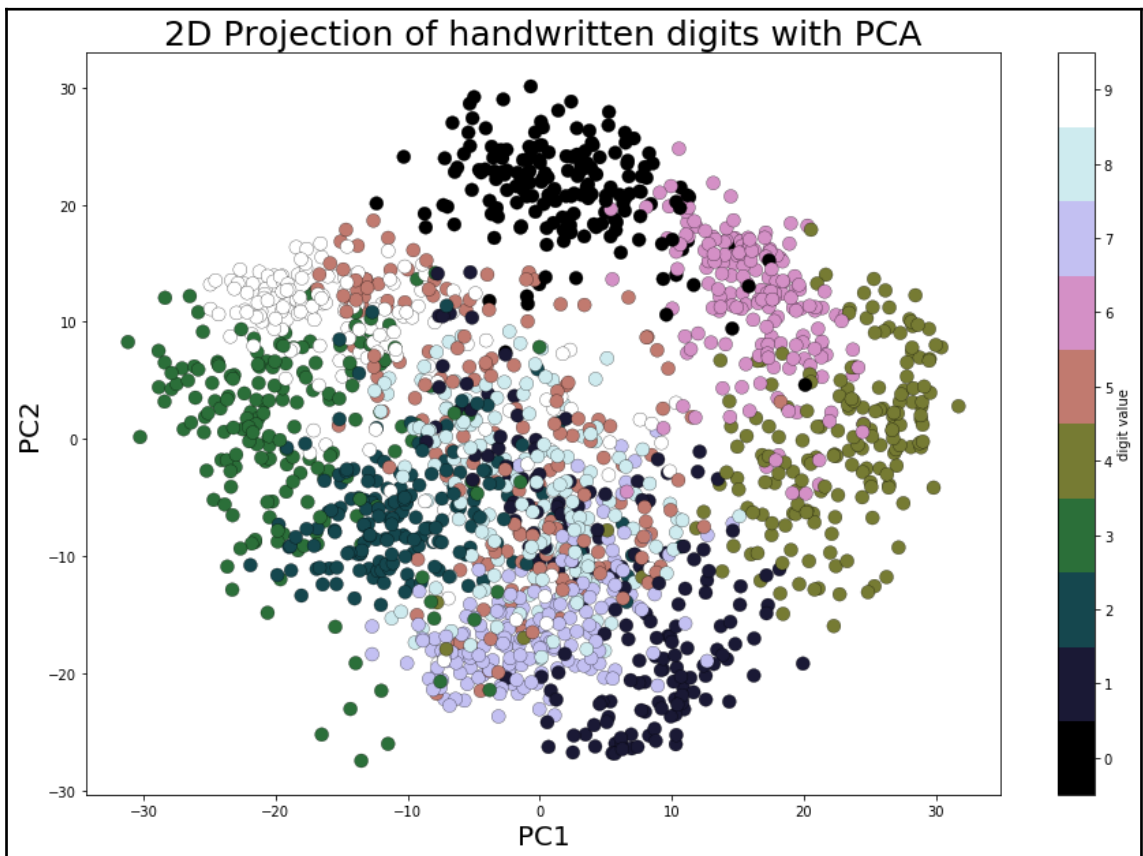
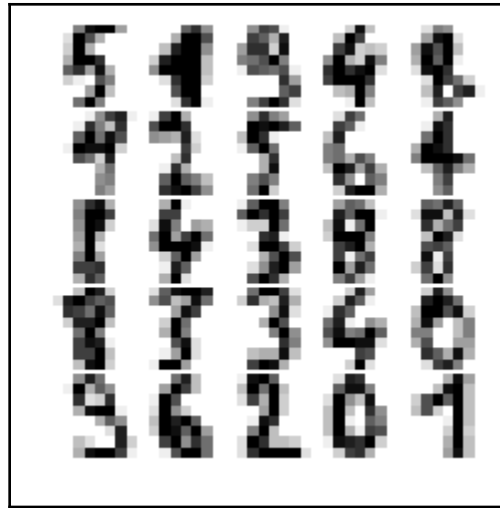
Quantized image (16 colors, Random)

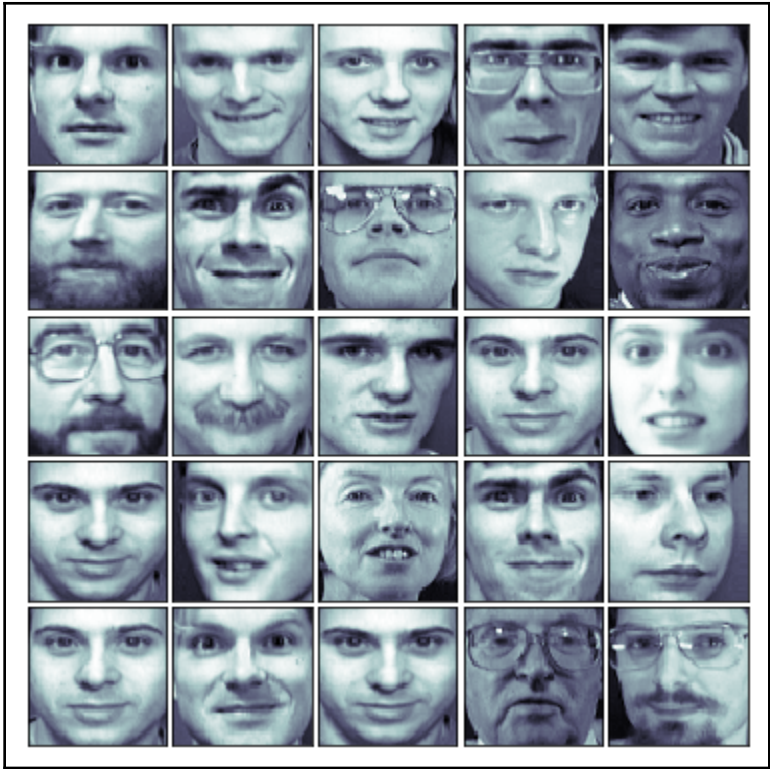


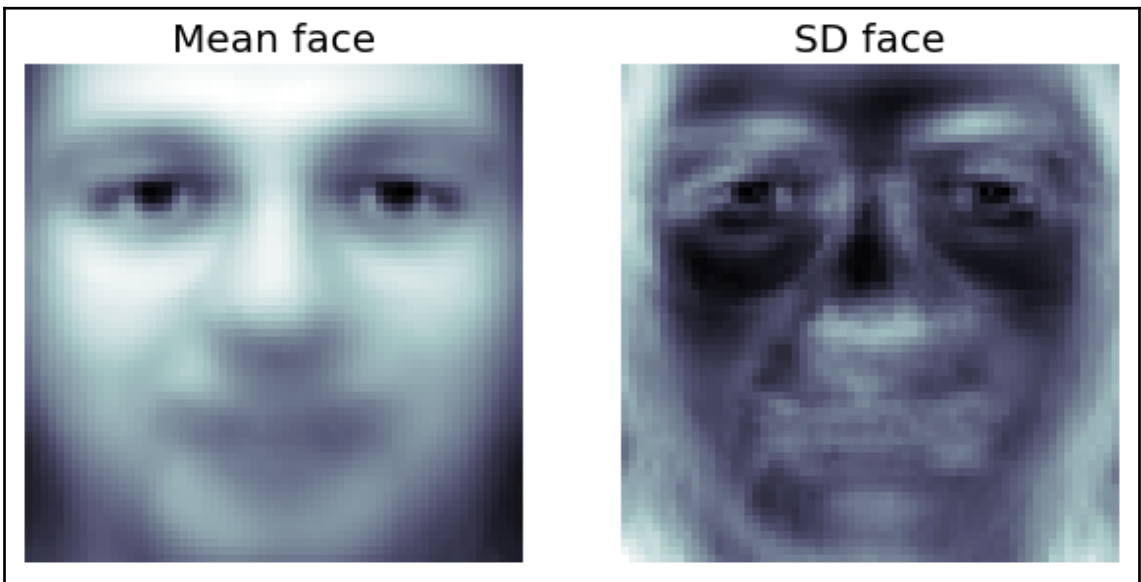
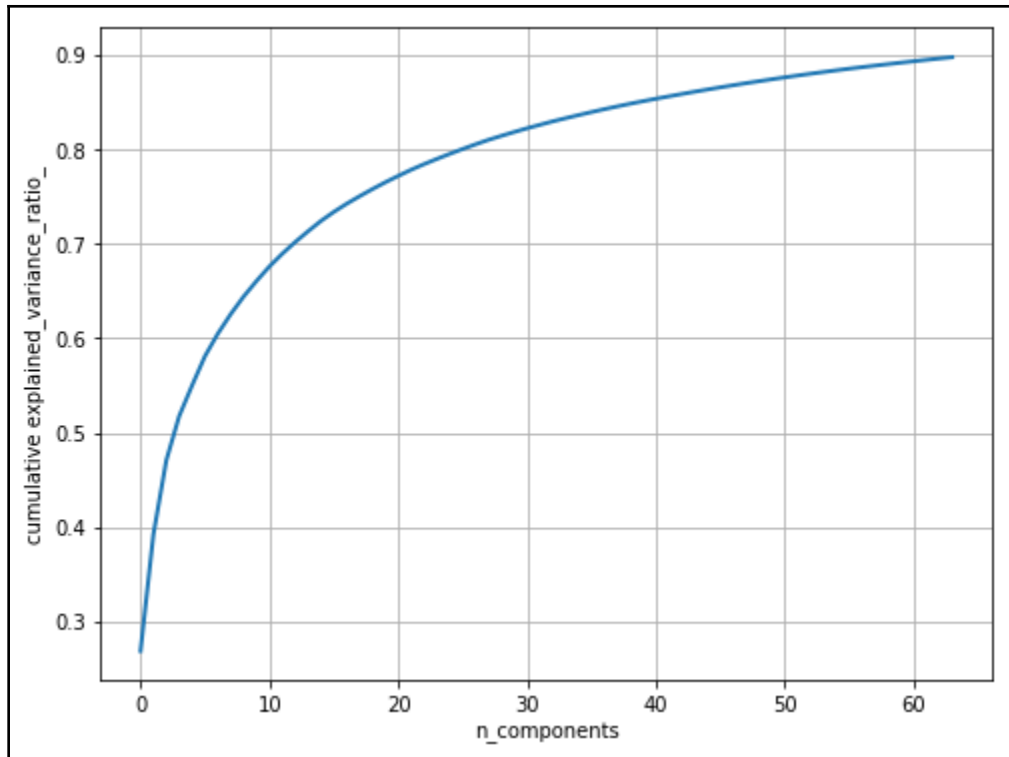
Quantized image (4 colors, Random)

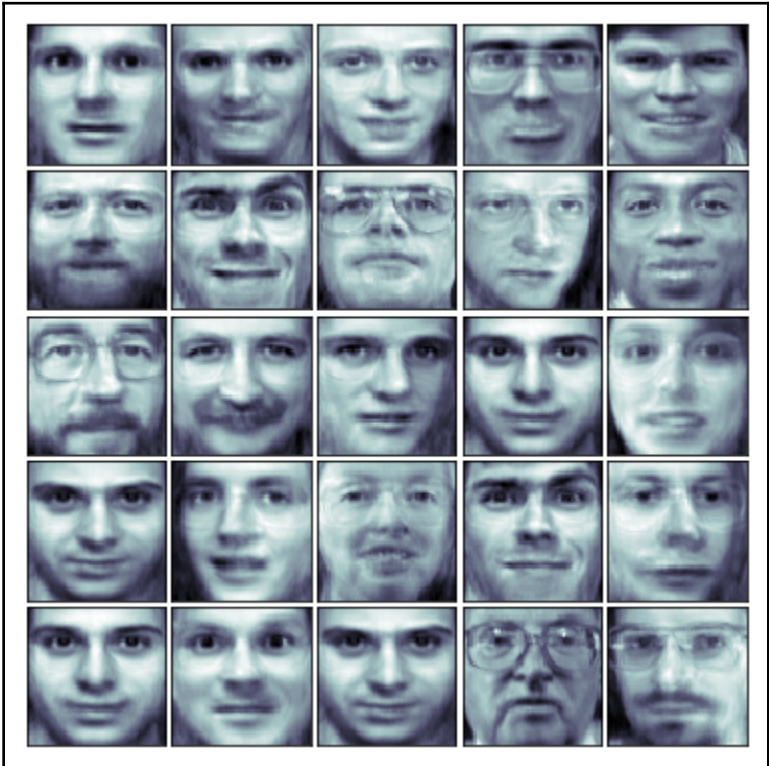
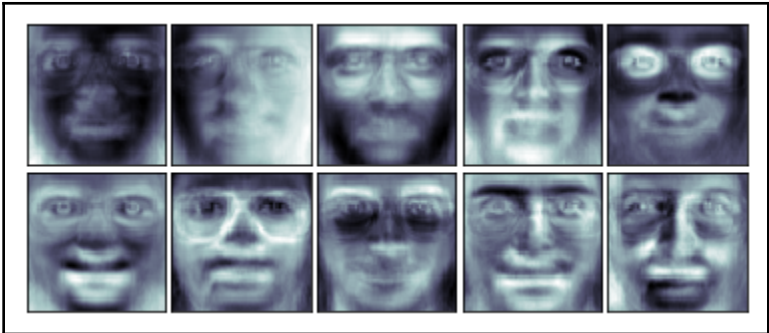


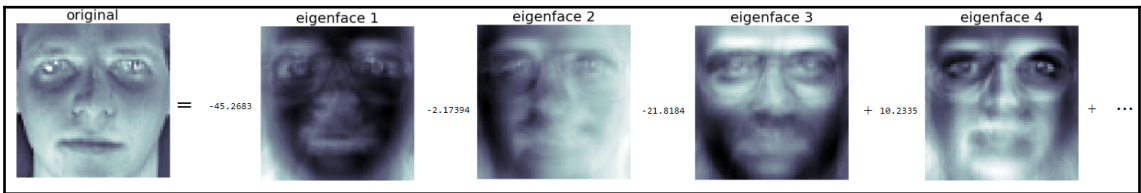
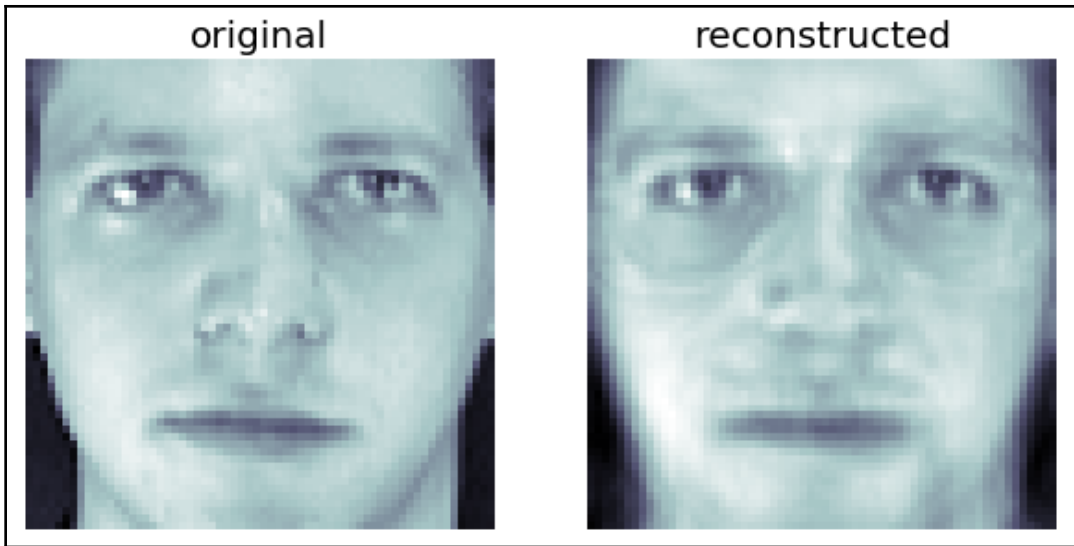


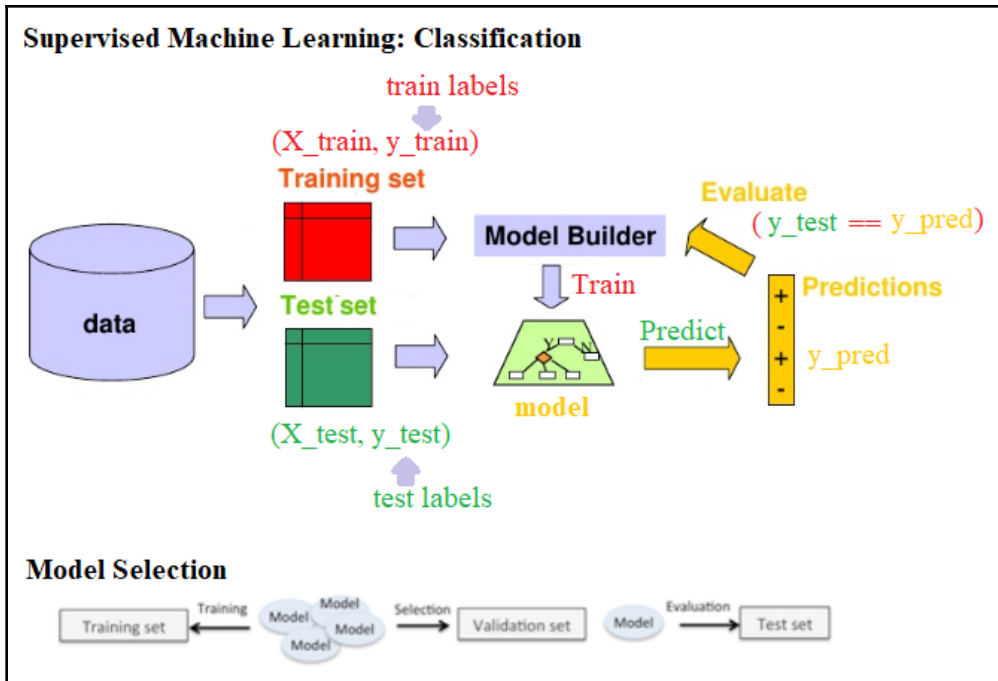


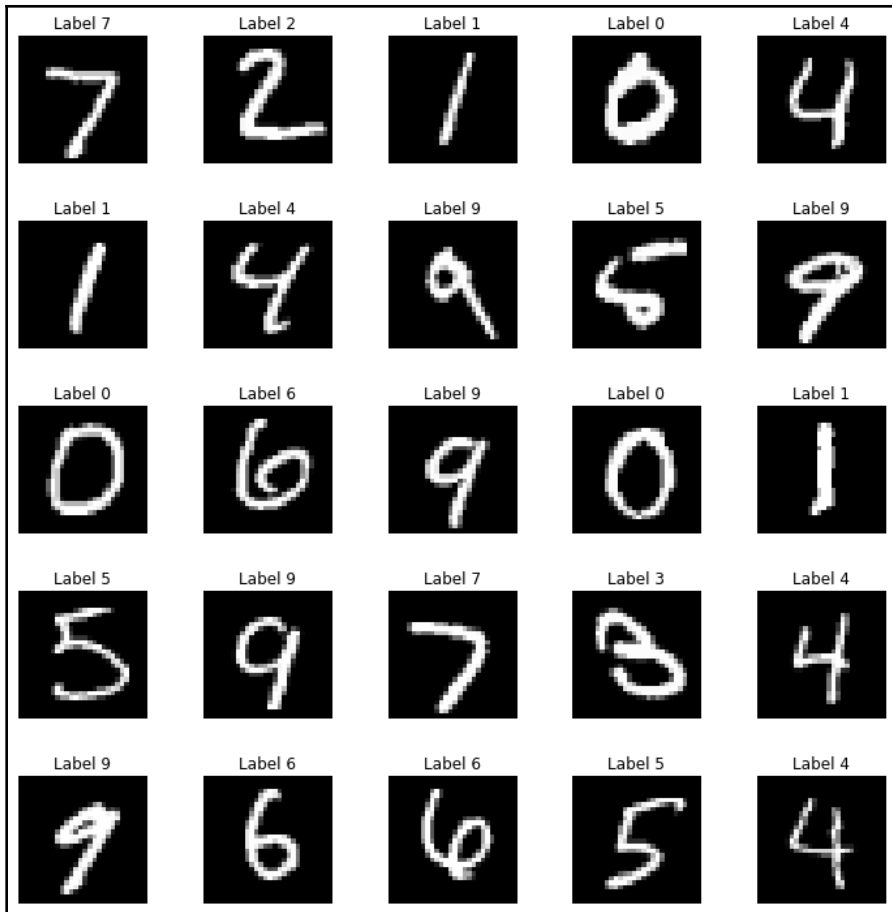


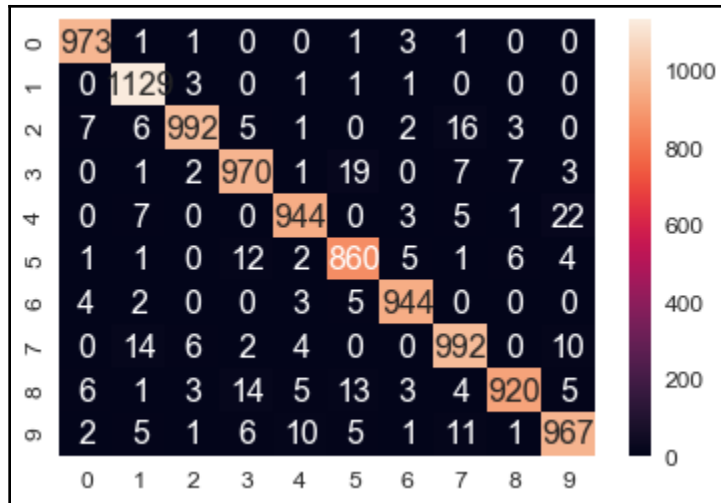






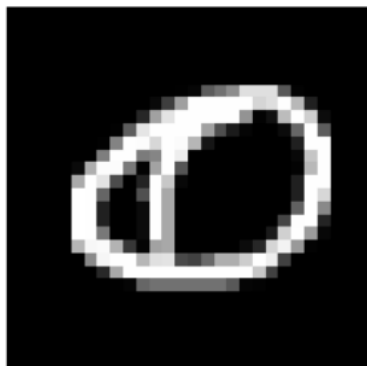




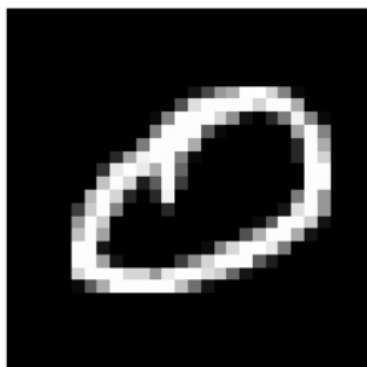


Success

test image

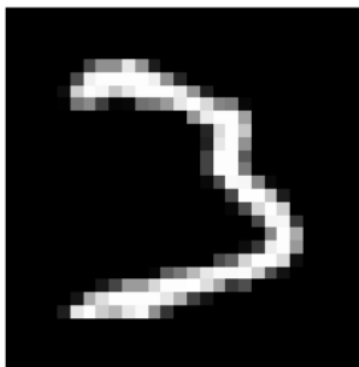


corresponding nearest neighbor image

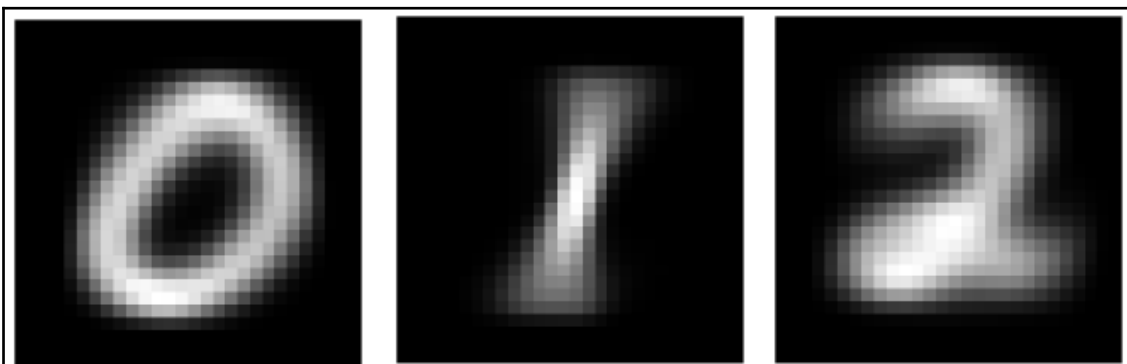


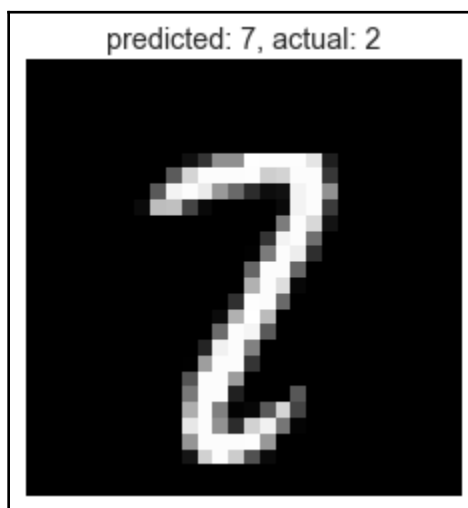
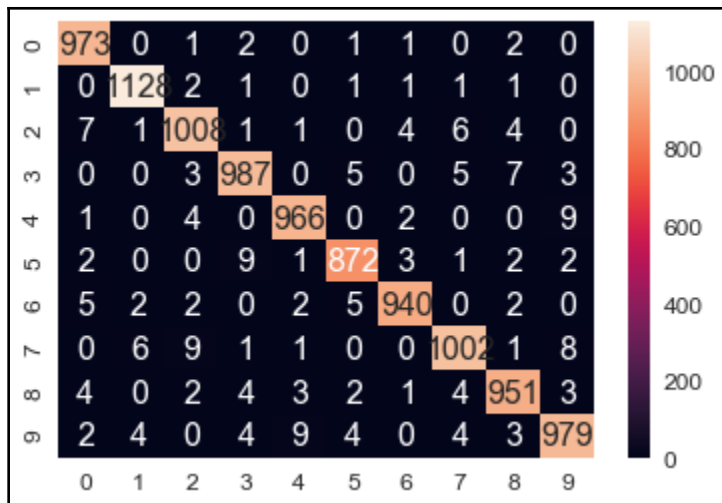
Failure

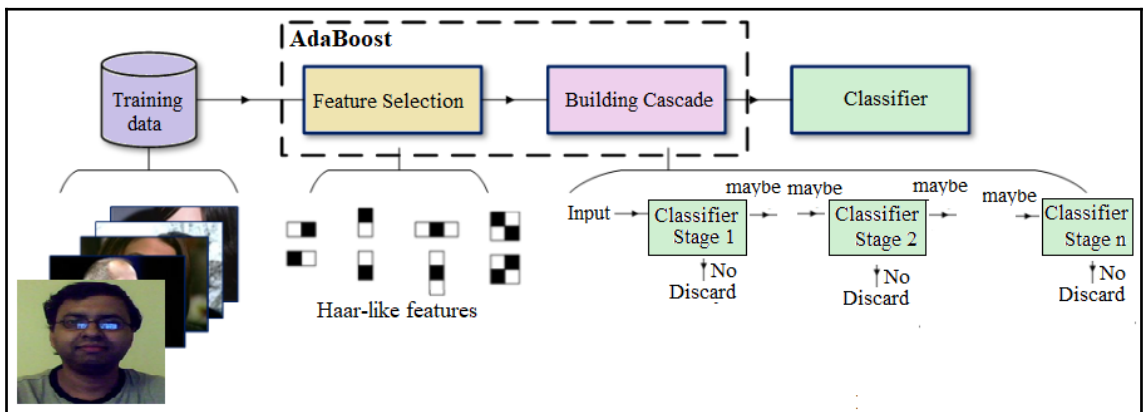
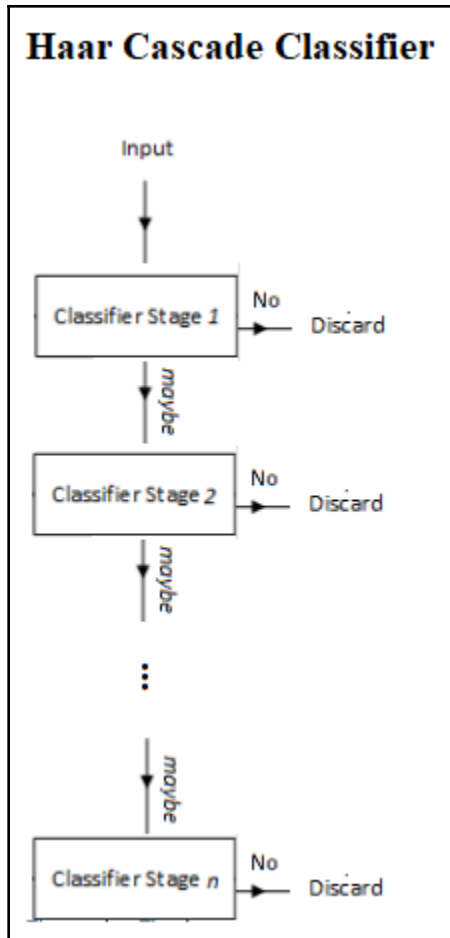
test image

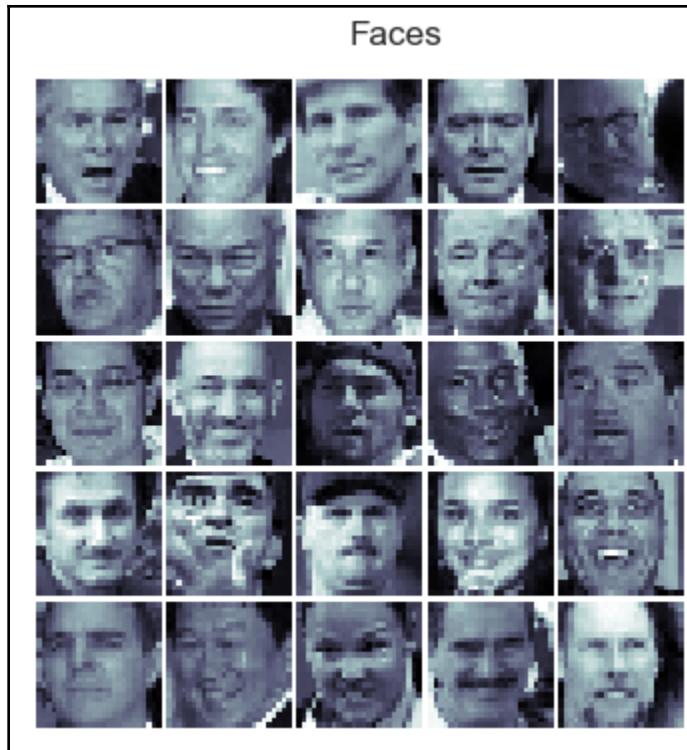


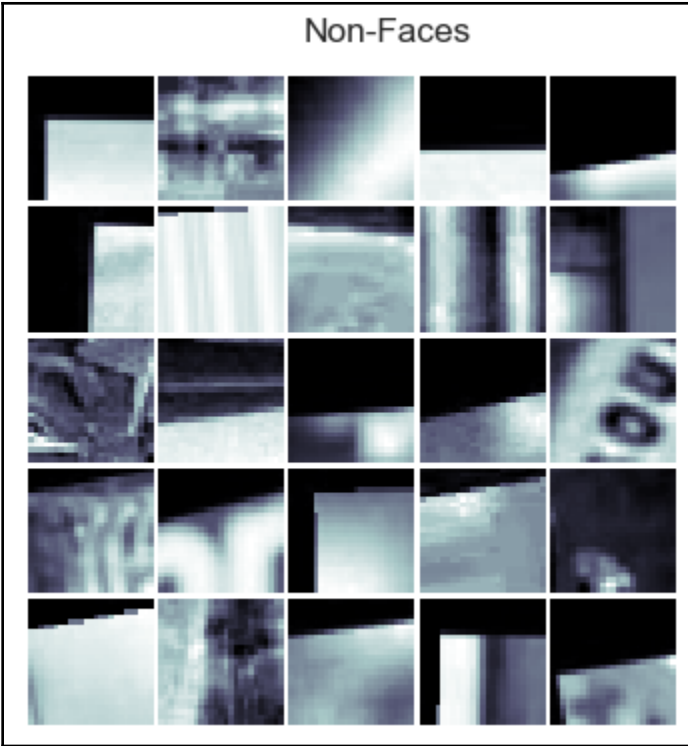
corresponding nearest neighbor image



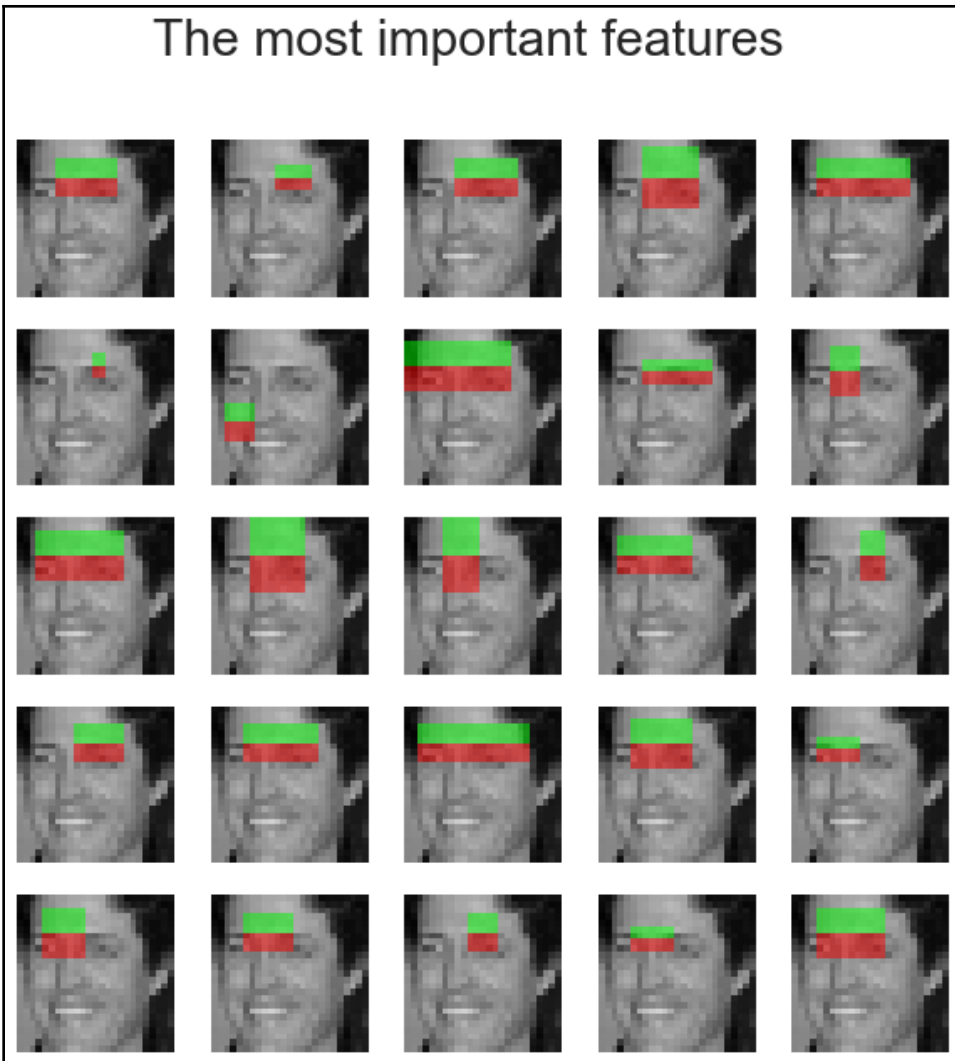


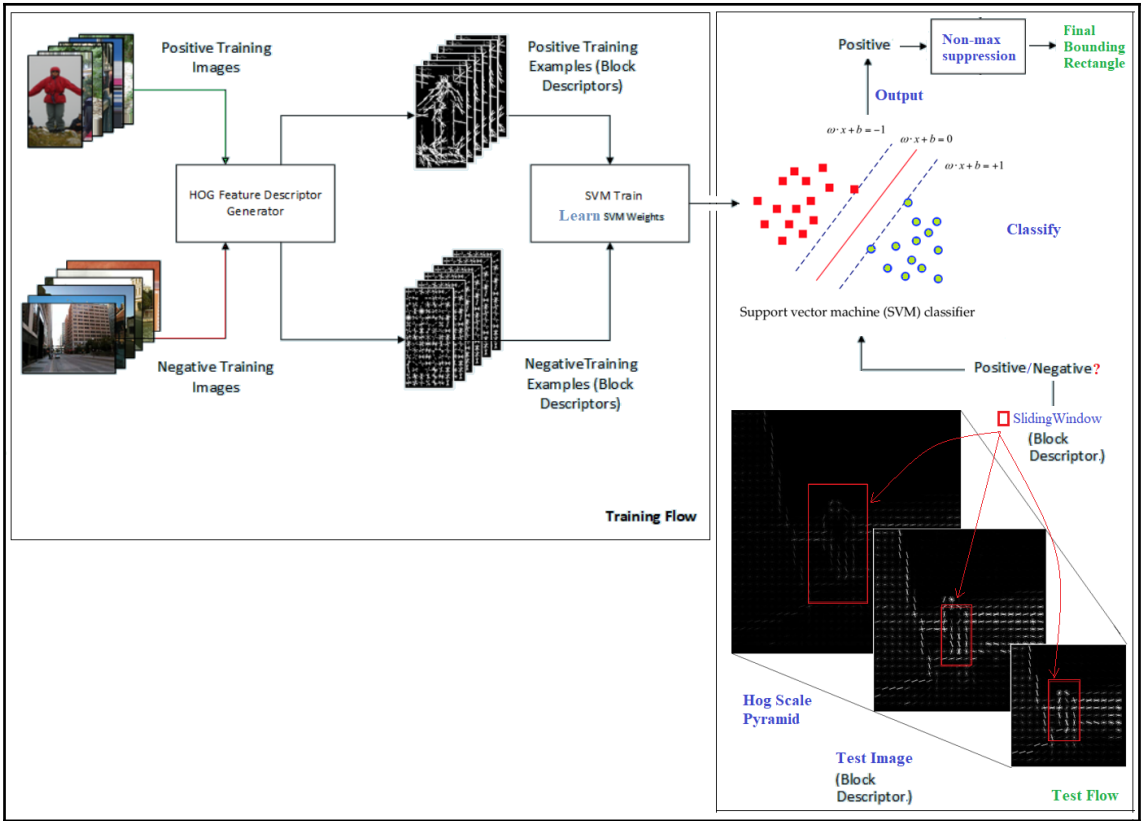






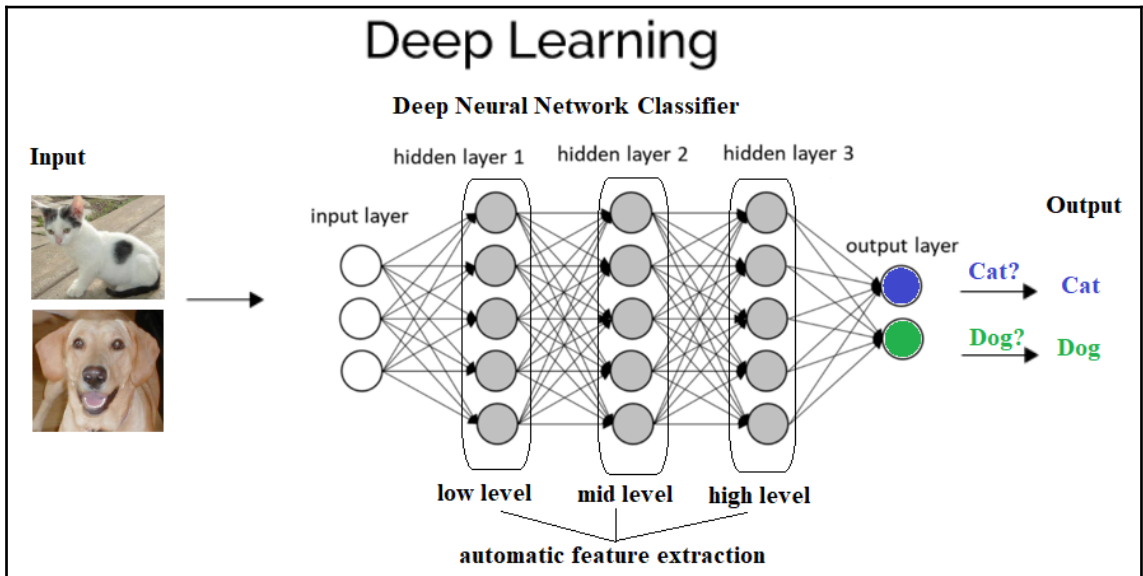
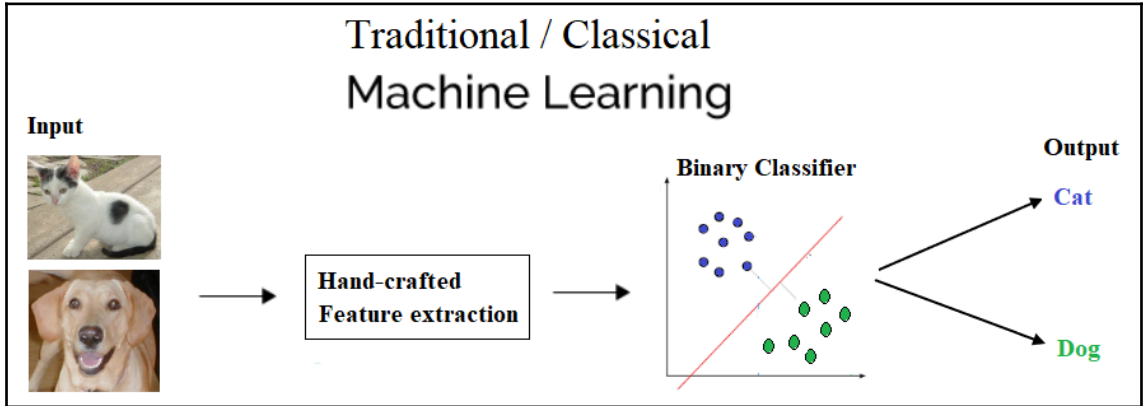
The most important features

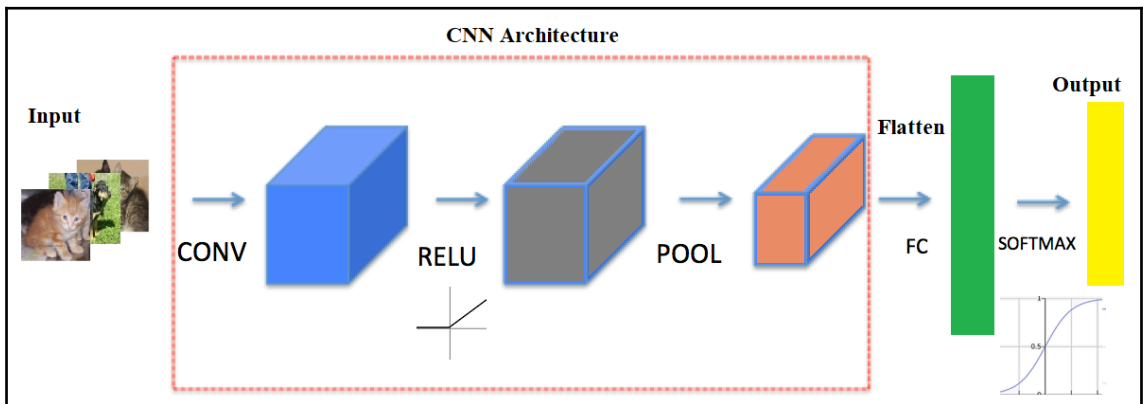
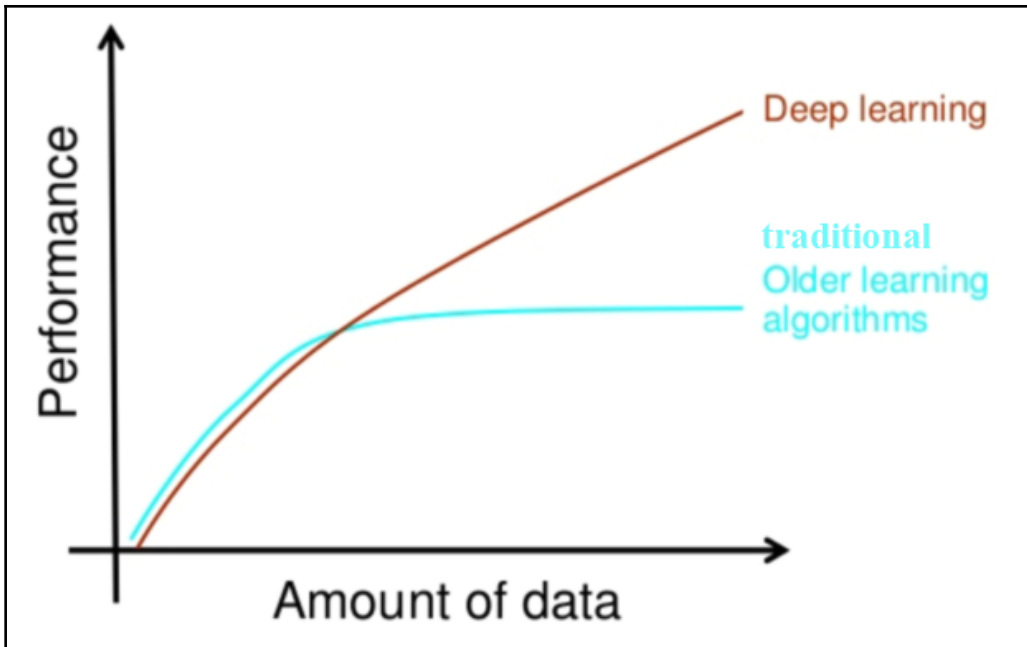


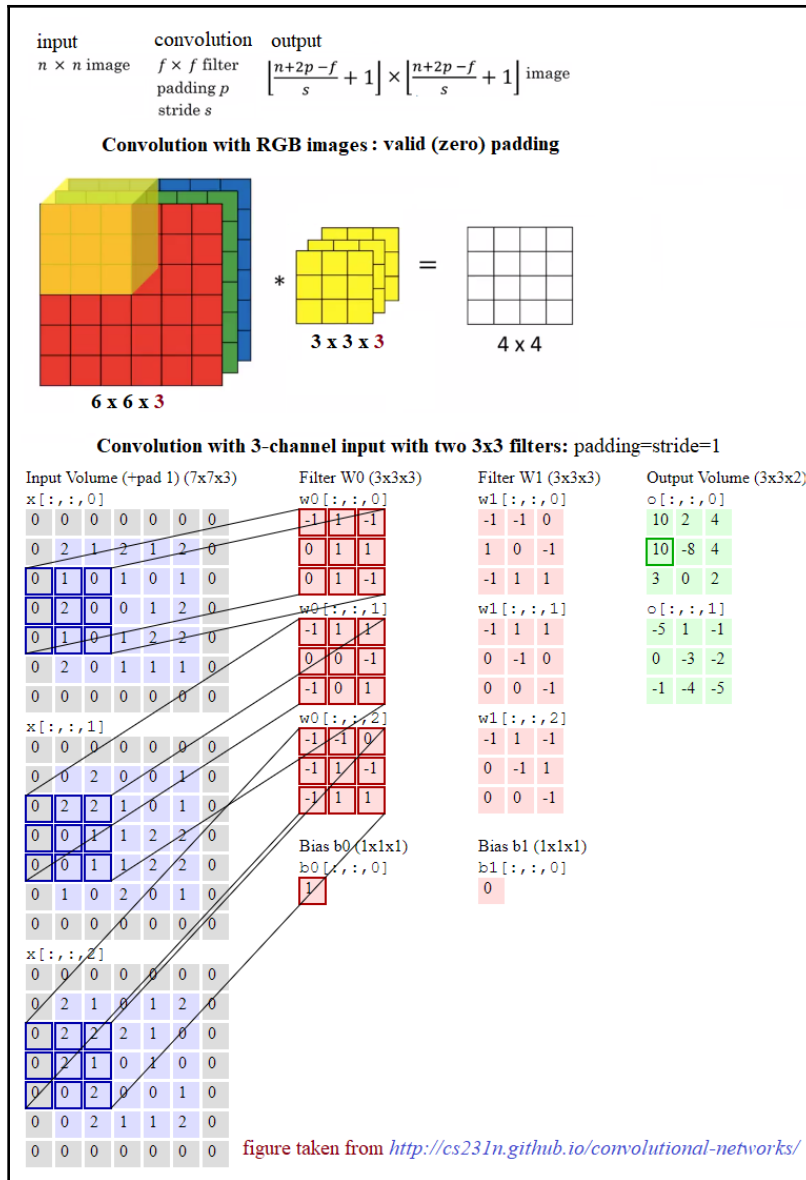


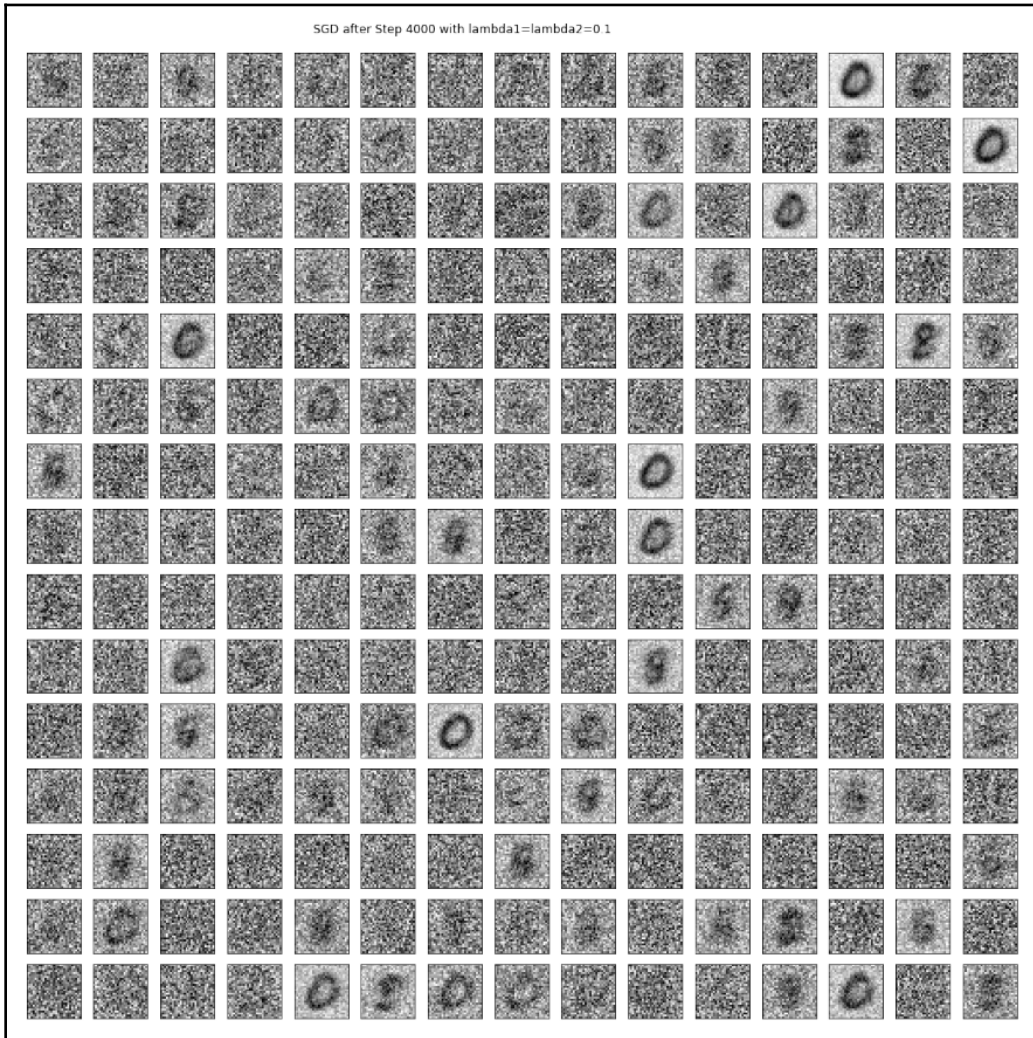
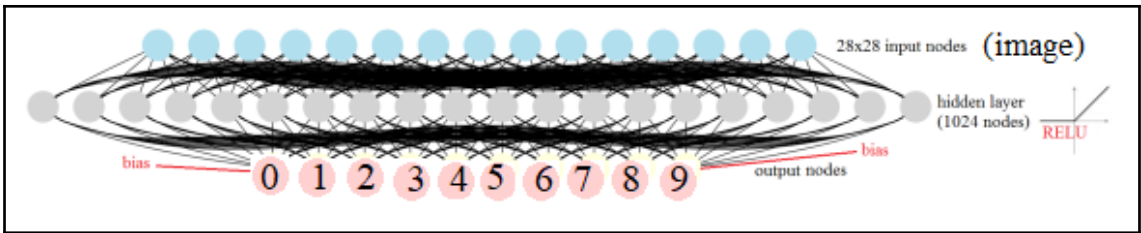


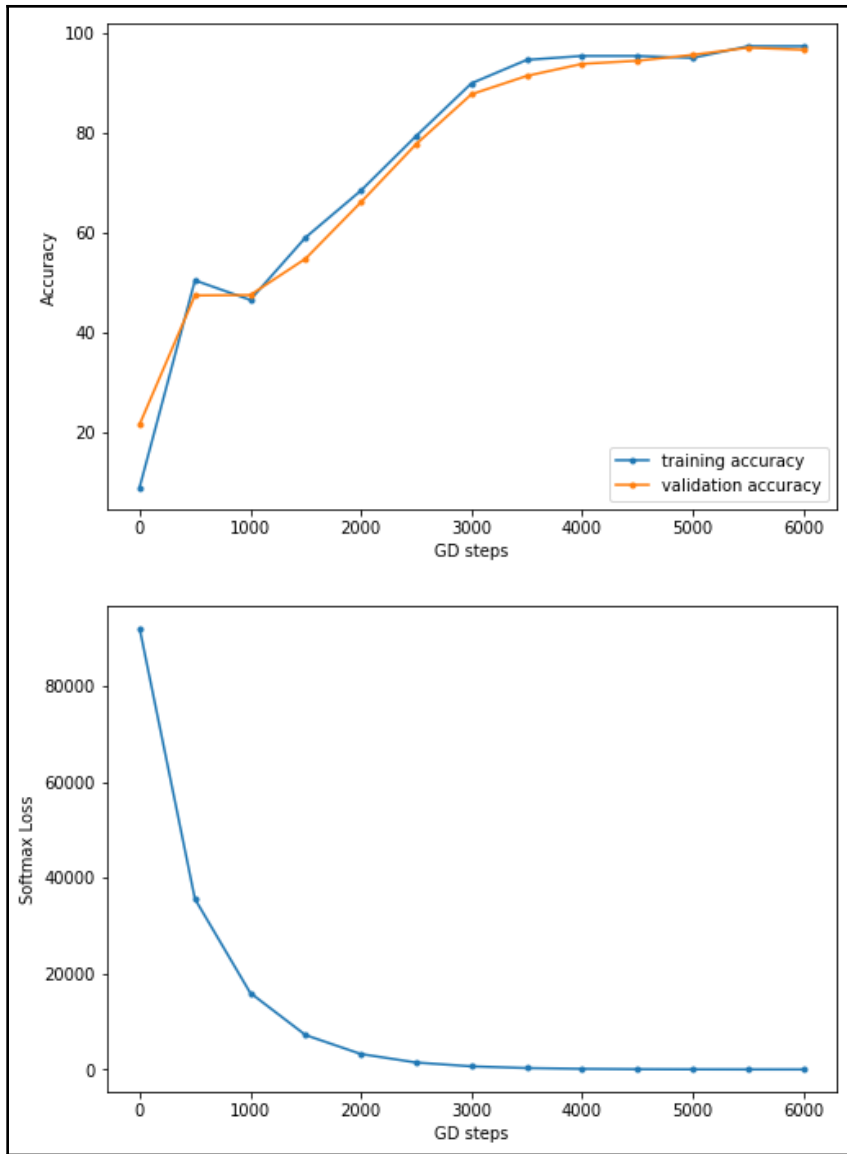
Chapter 10: Deep Learning in Image Processing - Image Classification

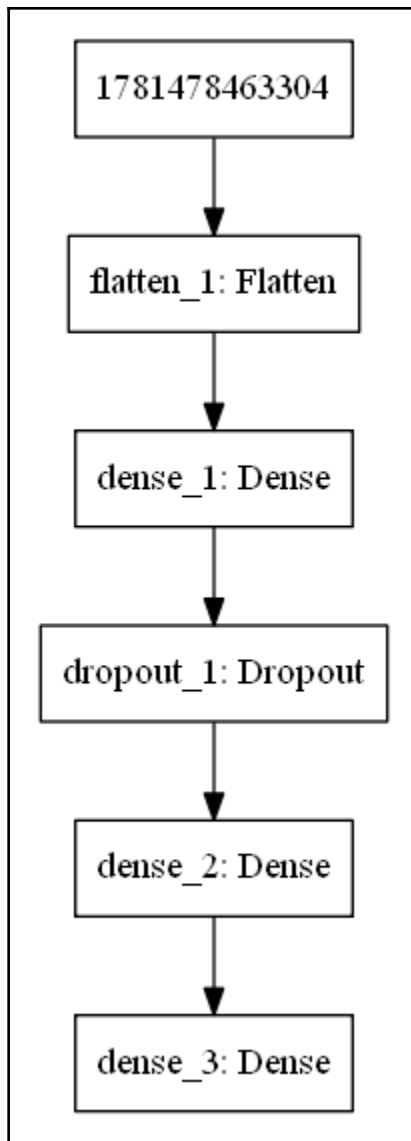


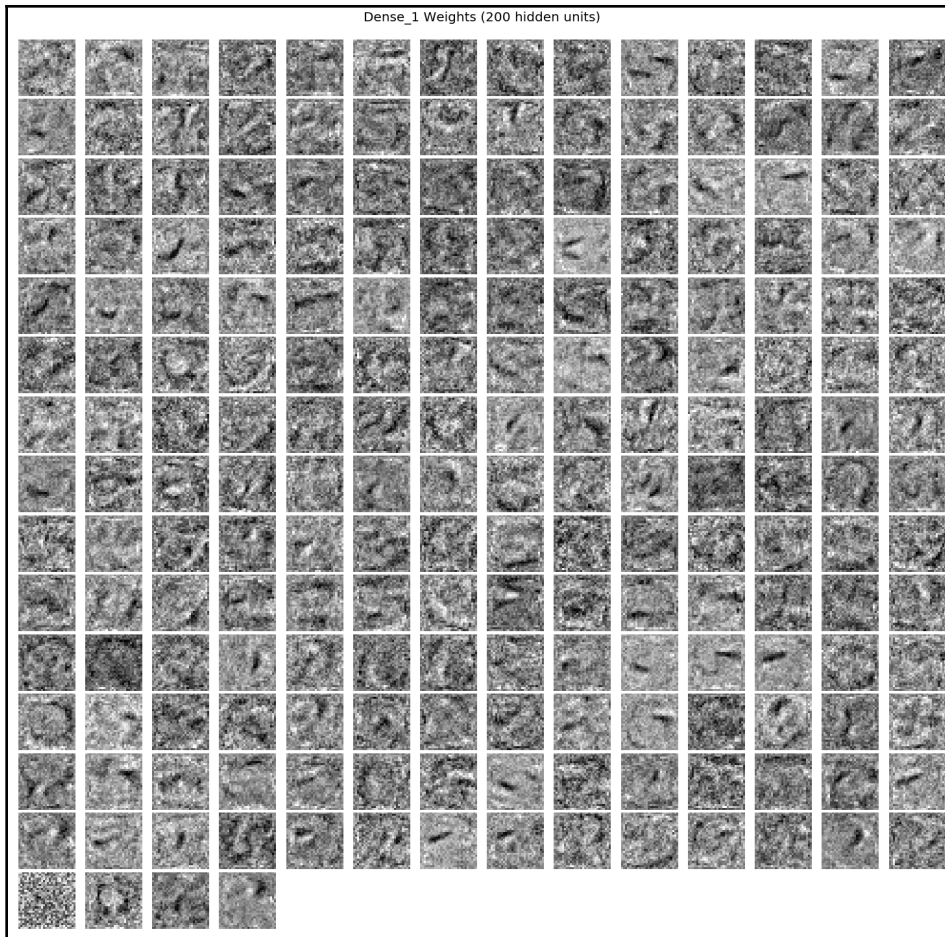


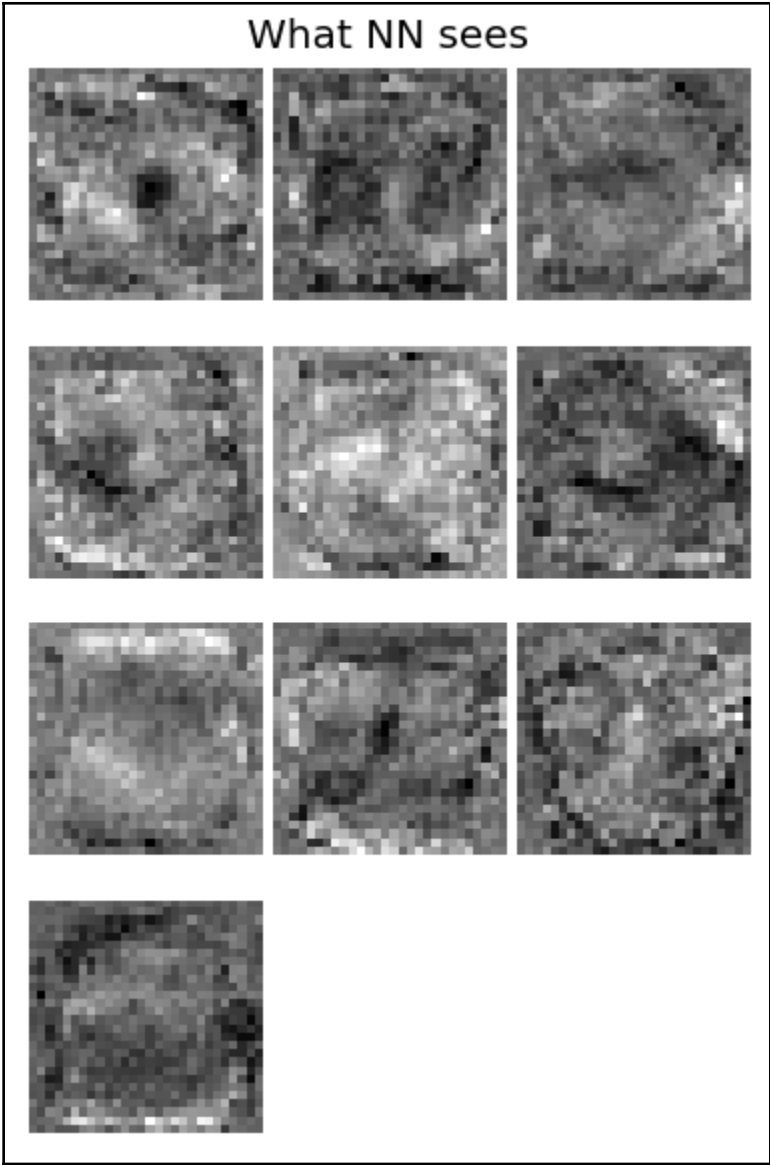


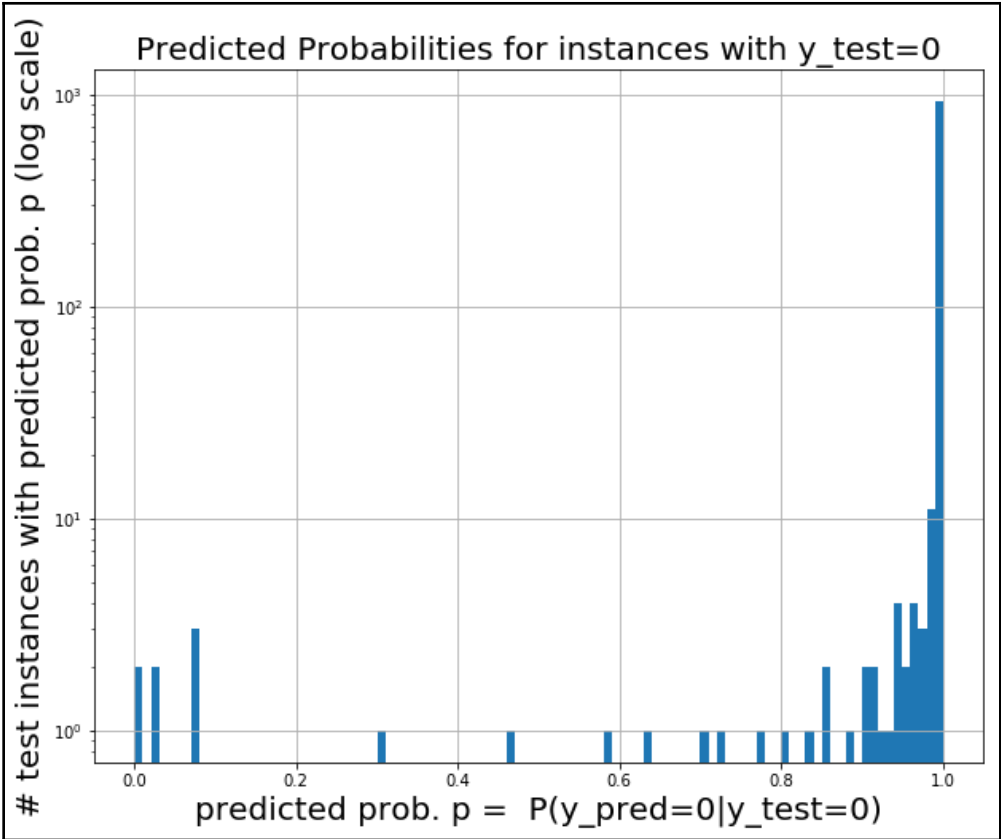


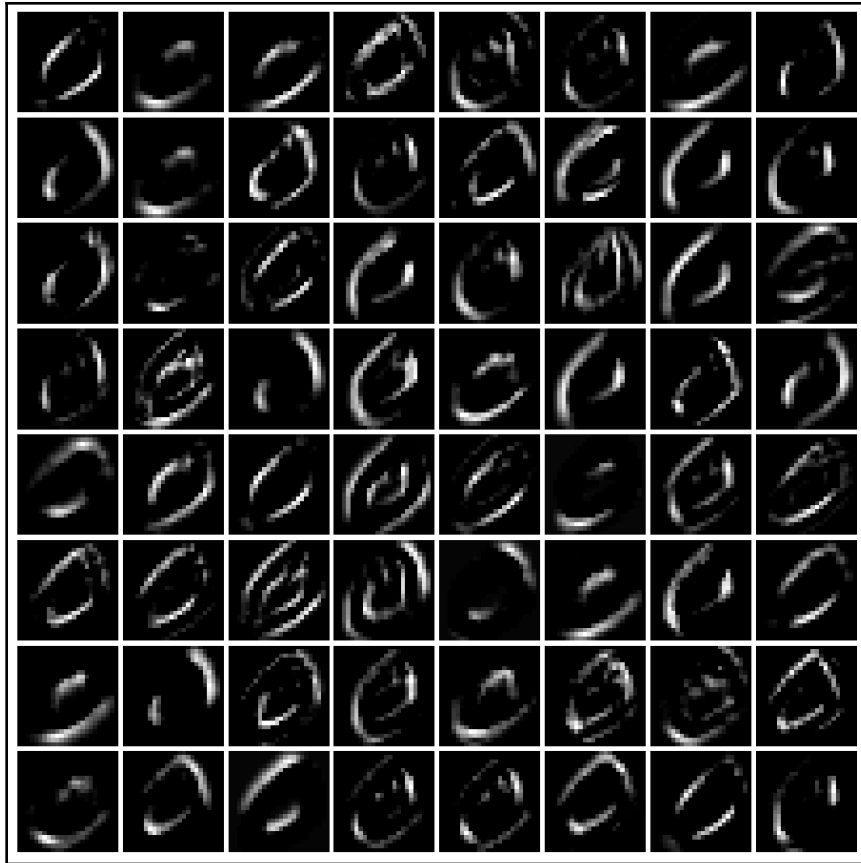


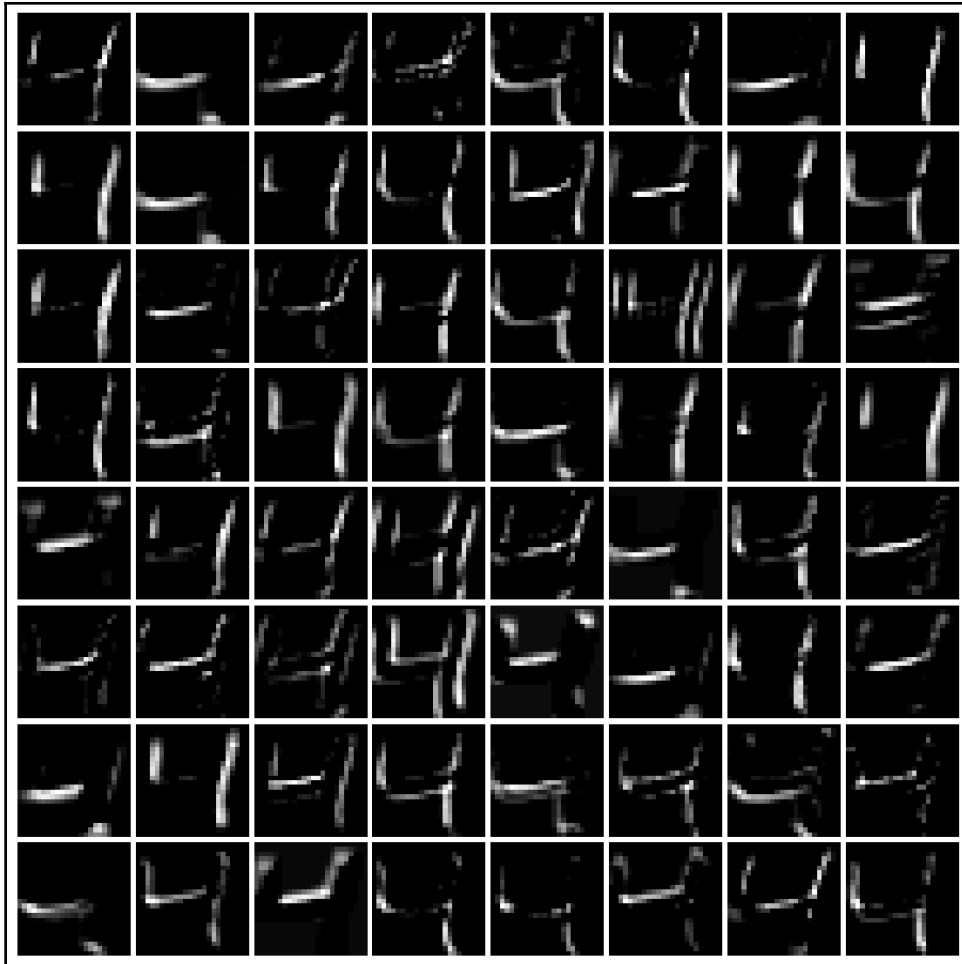


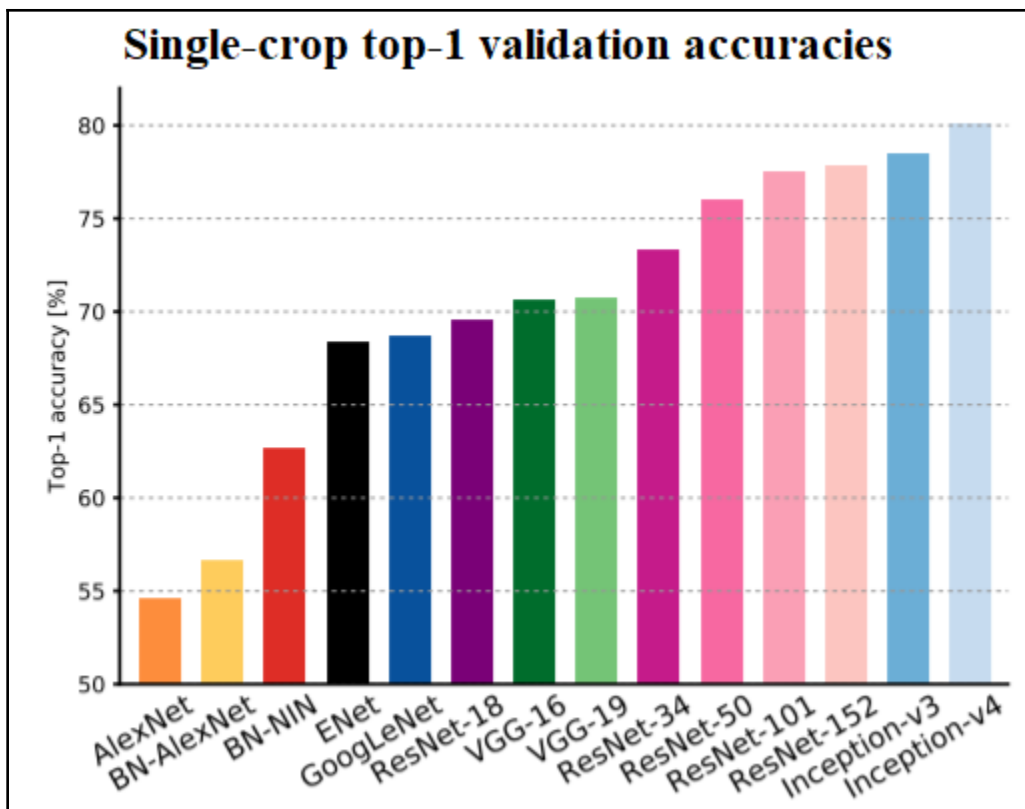


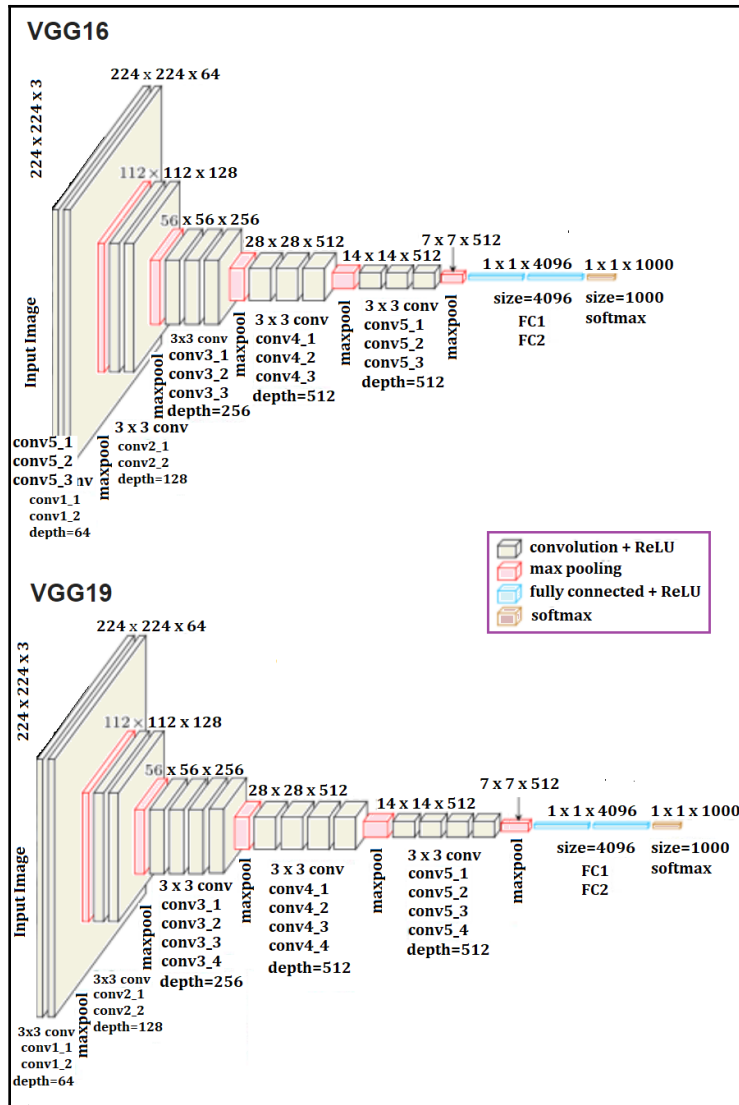


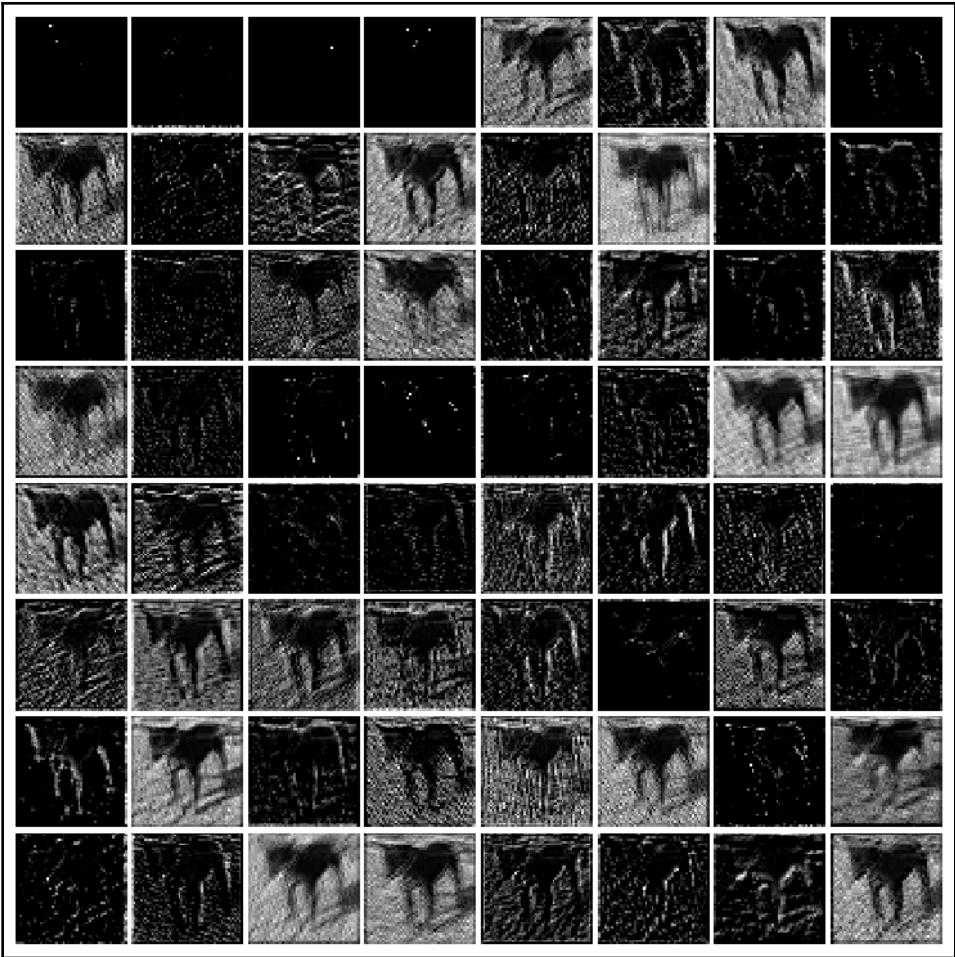


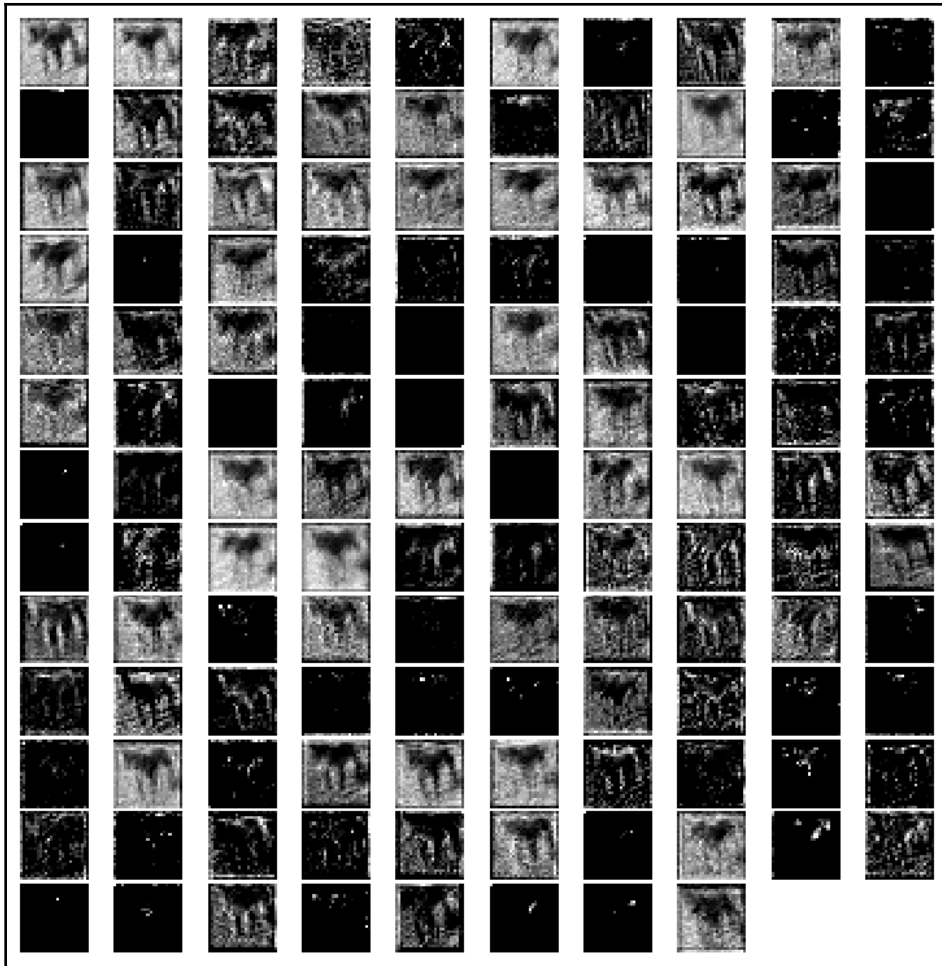




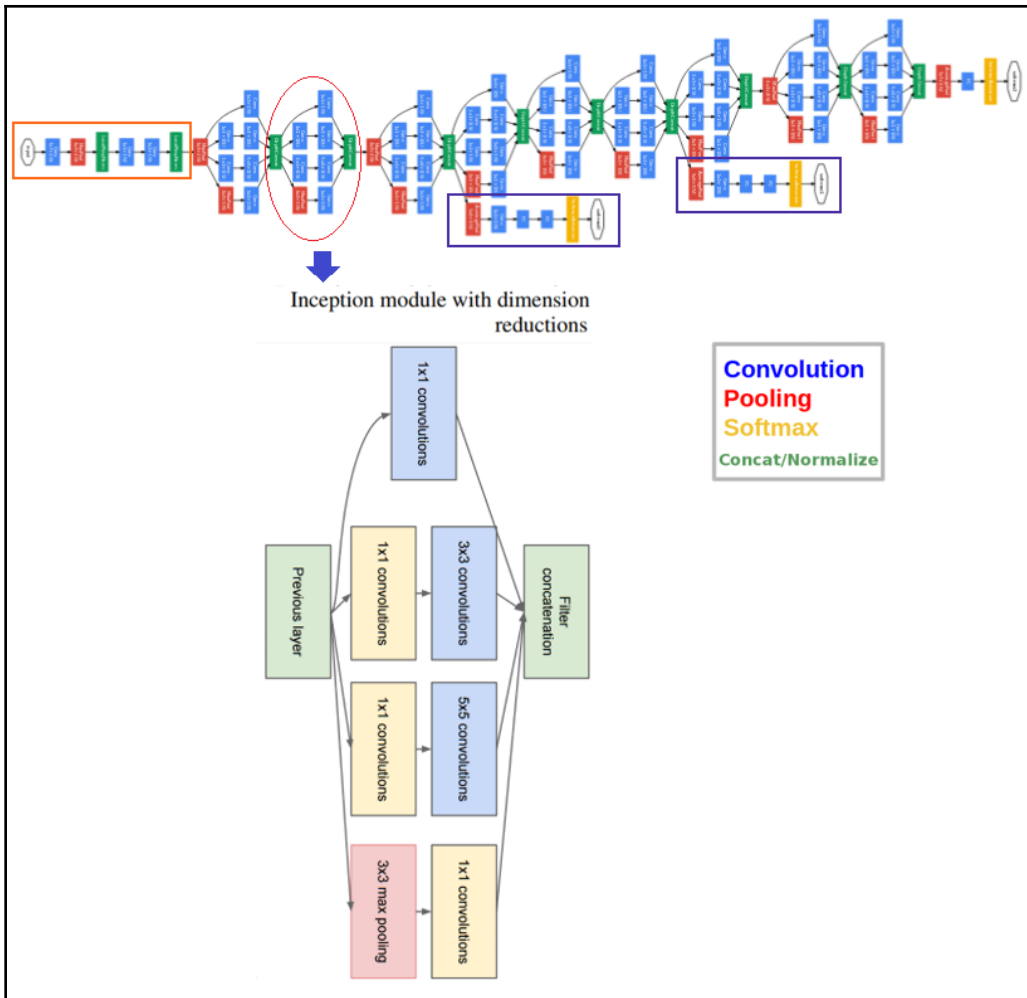


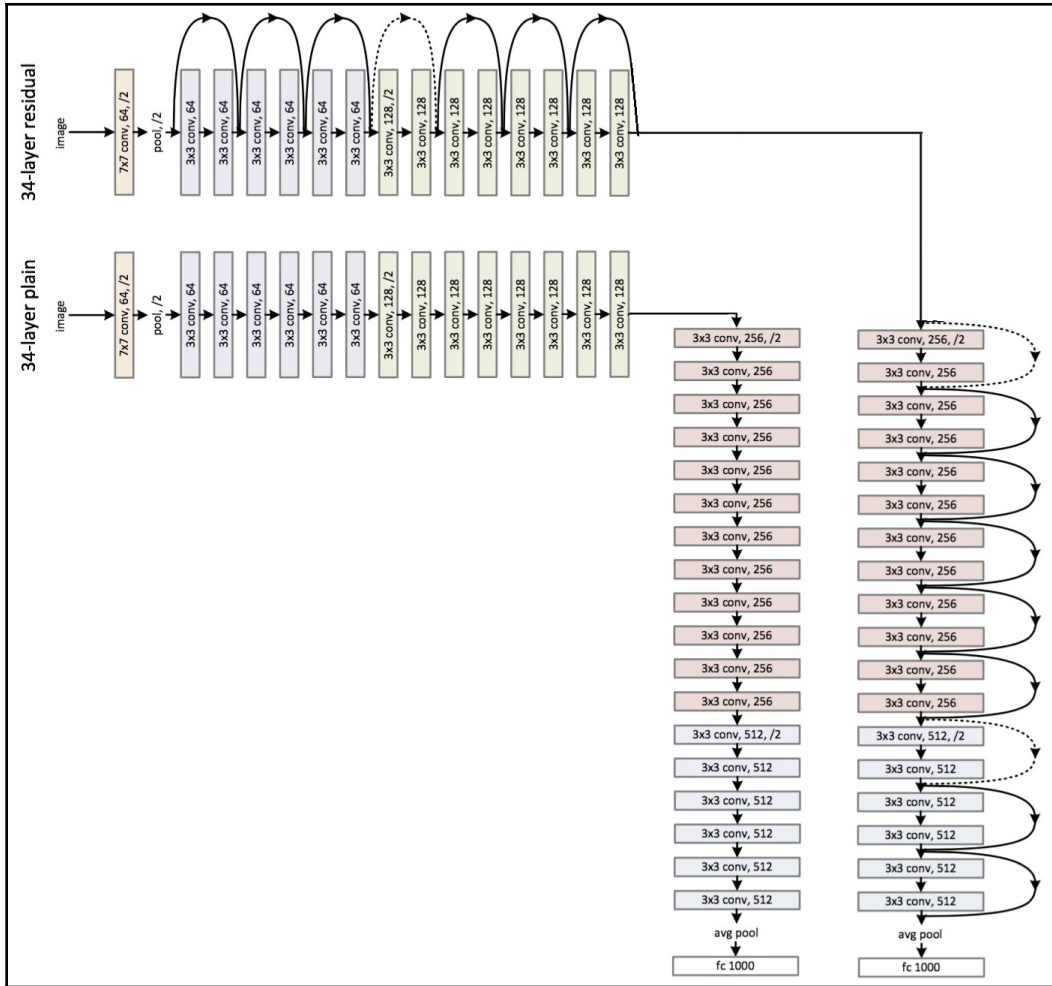




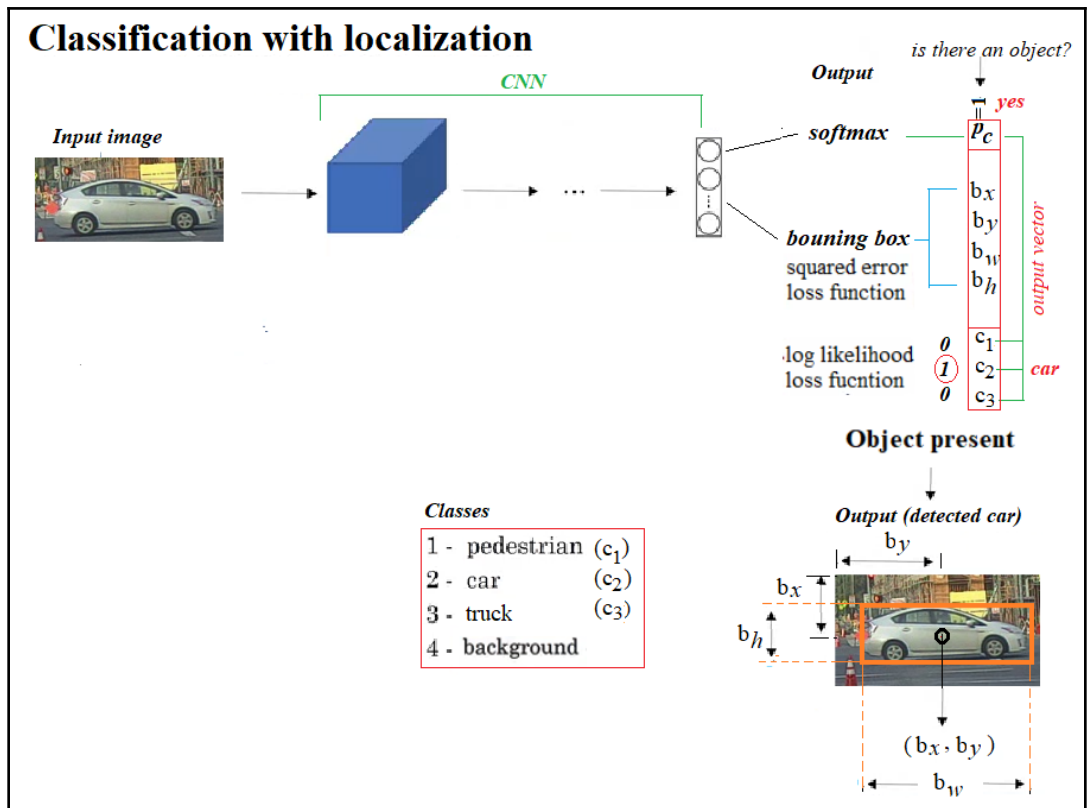
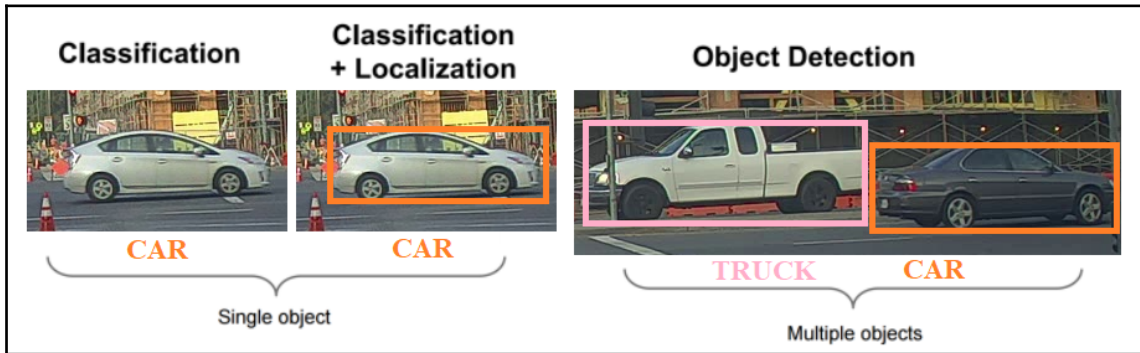






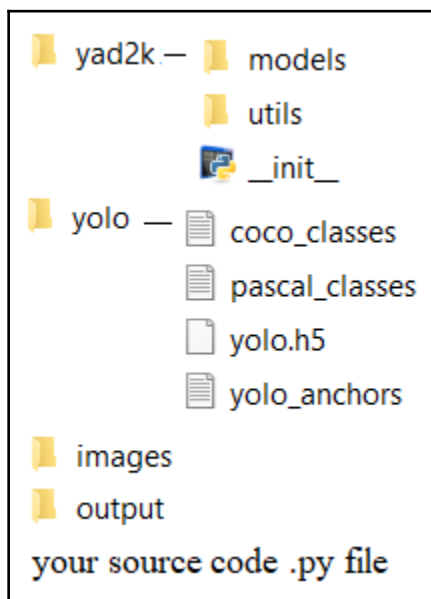


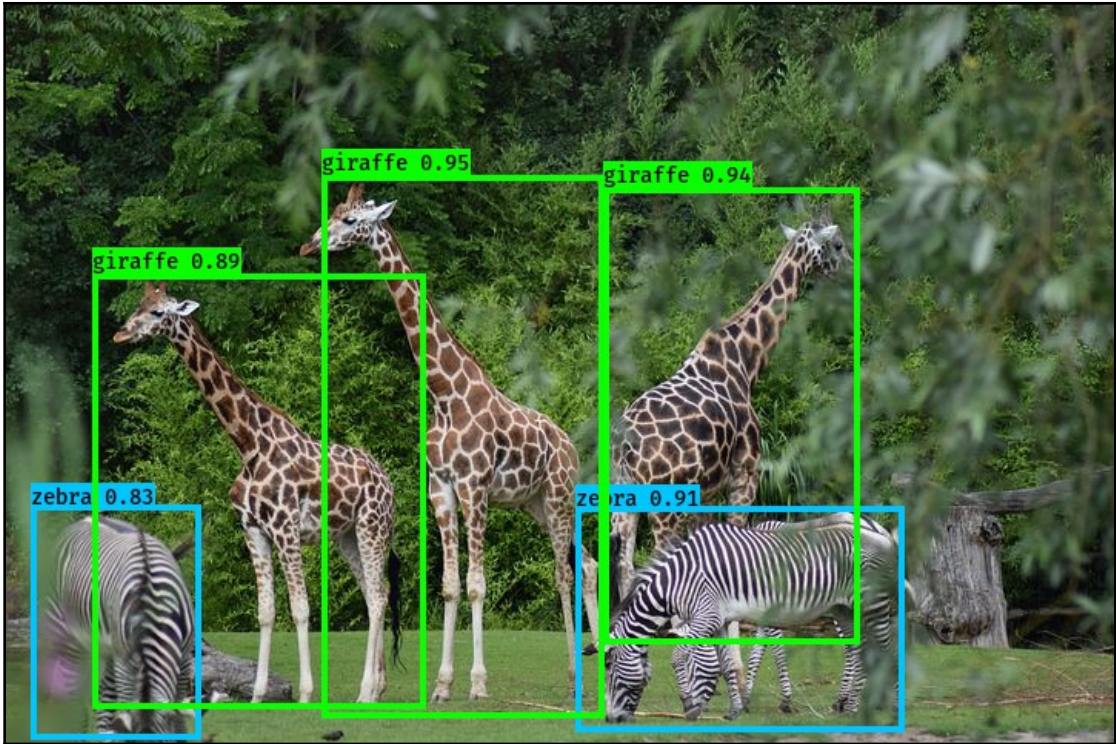
Chapter 11: Deep Learning in Image Processing - Object Detection, and more



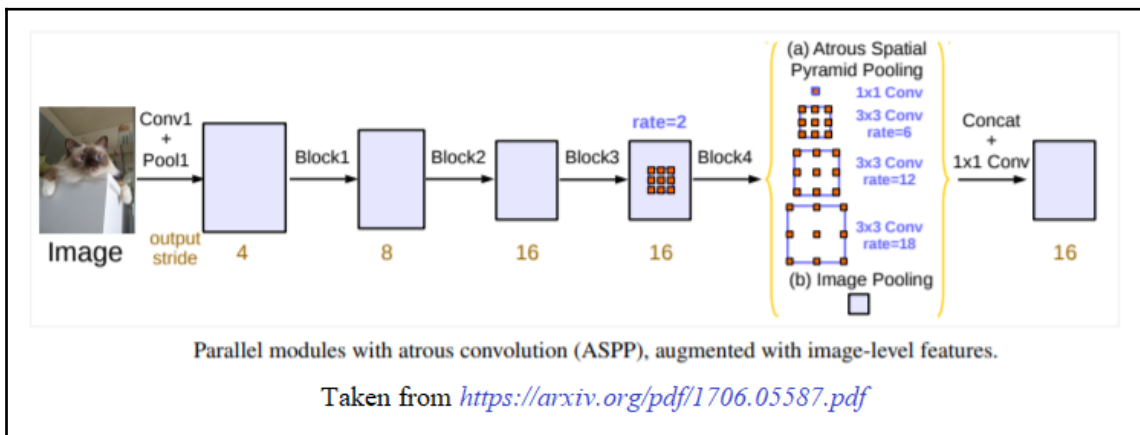
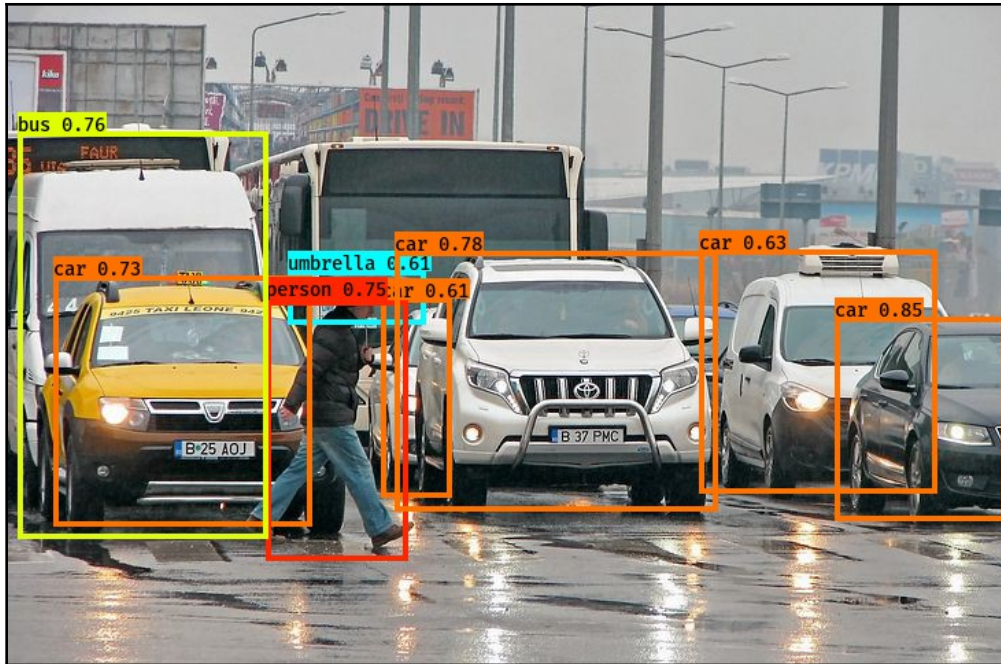
Performance on the COCO Dataset

Model	Train	Test	mAP	FLOPS	FPS	Cfg	Weights
SSD300	COCO trainval	test-dev	41.2	-	46		link
SSD500	COCO trainval	test-dev	46.5	-	19		link
YOLOv2 608x608	COCO trainval	test-dev	48.1	62.94 Bn	40	cfg	weights









Deeplab V3+ architecture

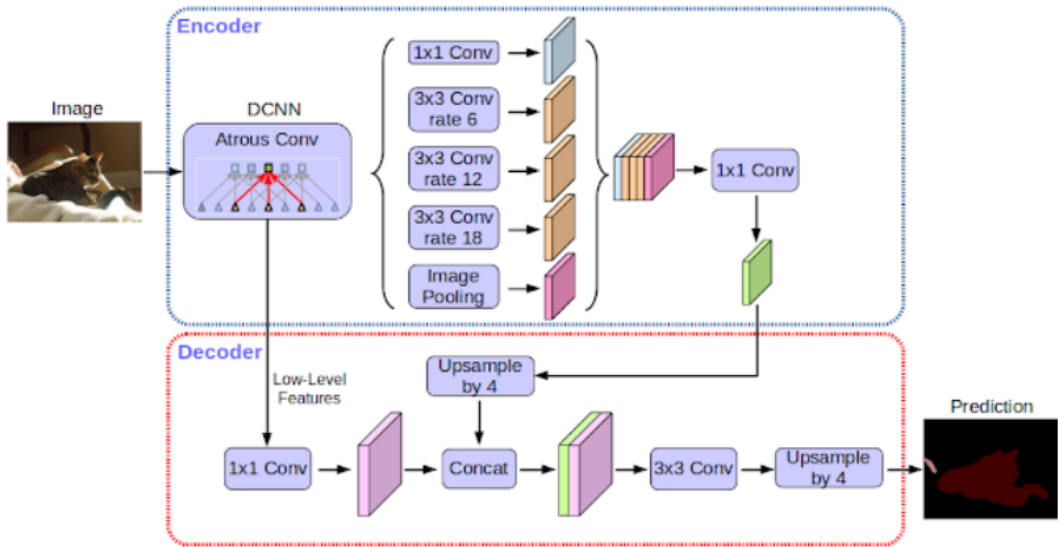


image taken from <https://ai.googleblog.com/2018/03/semantic-image-segmentation->



